

An Introduction to
Mildly Context-Sensitive Grammar Formalisms
— *Minimalist Grammars / Example* —

Gerhard Jäger & Jens Michaelis
Universität Potsdam

`{jaeger,michael}@ling.uni-potsdam.de`

MG-example 2

(α_0) =t.c.*that*

(α_5) v.*laugh*

(α_1) =t.+wh.c. $\emptyset$

(α_6) =n.d.-k.*the*

(α_2) = $\tilde{v}$.+k.t. $\emptyset$

(α_7) =n.d.-k.-wh.*which*

(α_3) =v.=d. $\tilde{v}$. $\emptyset$

(α_8) n.*king*

(α_4) =d.+k.v.*eat*

(α_9) n.*pie*

MG-example 2

(α_7) =n.d.-k.-wh.*which*

(α_9) n.*pie*

MG-example 2

(α_7) =n.d.-k.-wh.*which*

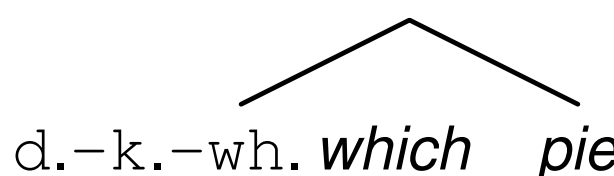
(α_9) n.*pie*

MG-example 2

(α_7) =n.d.-k.-wh.*which*

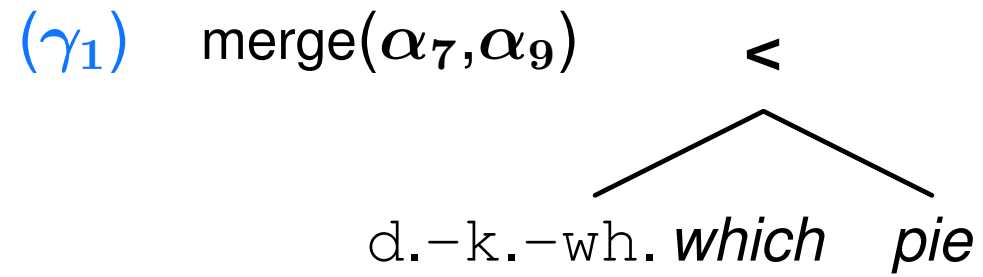
(α_9) n.*pie*

(γ_1) merge(α_7, α_9)



```
graph TD; A["<"] --- B["d.-k.-wh. which"]; A --- C["pie"]
```

MG-example 2



MG-example 2

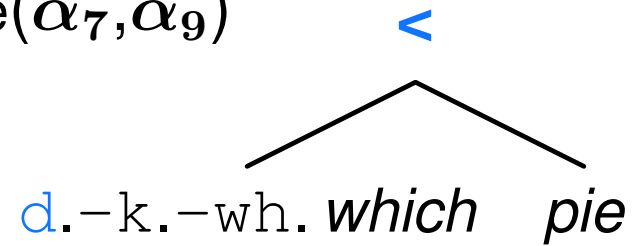
(γ_1) merge(α_7, α_9)

<

d.-k.-wh. *which* *pie*

MG-example 2

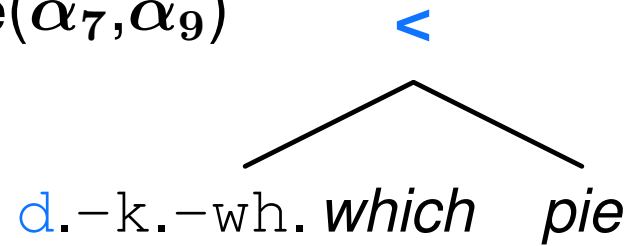
(γ_1) merge(α_7, α_9)



(α_4) =d.+k.v.*eat*

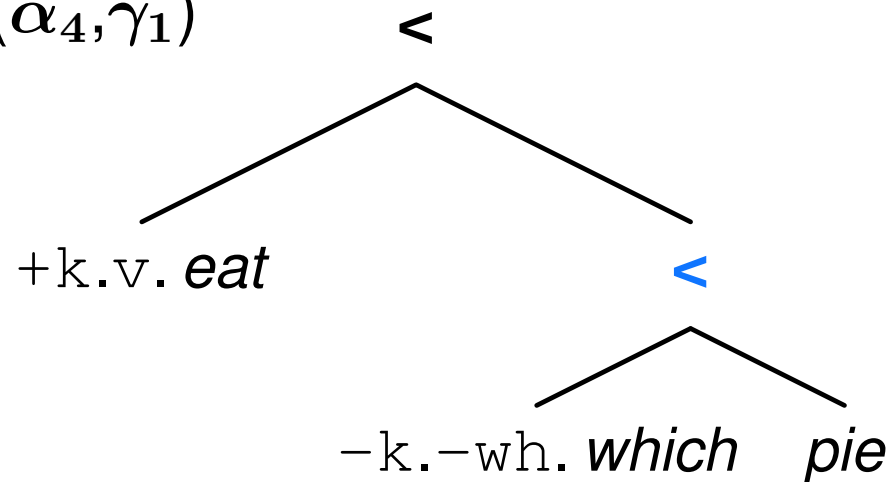
MG-example 2

(γ_1) merge(α_7, α_9)



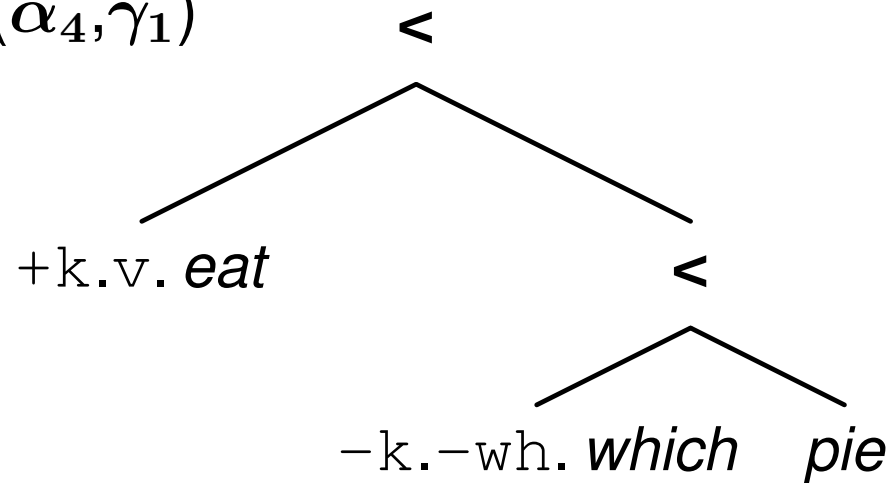
(α_4) =d.+k.v.*eat*

(γ_2) merge(α_4, γ_1)



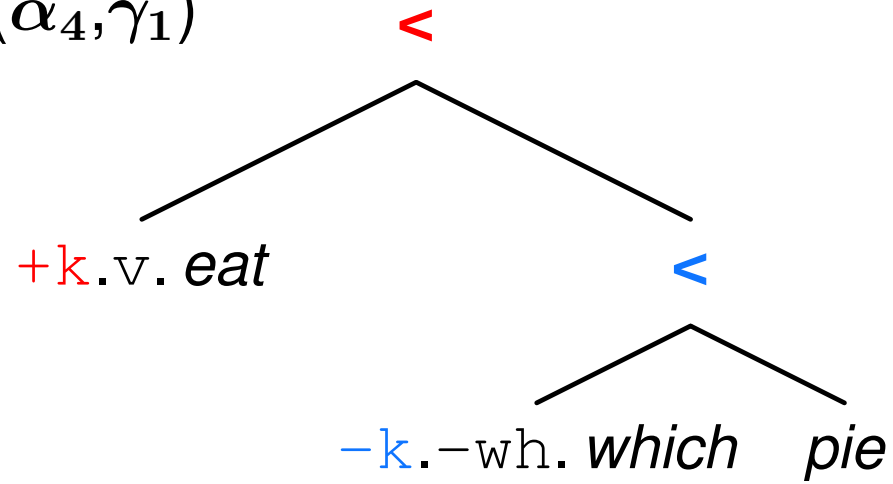
MG-example 2

(γ_2) merge(α_4, γ_1)



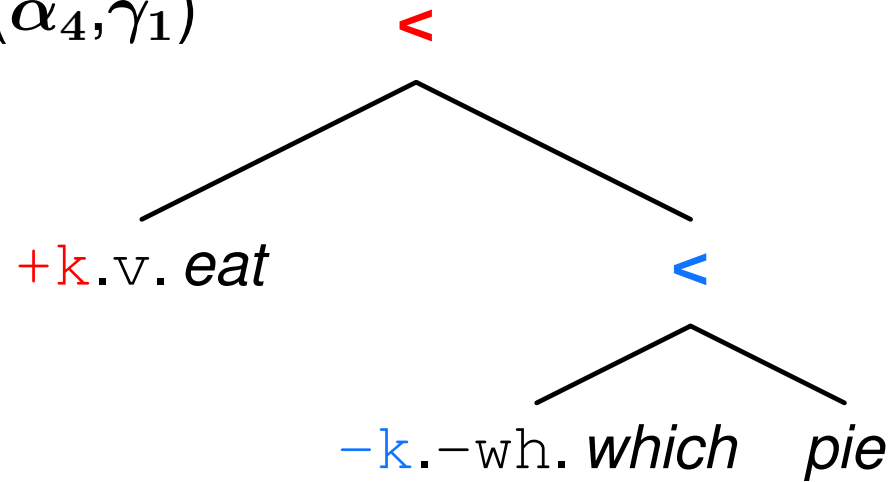
MG-example 2

(γ_2) merge(α_4, γ_1)

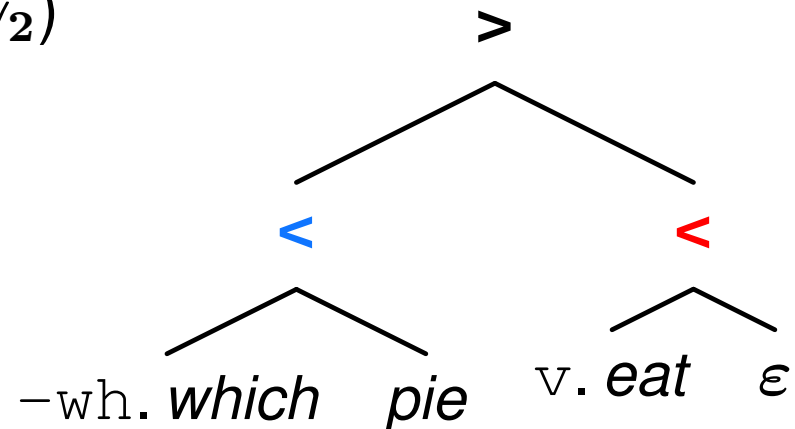


MG-example 2

(γ_2) $\text{merge}(\alpha_4, \gamma_1)$

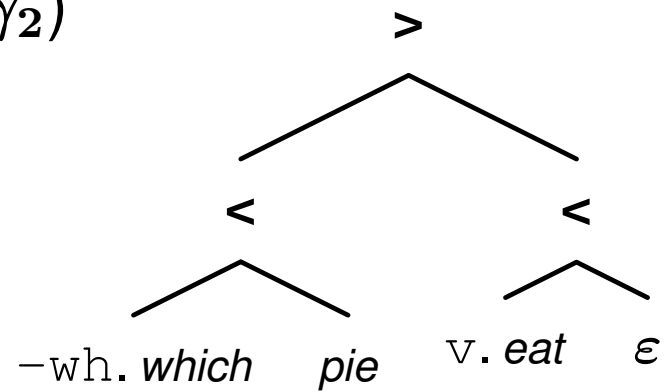


(γ_3) $\text{move}(\gamma_2)$



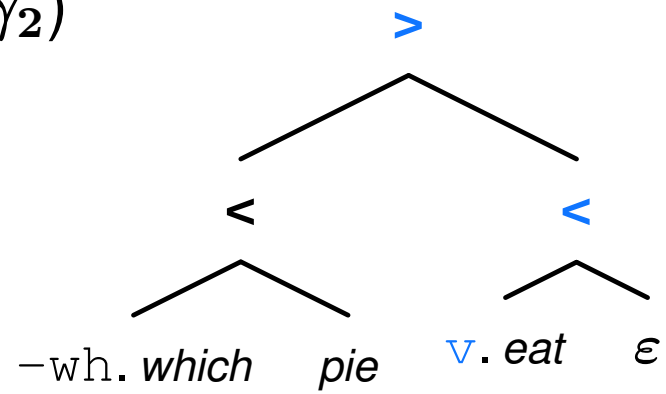
MG-example 2

(γ_3) move(γ_2)



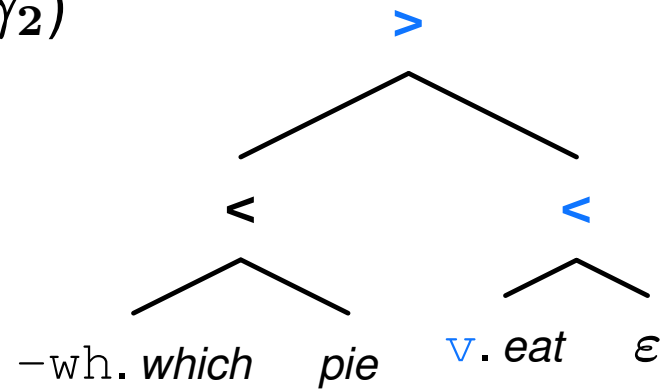
MG-example 2

(γ_3) move(γ_2)



MG-example 2

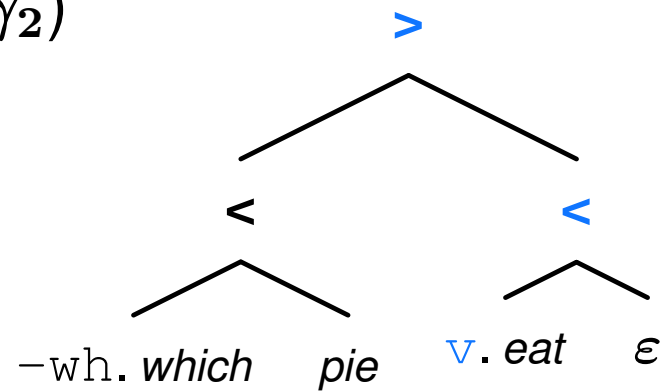
(γ_3) move(γ_2)



(α_3) $=v.=d.\tilde{v}.\emptyset$

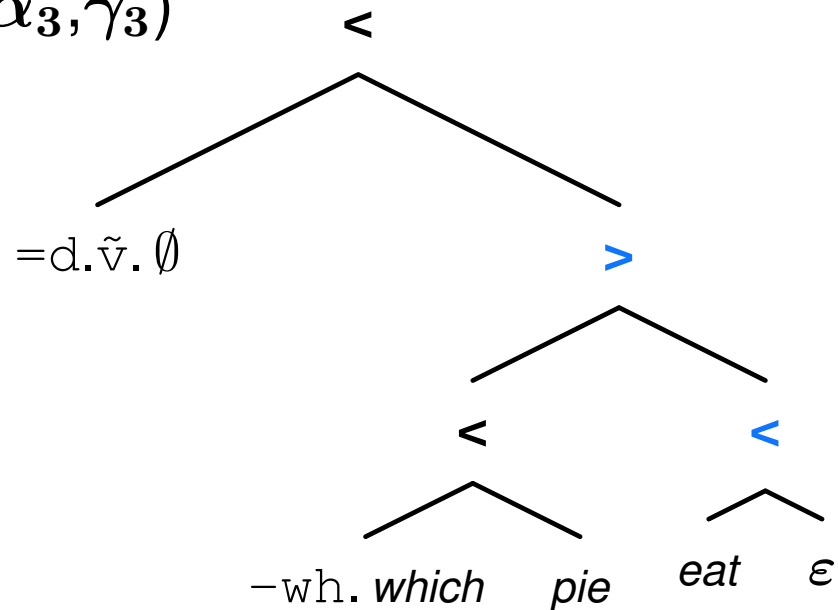
MG-example 2

(γ_3) $\text{move}(\gamma_2)$



(α_3) $=v.=d.\tilde{v}.\emptyset$

(γ_4) $\text{merge}(\alpha_3, \gamma_3)$



MG-example 2

(α_6) =n.d.-k. *the*

(α_8) n. *king*

MG-example 2

(α_6) =n.d.-k. *the*

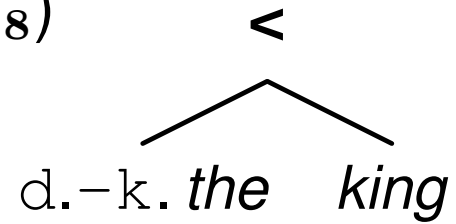
(α_8) n. *king*

MG-example 2

(α_6) =n.d.-k. *the*

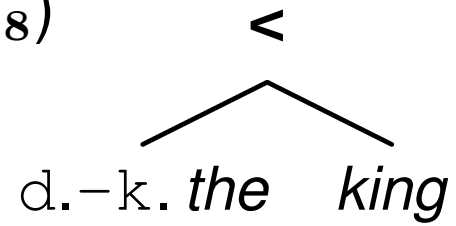
(α_8) n. *king*

(γ_5) merge(α_6, α_8)



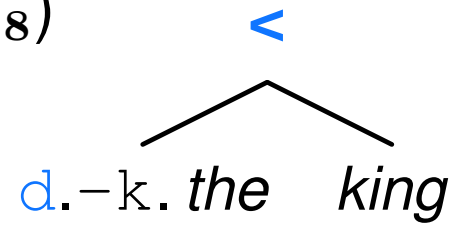
MG-example 2

(γ_5) merge(α_6, α_8)



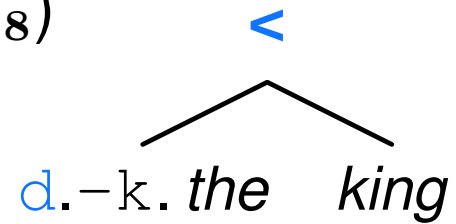
MG-example 2

(γ_5) merge(α_6, α_8)

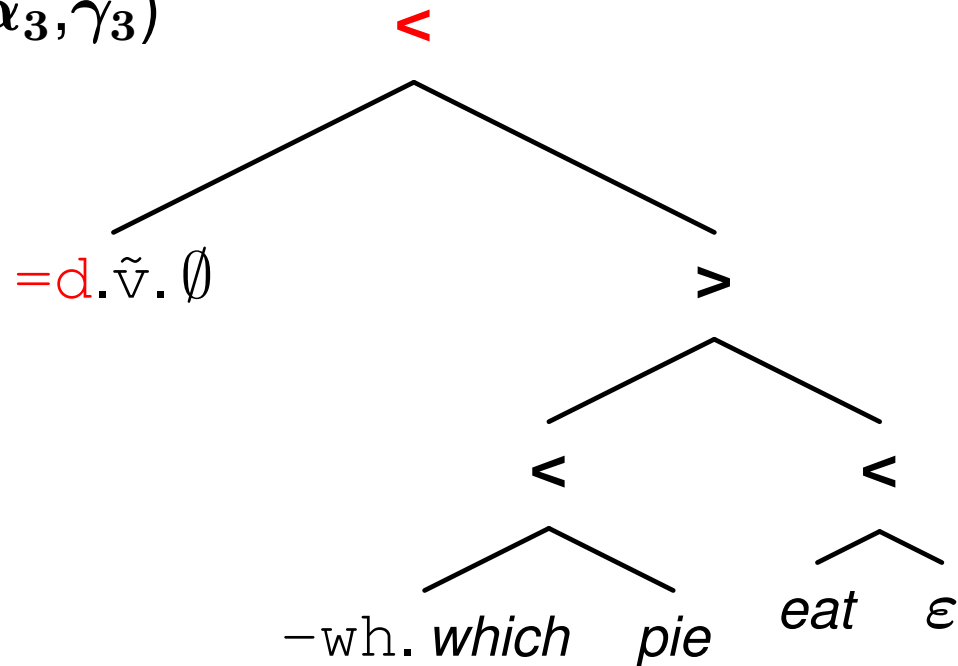


MG-example 2

(γ_5) $\text{merge}(\alpha_6, \alpha_8)$

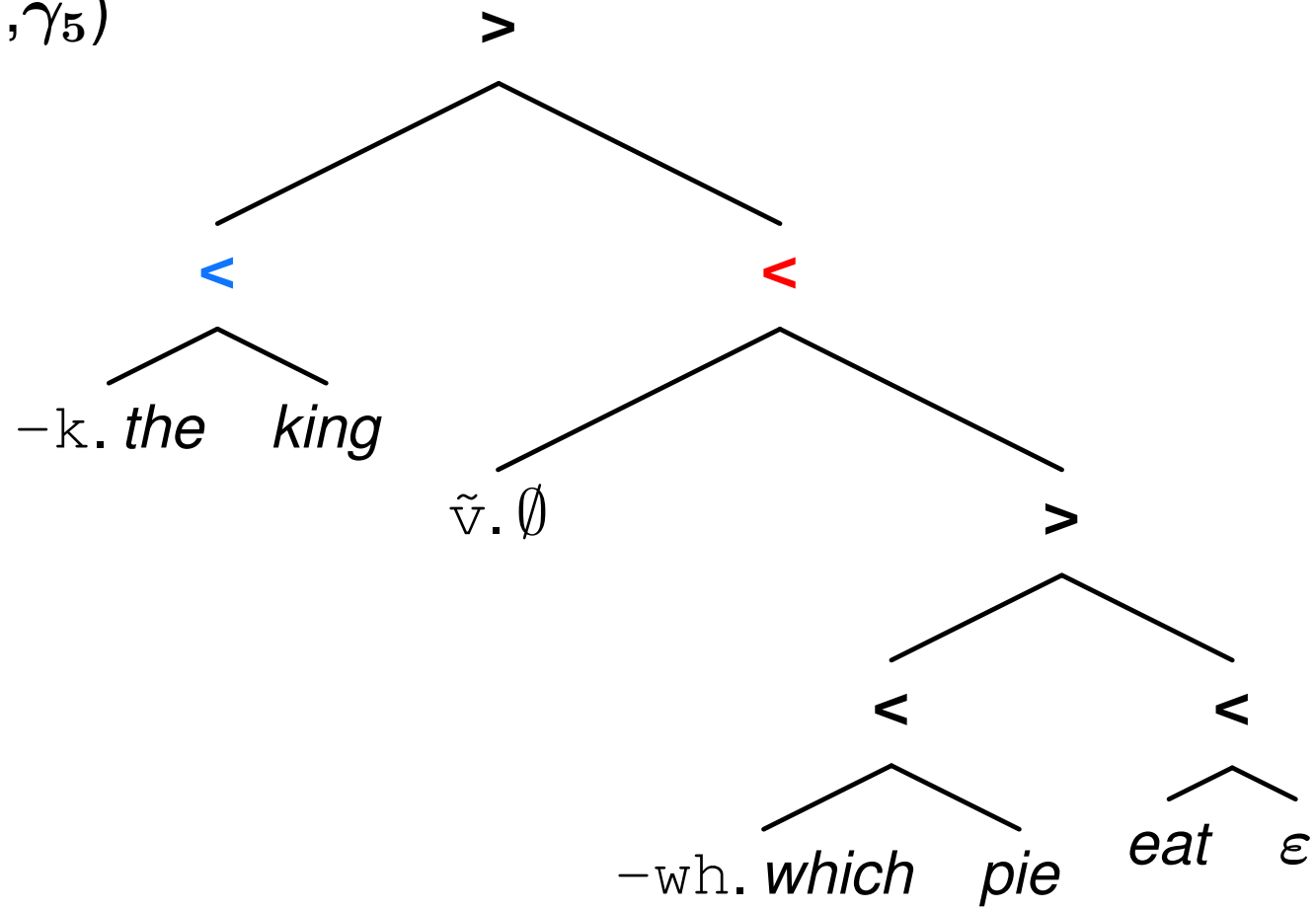


(γ_4) $\text{merge}(\alpha_3, \gamma_3)$



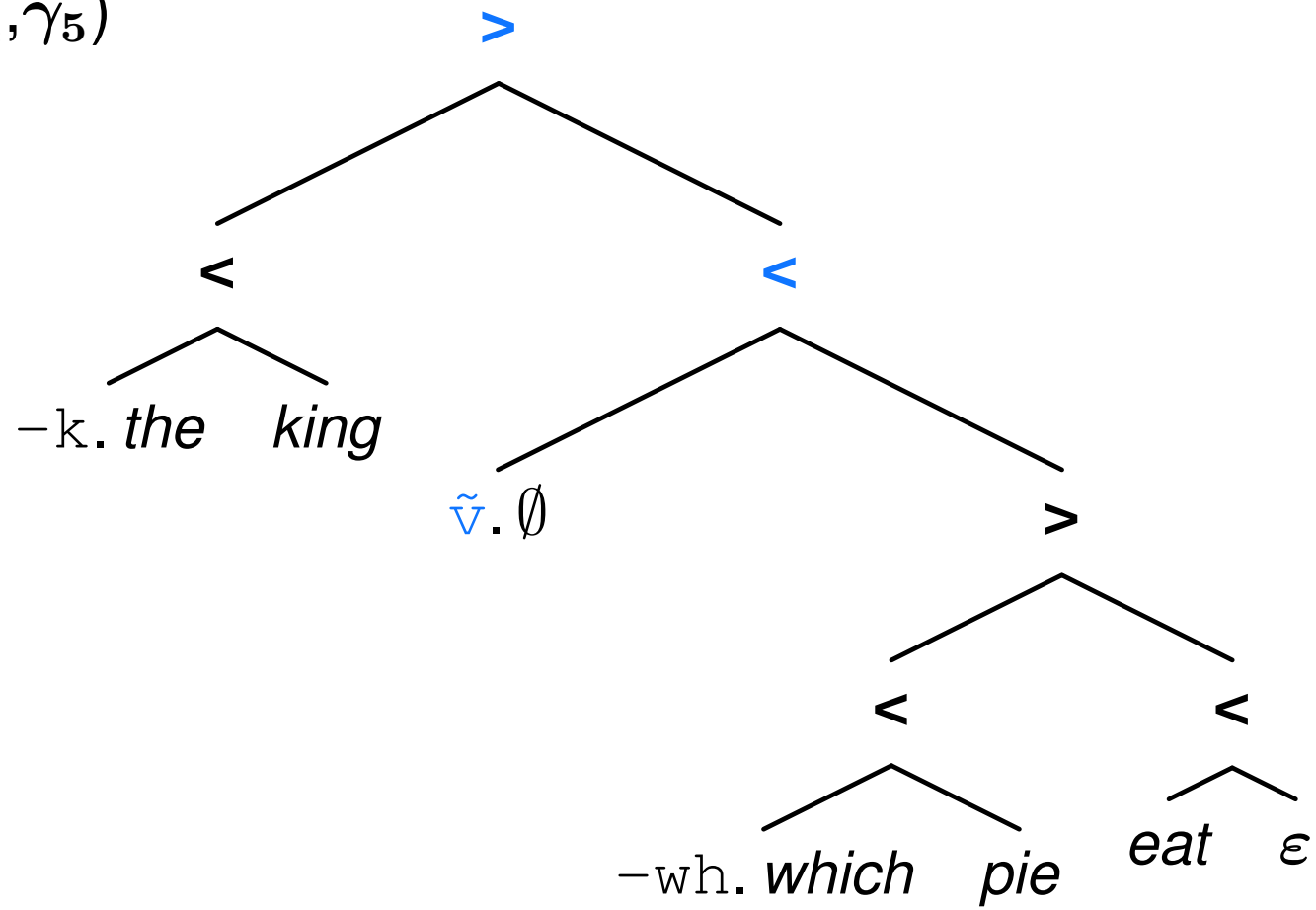
MG-example 2

(γ_6) $\text{merge}(\gamma_4, \gamma_5)$



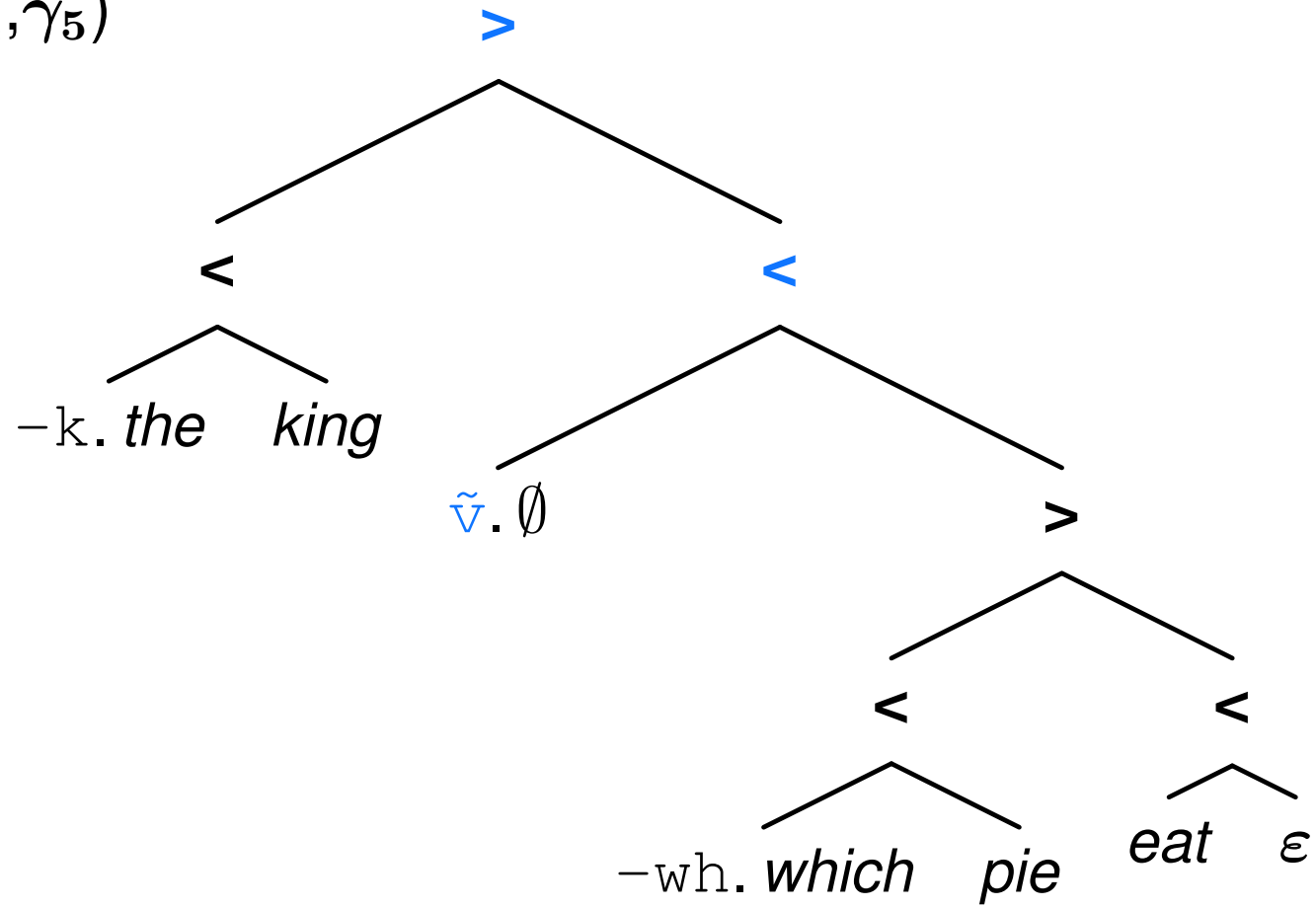
MG-example 2

(γ_6) $\text{merge}(\gamma_4, \gamma_5)$



MG-example 2

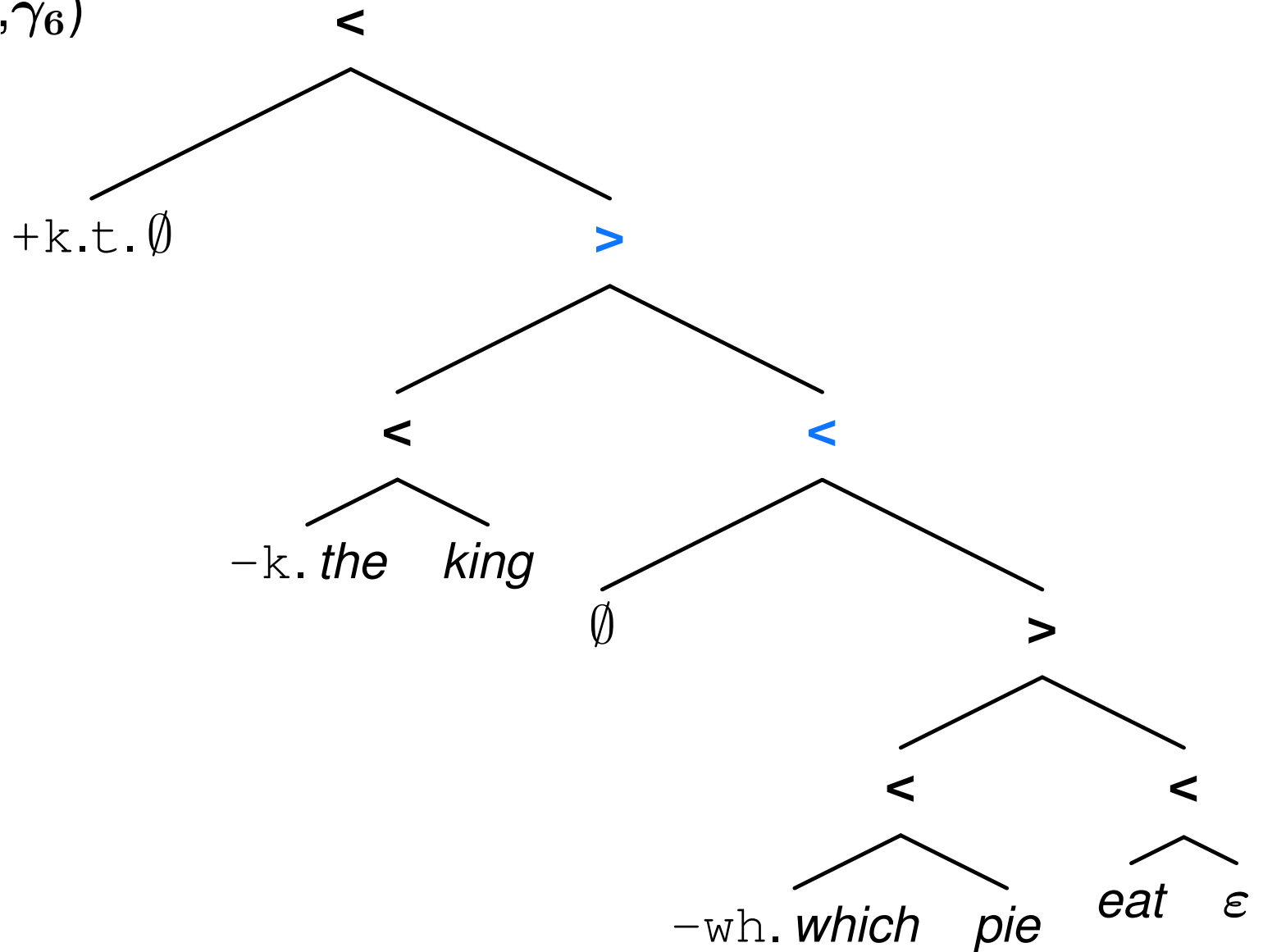
(γ_6) merge(γ_4, γ_5)



(α_2) $= \tilde{v}. +k.t. \emptyset$

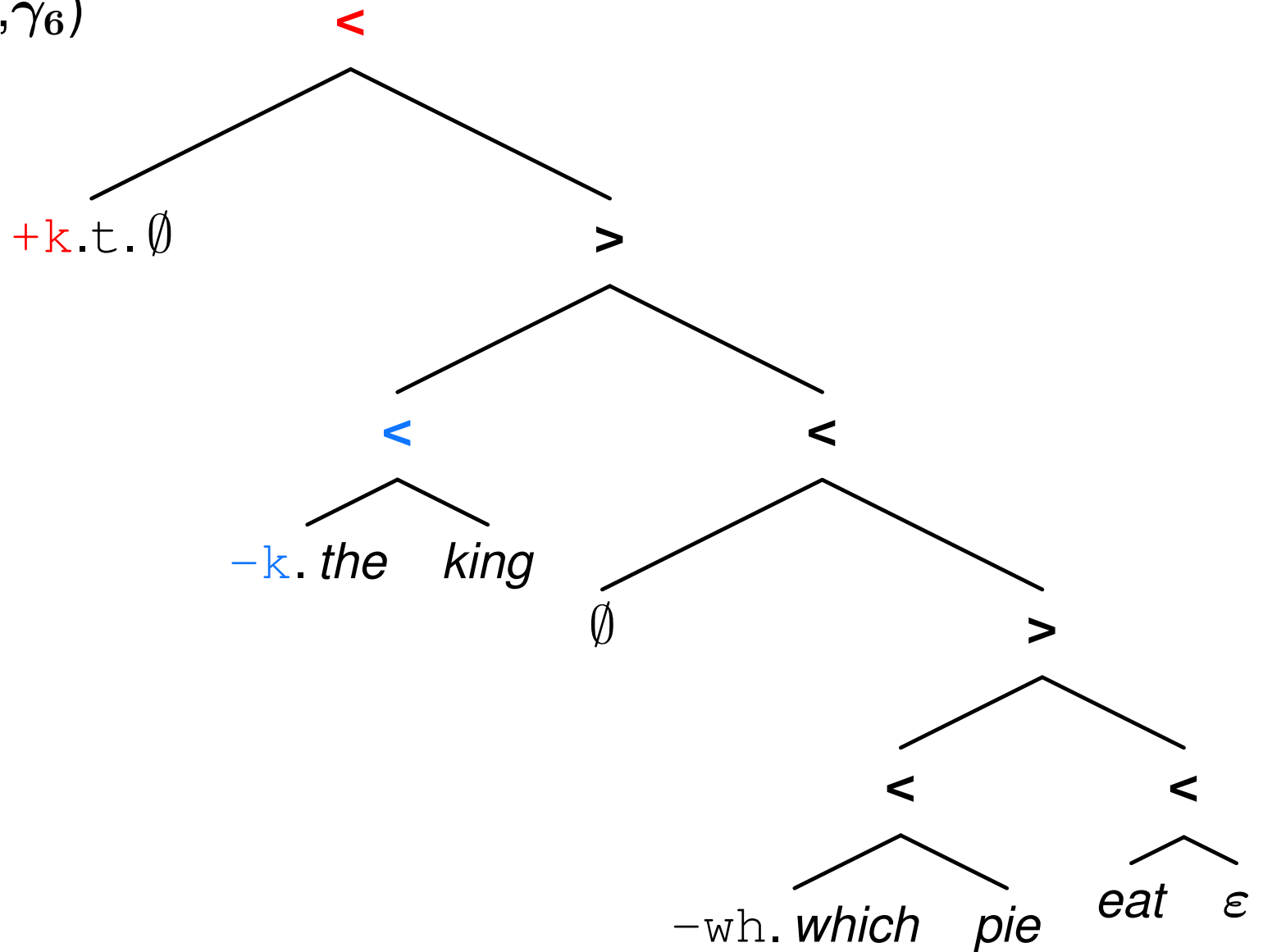
MG-example 2

(γ_7) $\text{merge}(\alpha_2, \gamma_6)$



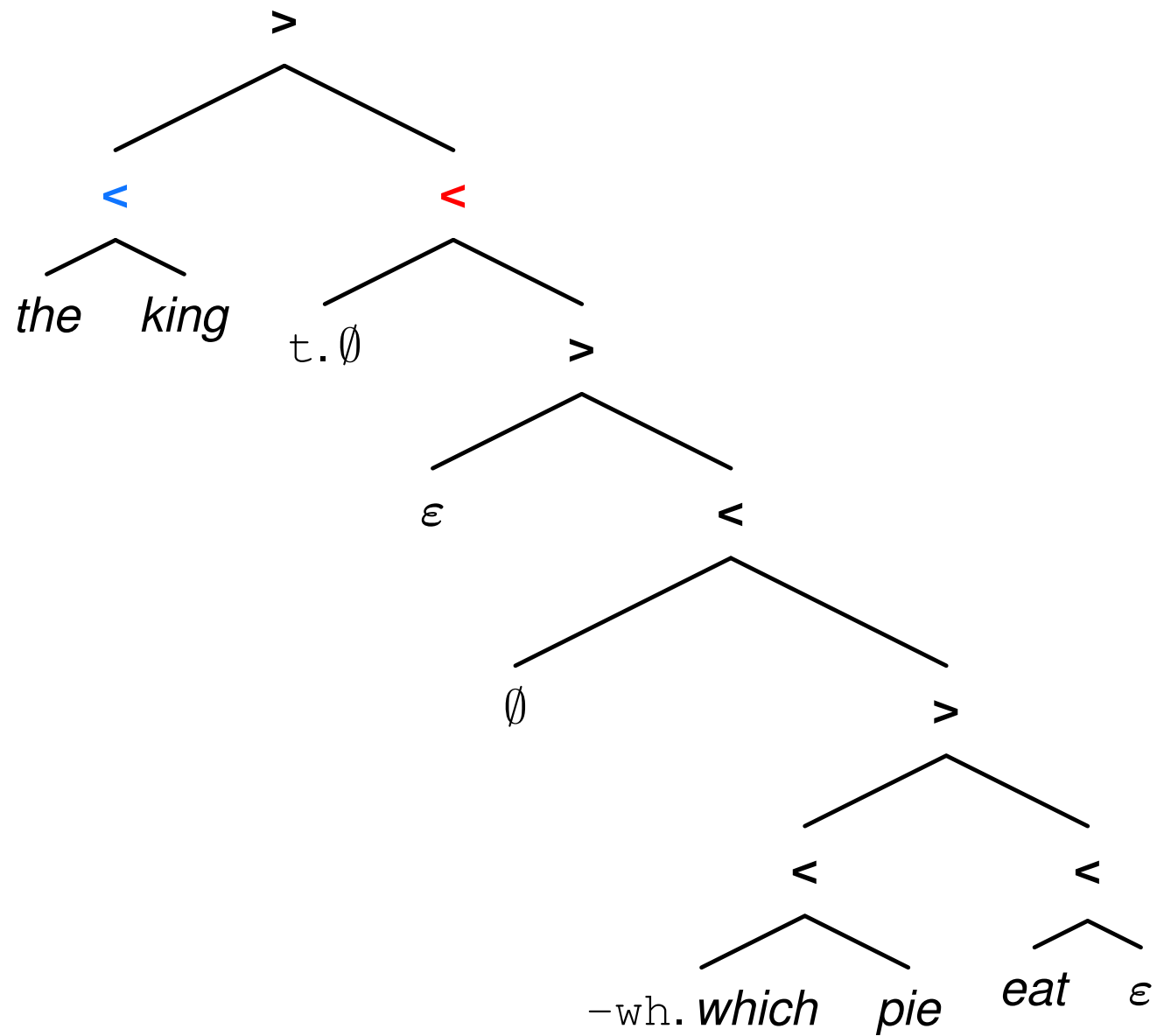
MG-example 2

(γ_7) $\text{merge}(\alpha_2, \gamma_6)$



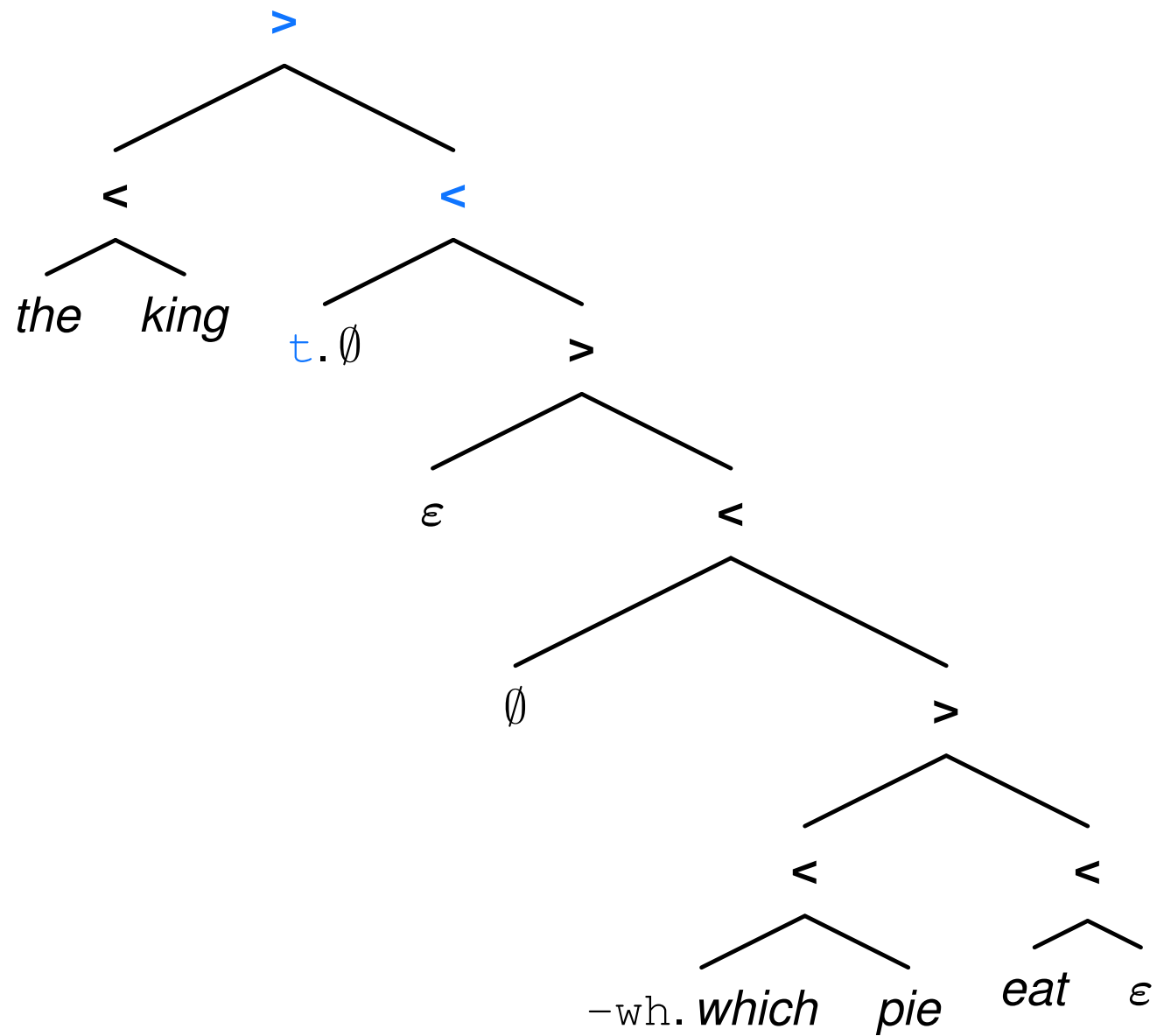
MG-example 2

(γ_8) move(γ_7)



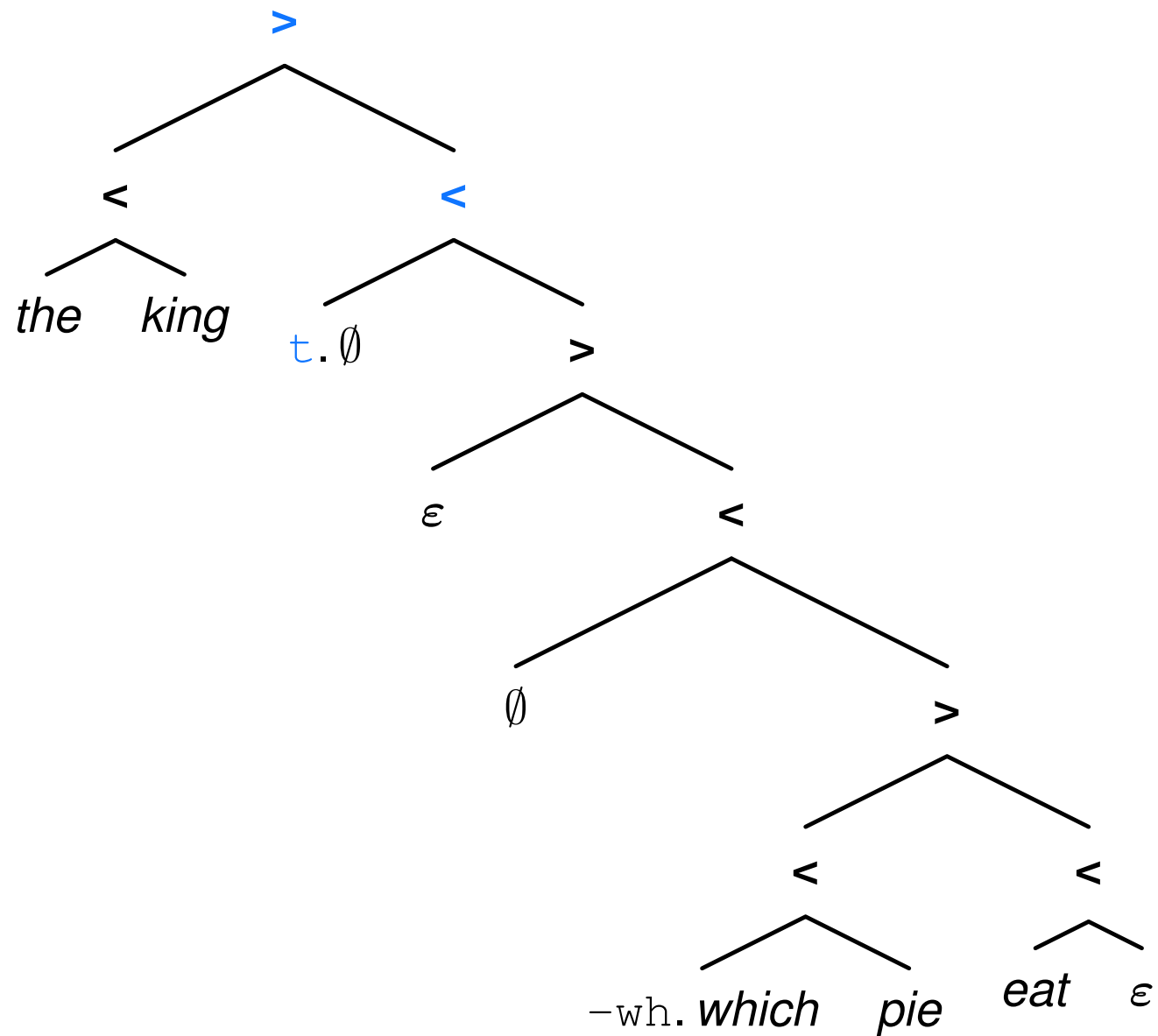
MG-example 2

(γ_8) move(γ_7)



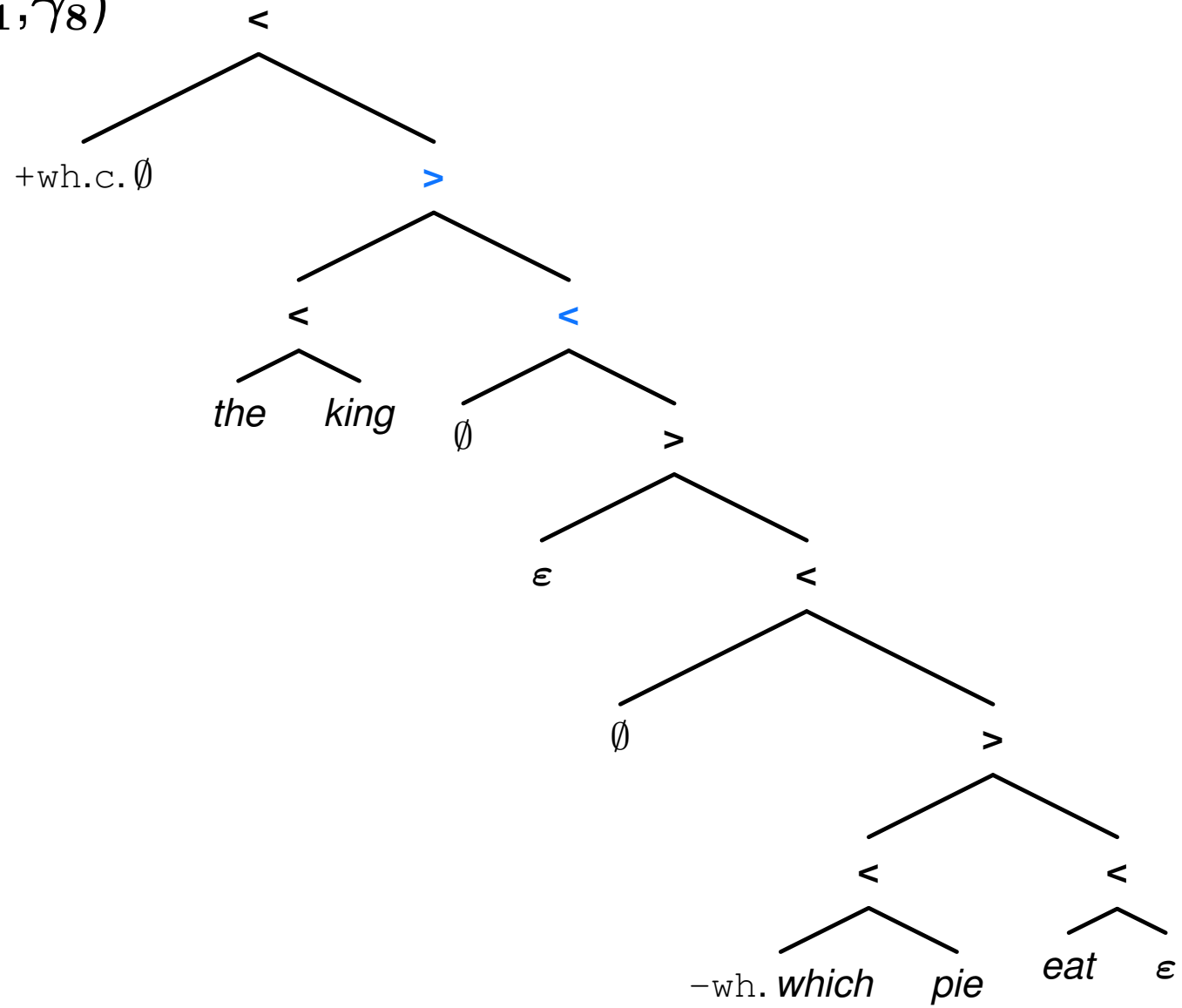
MG-example 2

(γ_8) move(γ_7)



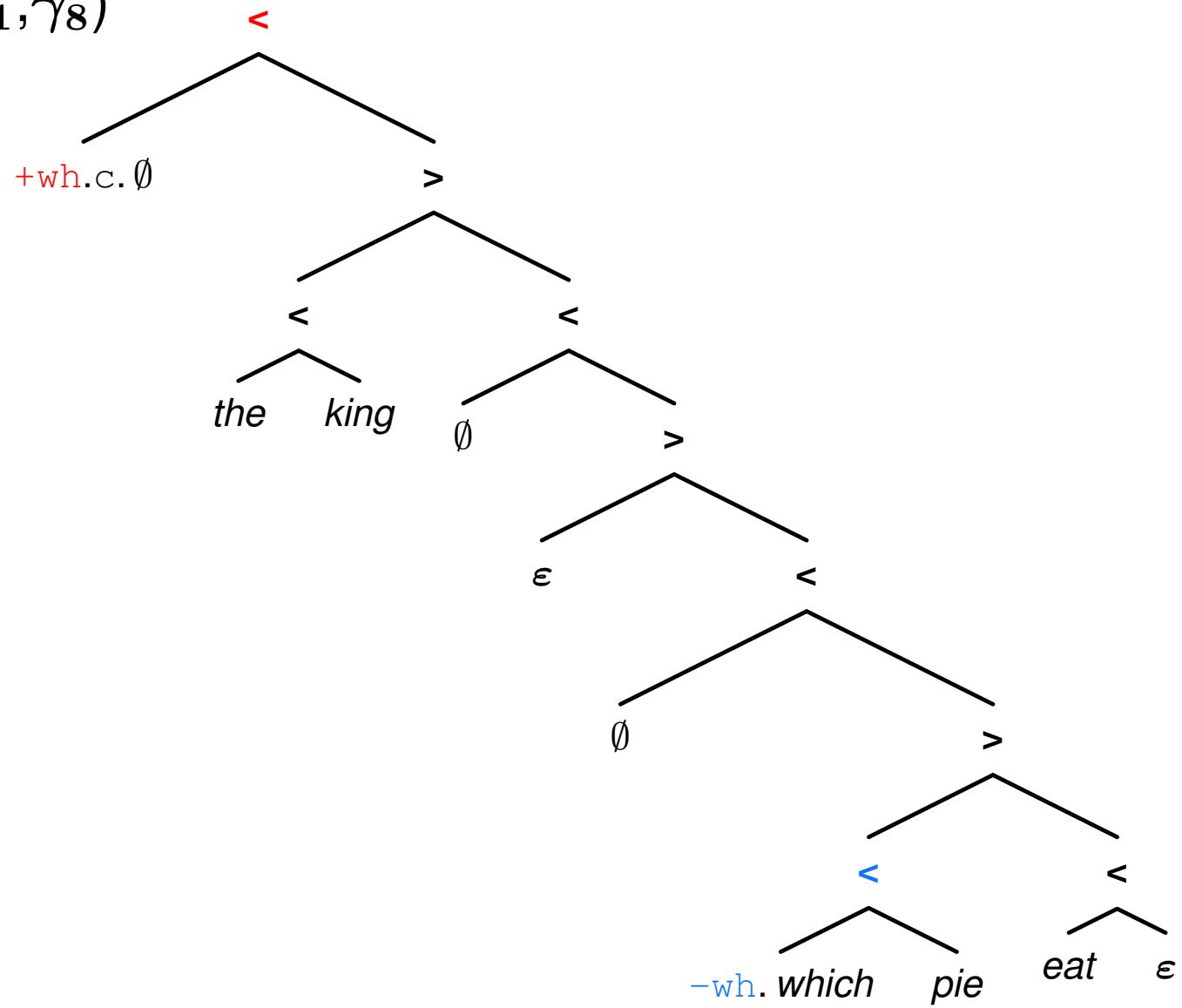
(α_1) = $t.+wh.c.\emptyset$

MG-example 2

$$(\gamma_9) \quad \text{merge}(\alpha_1, \gamma_8)$$


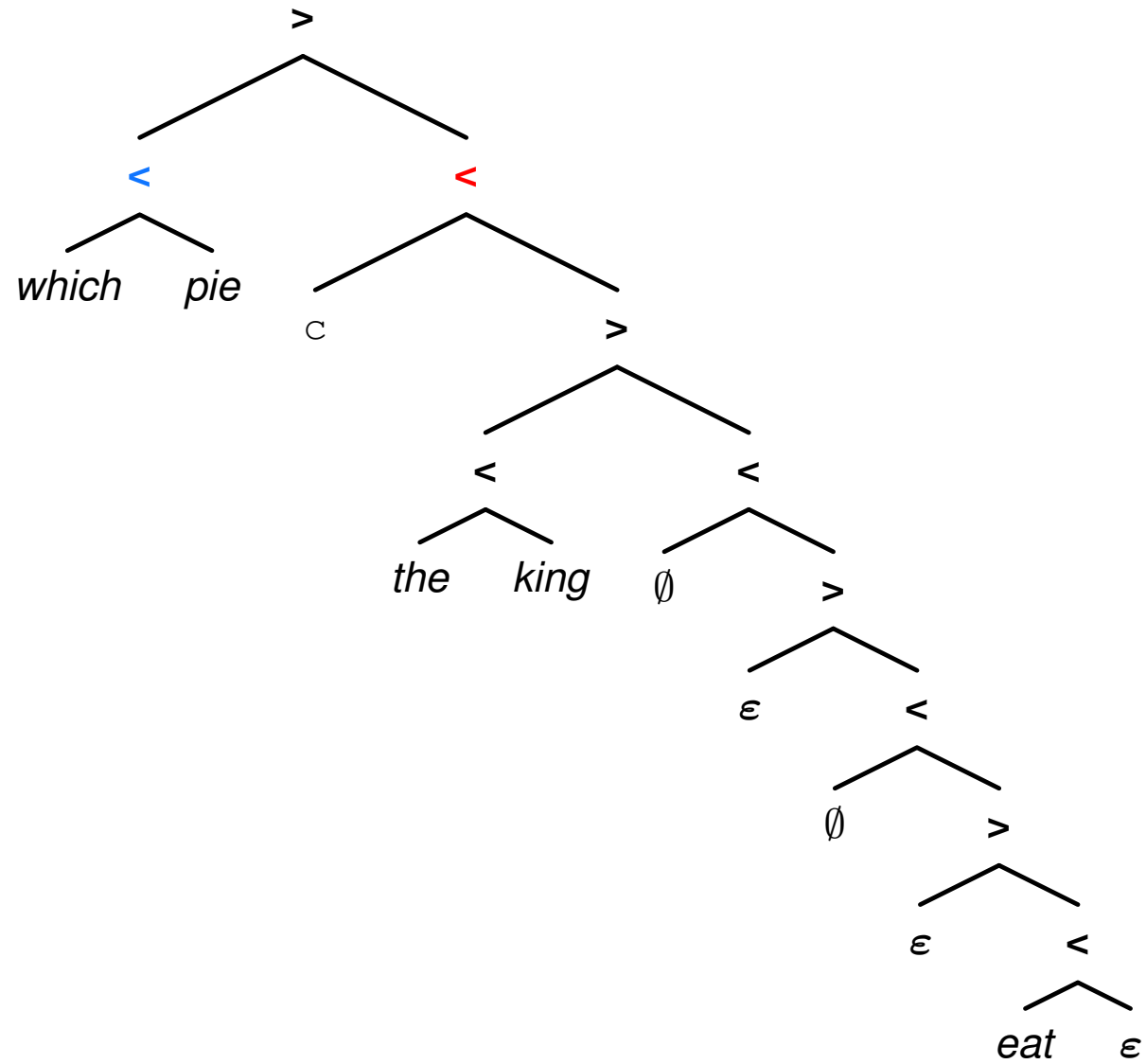
MG-example 2

(γ_9) $\text{merge}(\alpha_1, \gamma_8)$



MG-example 2

(γ_{10}) move(γ_9)



MG-example 2

(α_0) =t.c.*that*

(α_5) v.*laugh*

(α_1) =t.+wh.c. $\emptyset$

(α_6) =n.d.-k.*the*

(α_2) = $\tilde{v}$.+k.t. $\emptyset$

(α_7) =n.d.-k.-wh.*which*

(α_3) =v.=d. $\tilde{v}$. $\emptyset$

(α_8) n.*king*

(α_4) =d.+k.v.*eat*

(α_9) n.*pie*

MG-example 2

(α_7) =n.d.-k.-wh.*which*

(α_9) n.*pie*

MG-example 2

(α_7) =n.d.-k.-wh.*which*

$\langle \text{=n.d.-k.-wh}, \text{—}, \text{—}, \text{sim} \rangle$

(α_9) n.*pie*

$\langle \text{n}, \text{—}, \text{—}, \text{sim} \rangle$

MG-example 2

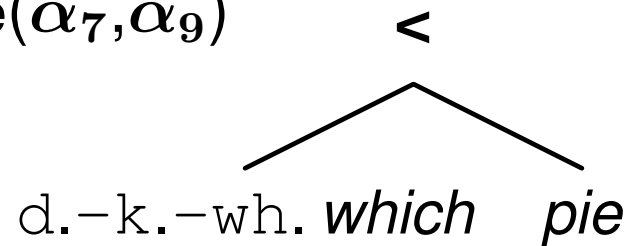
(α_7) =n.d.-k.-wh.*which*

$\langle \text{=n.d.-k.-wh}, \text{—}, \text{—}, \text{sim} \rangle$

(α_9) n.*pie*

$\langle \text{n}, \text{—}, \text{—}, \text{sim} \rangle$

(γ_1) merge(α_7, α_9)



$\langle \text{d.-k.-wh}, \text{—}, \text{—}, \text{com} \rangle$

MG-example 2

(γ_1) merge(α_7, α_9)

<

< d.-k.-wh, —, —, com >

d.-k.-wh. *which* *pie*

MG-example 2

(γ_1) merge(α_7, α_9)

<

< d.-k.-wh, —, —, com >

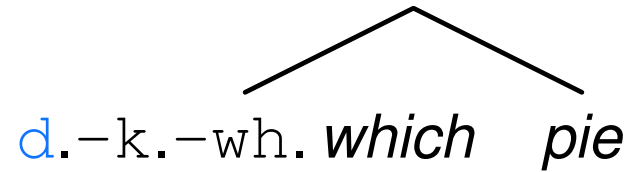
d.-k.-wh. *which* *pie*

MG-example 2

(γ_1) merge(α_7, α_9)

<

< d.-k.-wh, —, —, com >

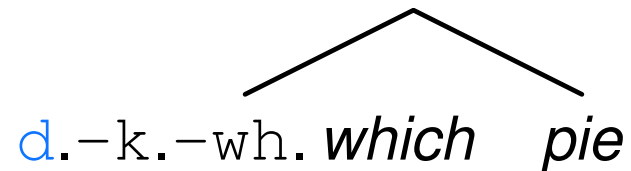


(α_4) =d.+k.v.eat

< =d.+k.v.-k.-wh, —, —, sim >

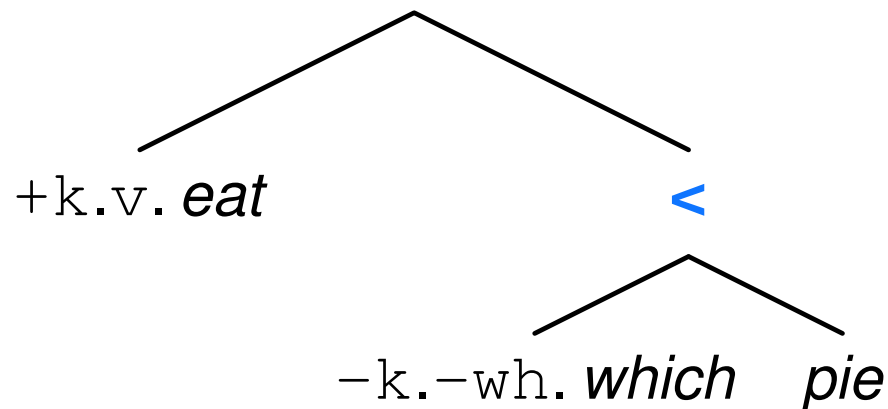
MG-example 2

(γ_1) merge(α_7, α_9) $<$ $d.-k.-wh$, —, —, com $>$

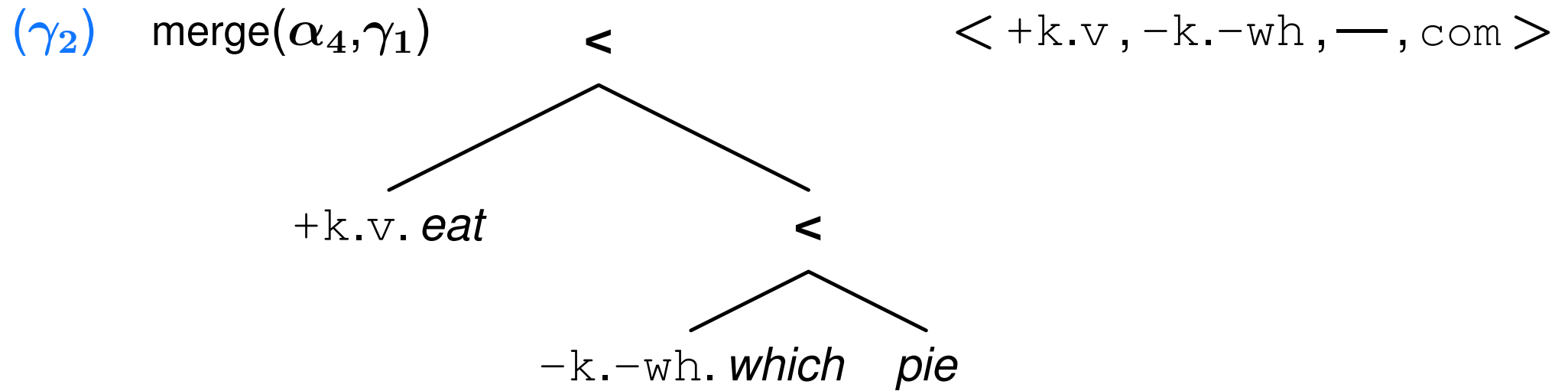


(α_4) $=d.+k.v.eat$ $< =d.+k.v.-k.-wh$, —, —, sim $>$

(γ_2) merge(α_4, γ_1) $< +k.v$, $-k.-wh$, —, com $>$



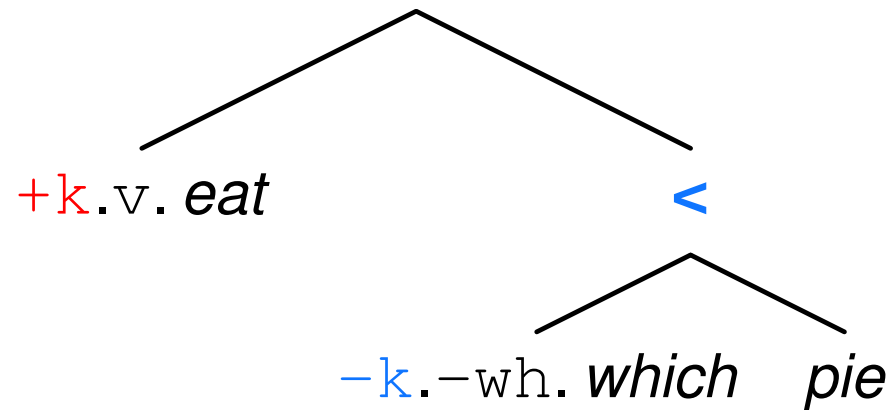
MG-example 2



MG-example 2

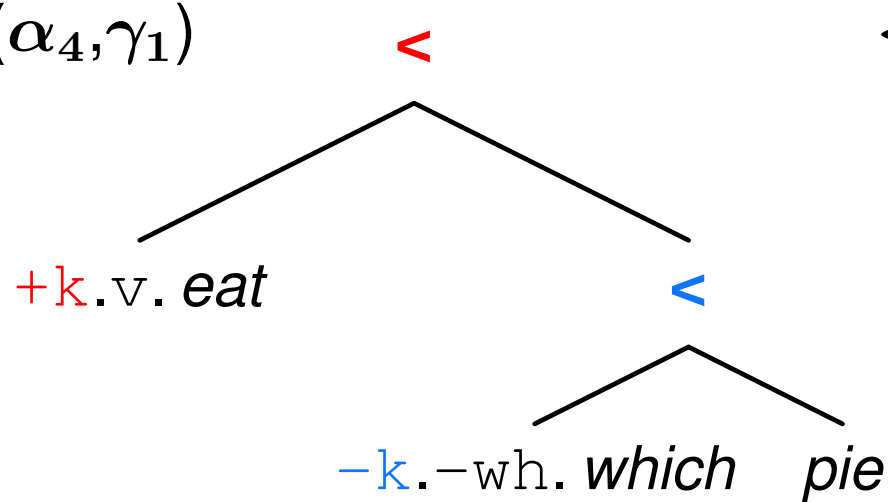
(γ_2) merge(α_4, γ_1)

$\langle +k.v, -k.-wh, \text{—}, \text{com} \rangle$



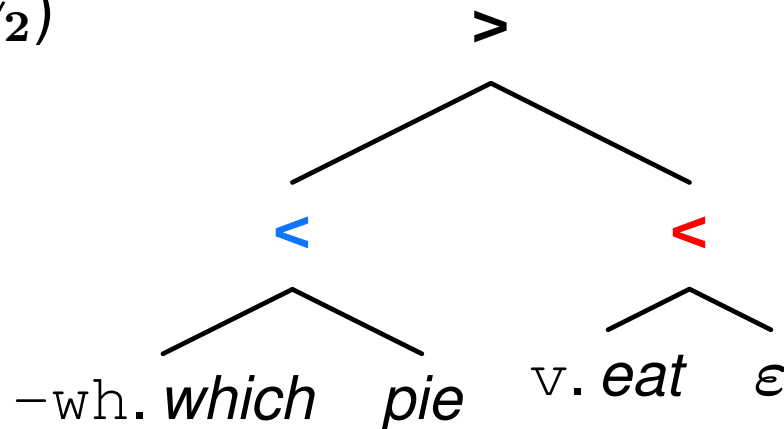
MG-example 2

(γ_2) merge(α_4, γ_1)



$\langle +k.v, -k.-wh, \text{---}, \text{com} \rangle$

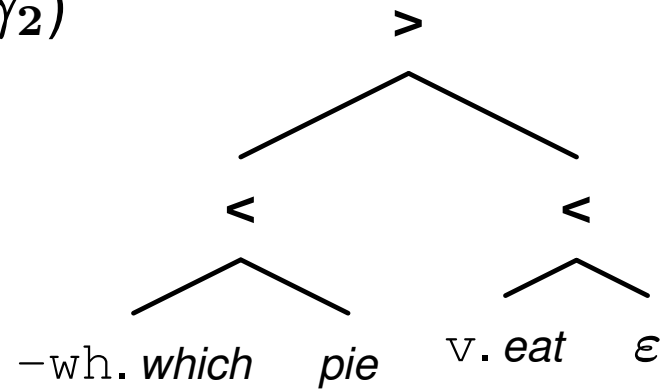
(γ_3) move(γ_2)



$\langle v, \text{---}, -wh, \text{com} \rangle$

MG-example 2

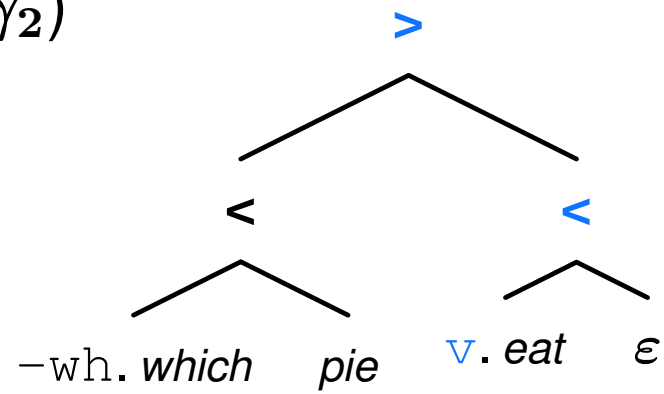
(γ_3) move(γ_2)



$\langle v, \text{—}, -wh, com \rangle$

MG-example 2

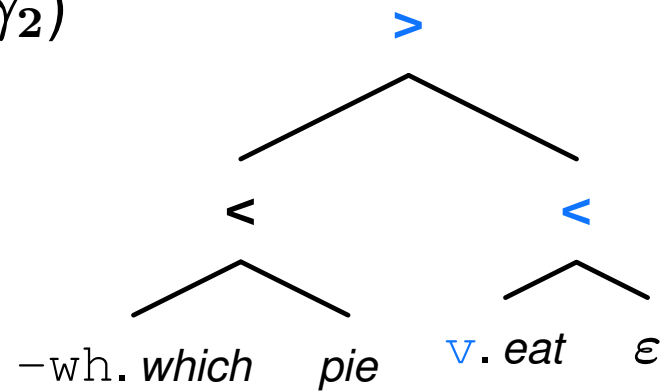
(γ_3) move(γ_2)



$\langle v, -, -wh, com \rangle$

MG-example 2

(γ_3) move(γ_2)



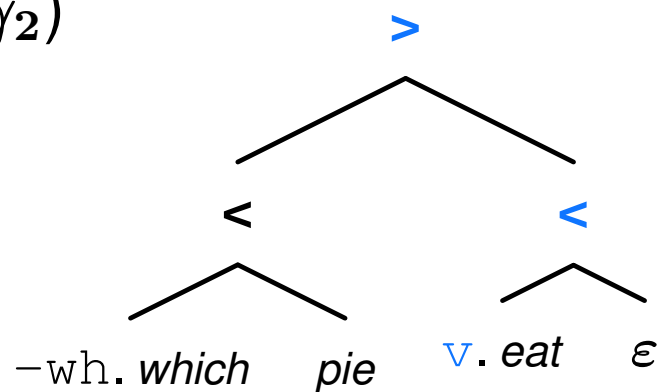
$\langle v, \text{—}, \text{—wh}, \text{com} \rangle$

(α_3) $=v.=d.\tilde{v}.\emptyset$

$\langle =v.=d.\tilde{v}, \text{—}, \text{—}, \text{sim} \rangle$

MG-example 2

(γ_3) move(γ_2)

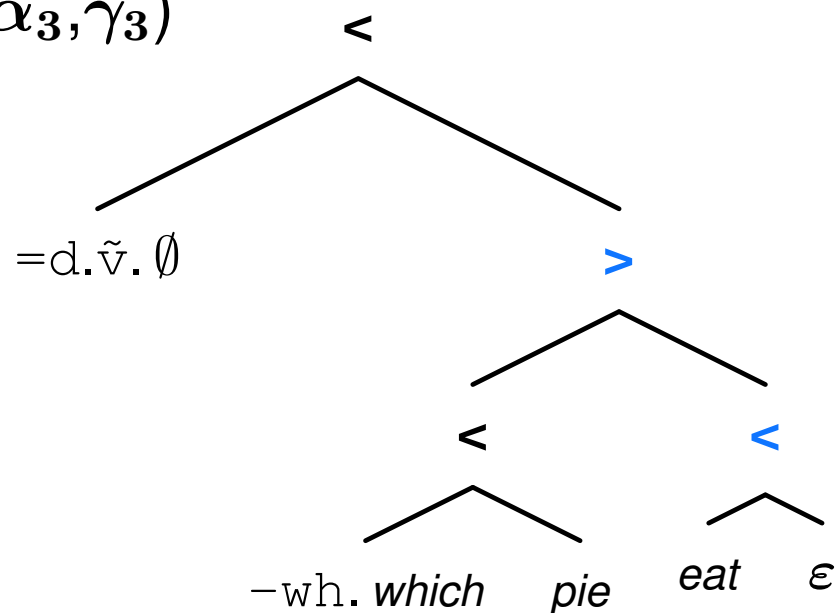


$\langle \text{v}, \text{—}, \text{—wh}, \text{com} \rangle$

(α_3) $=\text{v}.=d.\tilde{v}.\emptyset$

$\langle =\text{v}.=d.\tilde{v}, \text{—}, \text{—}, \text{sim} \rangle$

(γ_4) merge(α_3, γ_3)



$\langle =d\tilde{v}, \text{—}, \text{—wh}, \text{com} \rangle$

MG-example 2

(α_6) =n.d.-k. *the*

$\langle \text{=n.d.-k}, \text{—}, \text{—}, \text{sim} \rangle$

(α_8) n. *king*

$\langle \text{n}, \text{—}, \text{—}, \text{sim} \rangle$

MG-example 2

(α_6) =n.d.-k. *the*

$\langle \text{=n.d.-k}, \text{—}, \text{—}, \text{sim} \rangle$

(α_8) n. *king*

$\langle \text{n}, \text{—}, \text{—}, \text{sim} \rangle$

MG-example 2

(α_6) =n.d.-k. *the*

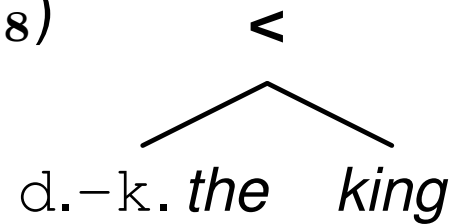
$\langle \text{=n.d.-k}, \text{---}, \text{---}, \text{sim} \rangle$

(α_8) n. *king*

$\langle \text{n}, \text{---}, \text{---}, \text{sim} \rangle$

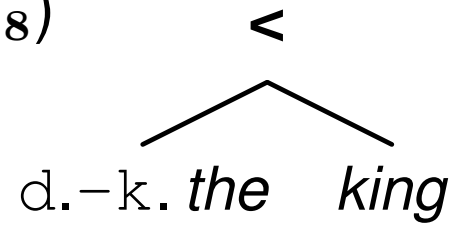
(γ_5) merge(α_6, α_8)

$\langle \text{d.-k}, \text{---}, \text{---}, \text{com} \rangle$



MG-example 2

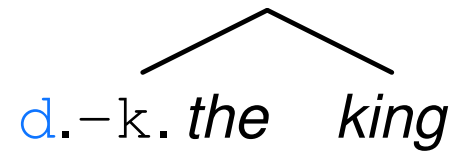
(γ_5) merge(α_6, α_8)



< d.-k , — , — , com >

MG-example 2

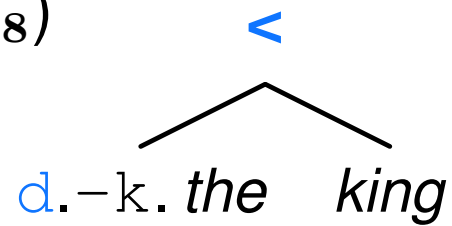
(γ_5) merge(α_6, α_8)



< d.-k , — , — , com >

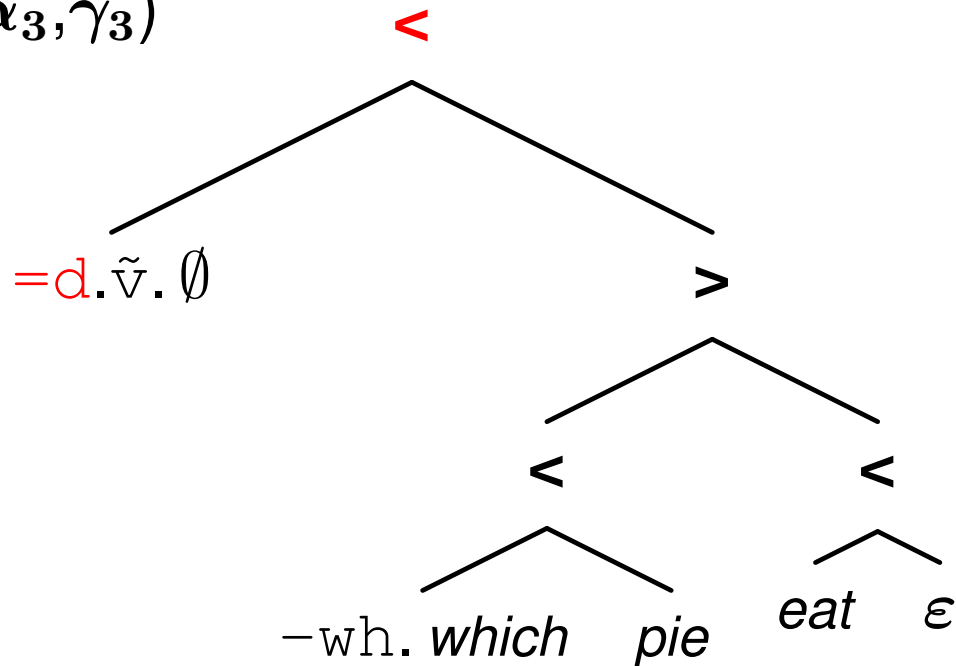
MG-example 2

(γ_5) $\text{merge}(\alpha_6, \alpha_8)$



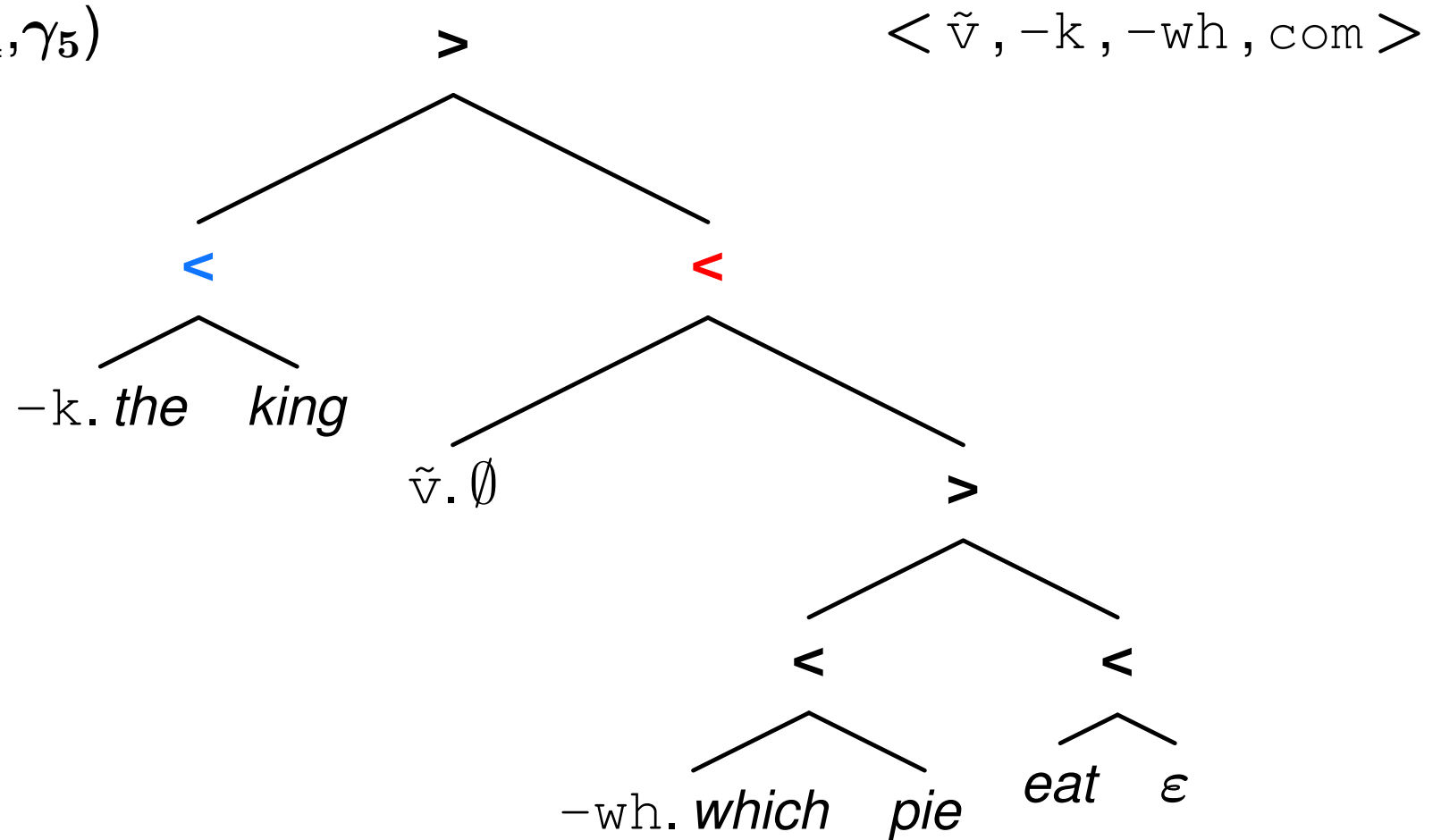
$\langle \text{d.-k}, \text{---}, \text{---}, \text{com} \rangle$

(γ_4) $\text{merge}(\alpha_3, \gamma_3)$



MG-example 2

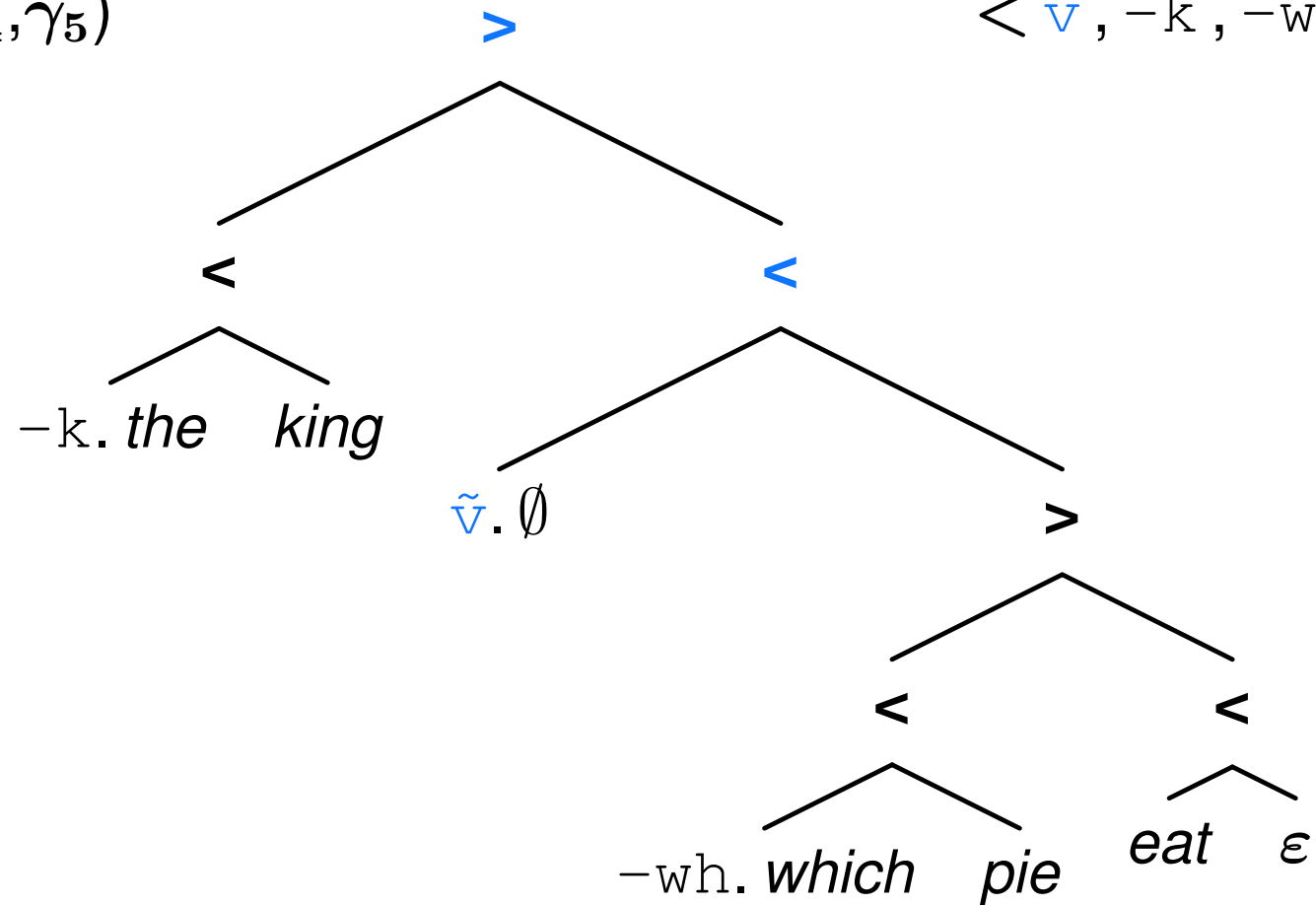
(γ_6) merge(γ_4, γ_5)



MG-example 2

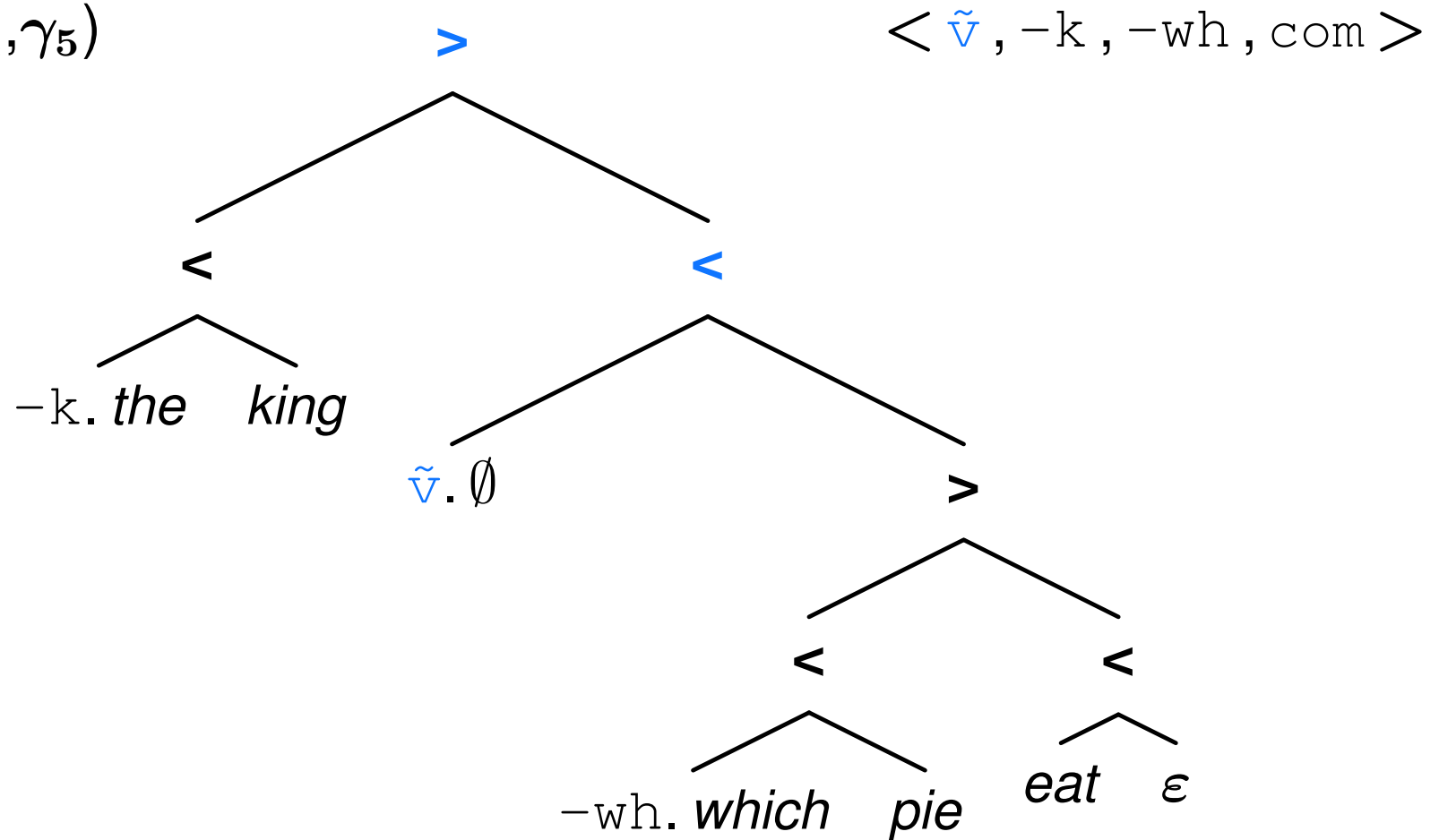
(γ_6) merge(γ_4, γ_5)

$\langle \tilde{v}, -k, -wh, com \rangle$



MG-example 2

(γ_6) merge(γ_4, γ_5)

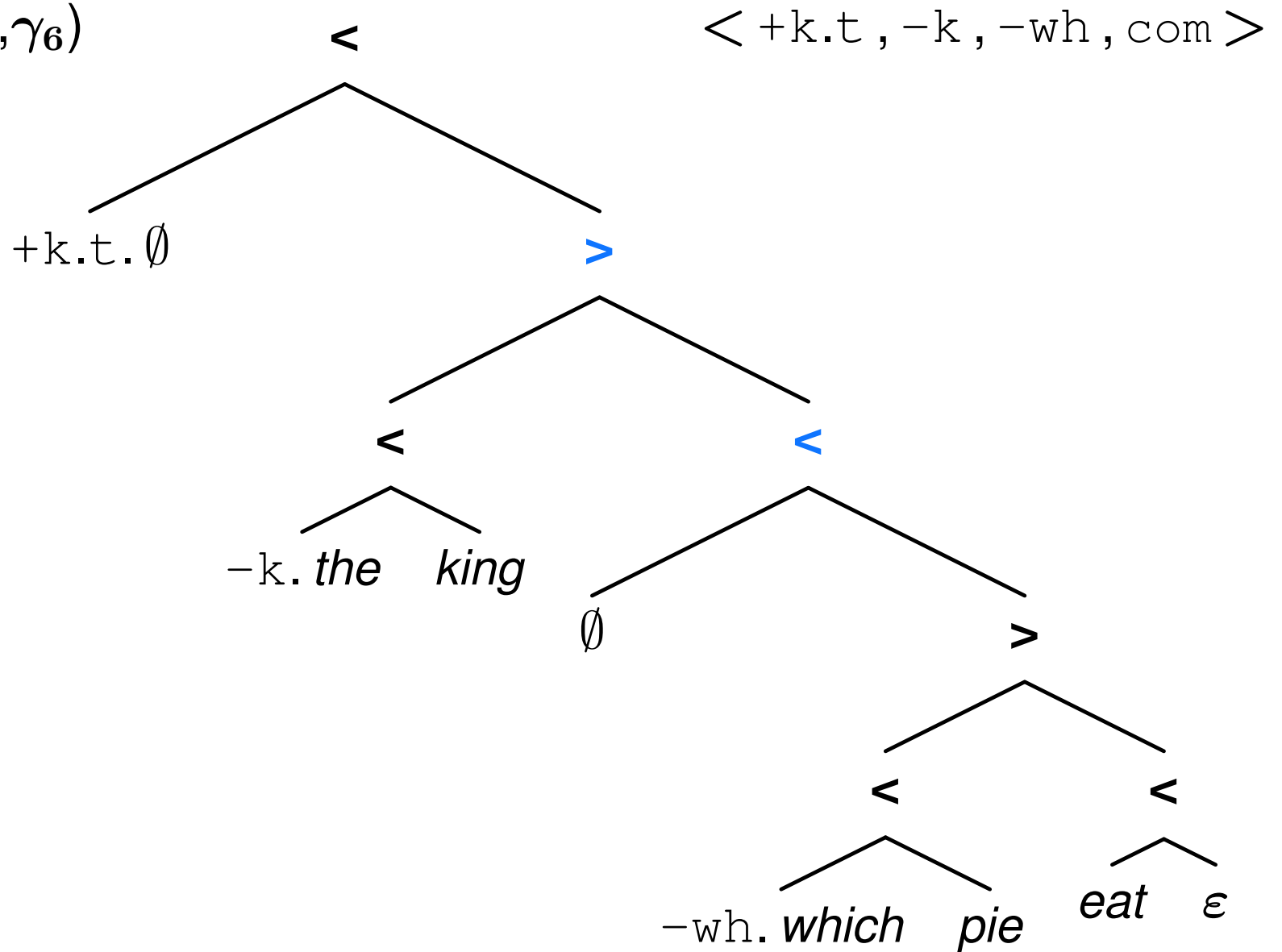


(α_2) $= \tilde{v}.+k.t.\emptyset$

$\langle =\tilde{v}.+k.t, \text{---}, \text{---}, sim \rangle$

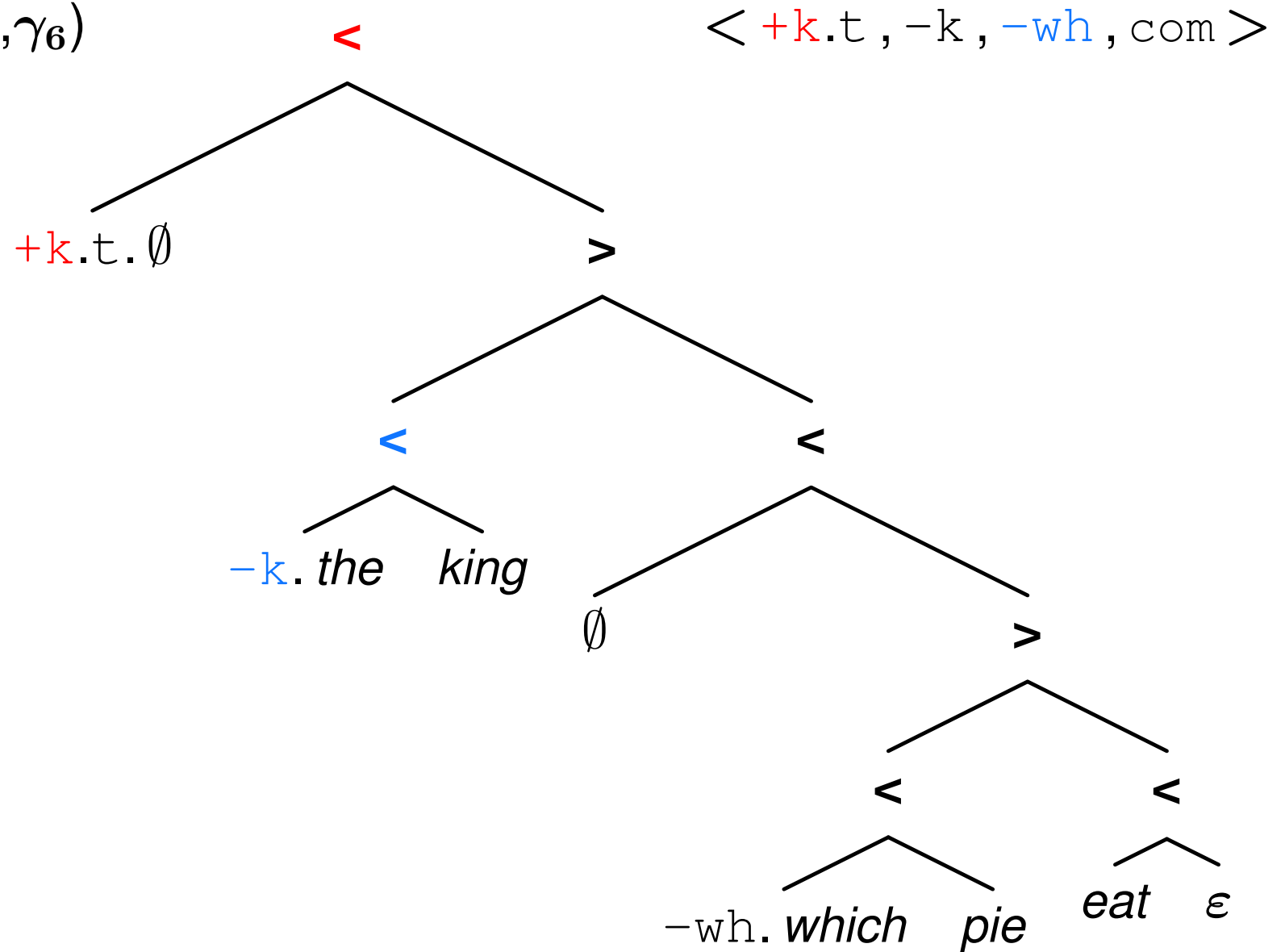
MG-example 2

(γ_7) merge(α_2, γ_6)



MG-example 2

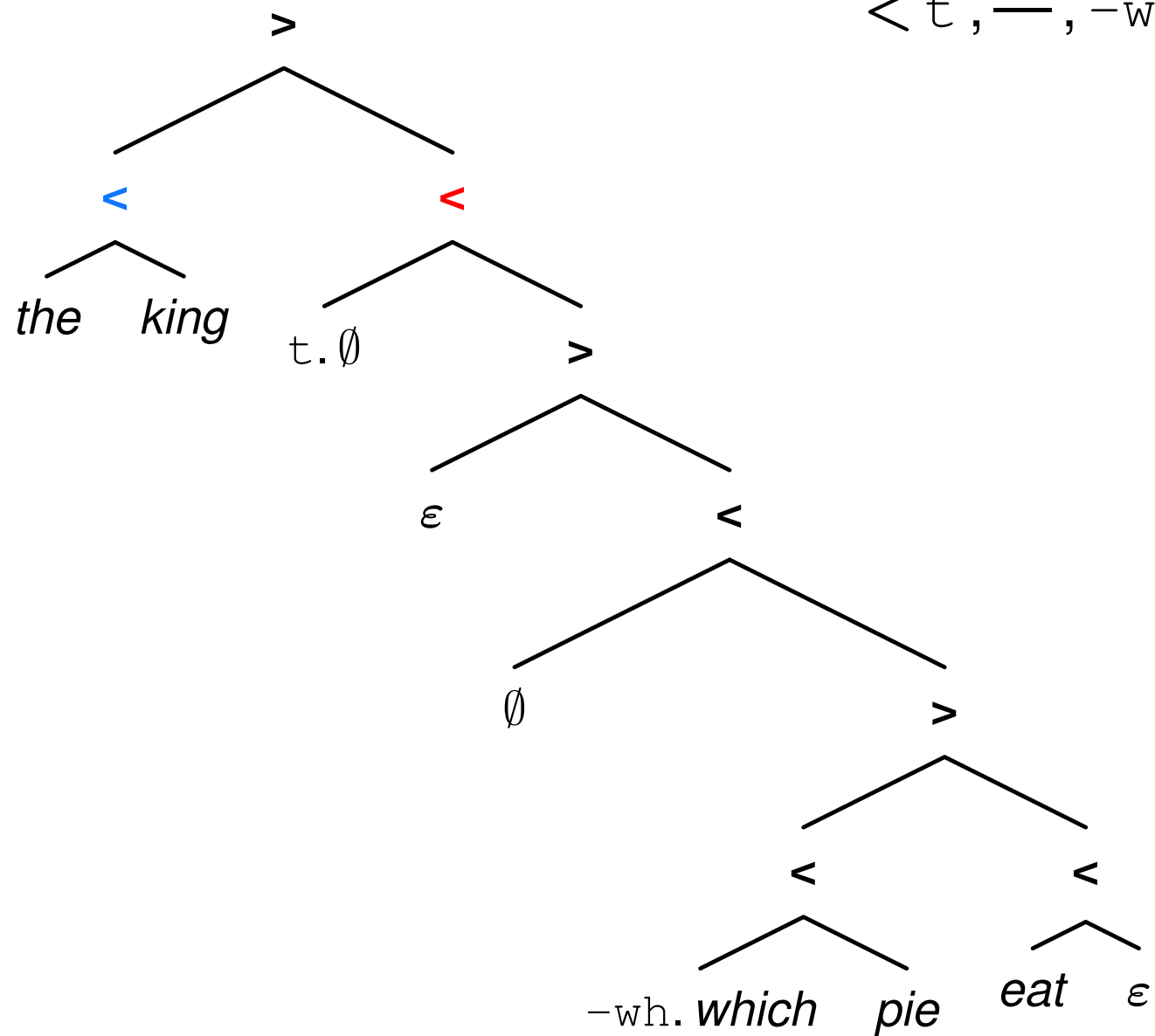
(γ_7) $\text{merge}(\alpha_2, \gamma_6)$



MG-example 2

(γ_8) move(γ_7)

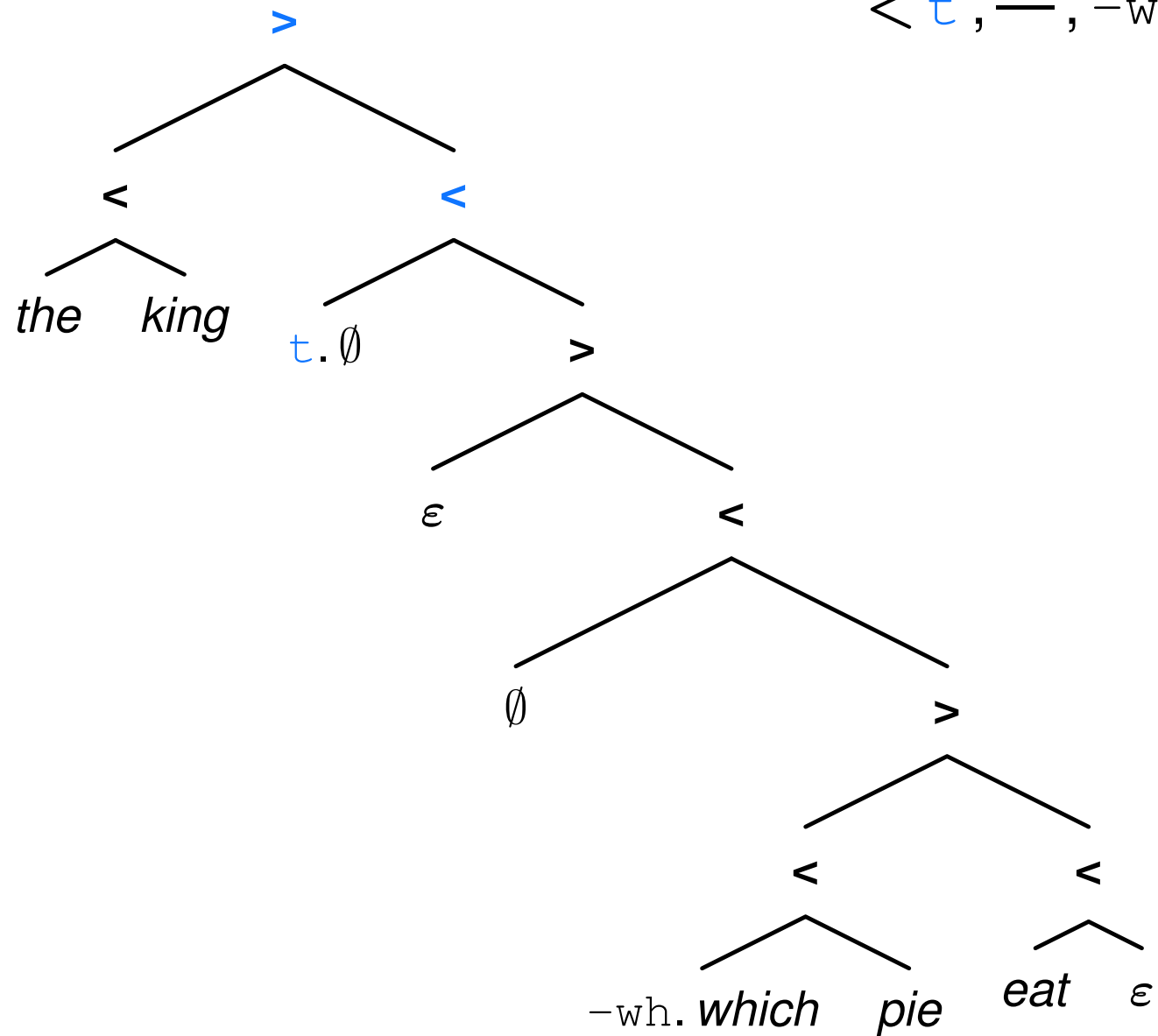
$\langle t, \text{—}, \text{—wh}, \text{com} \rangle$



MG-example 2

(γ_8) move(γ_7)

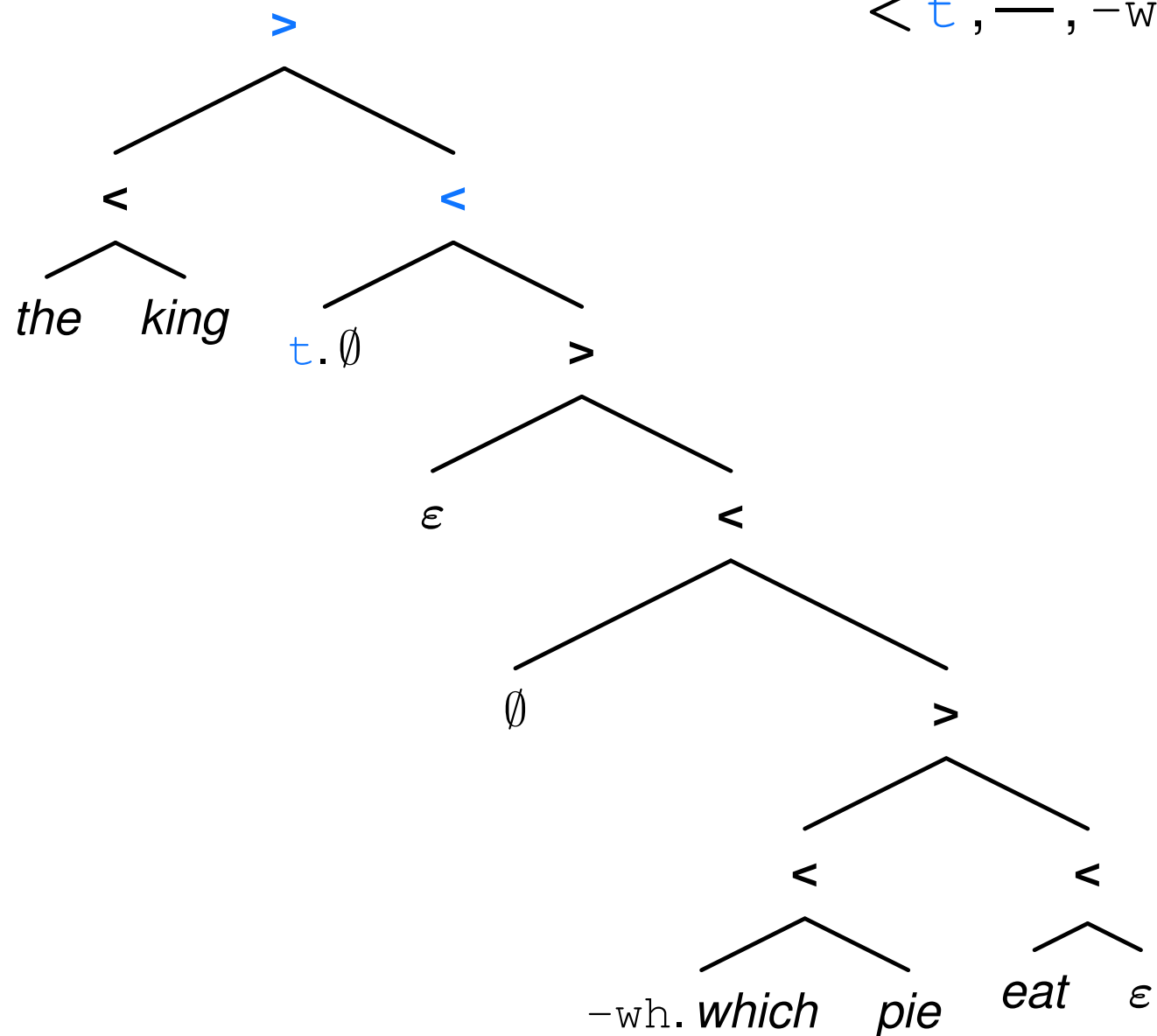
$\langle t, \text{—}, \text{—wh}, \text{com} \rangle$



MG-example 2

(γ_8) move(γ_7)

$\langle t, \text{—}, \text{—wh}, \text{com} \rangle$



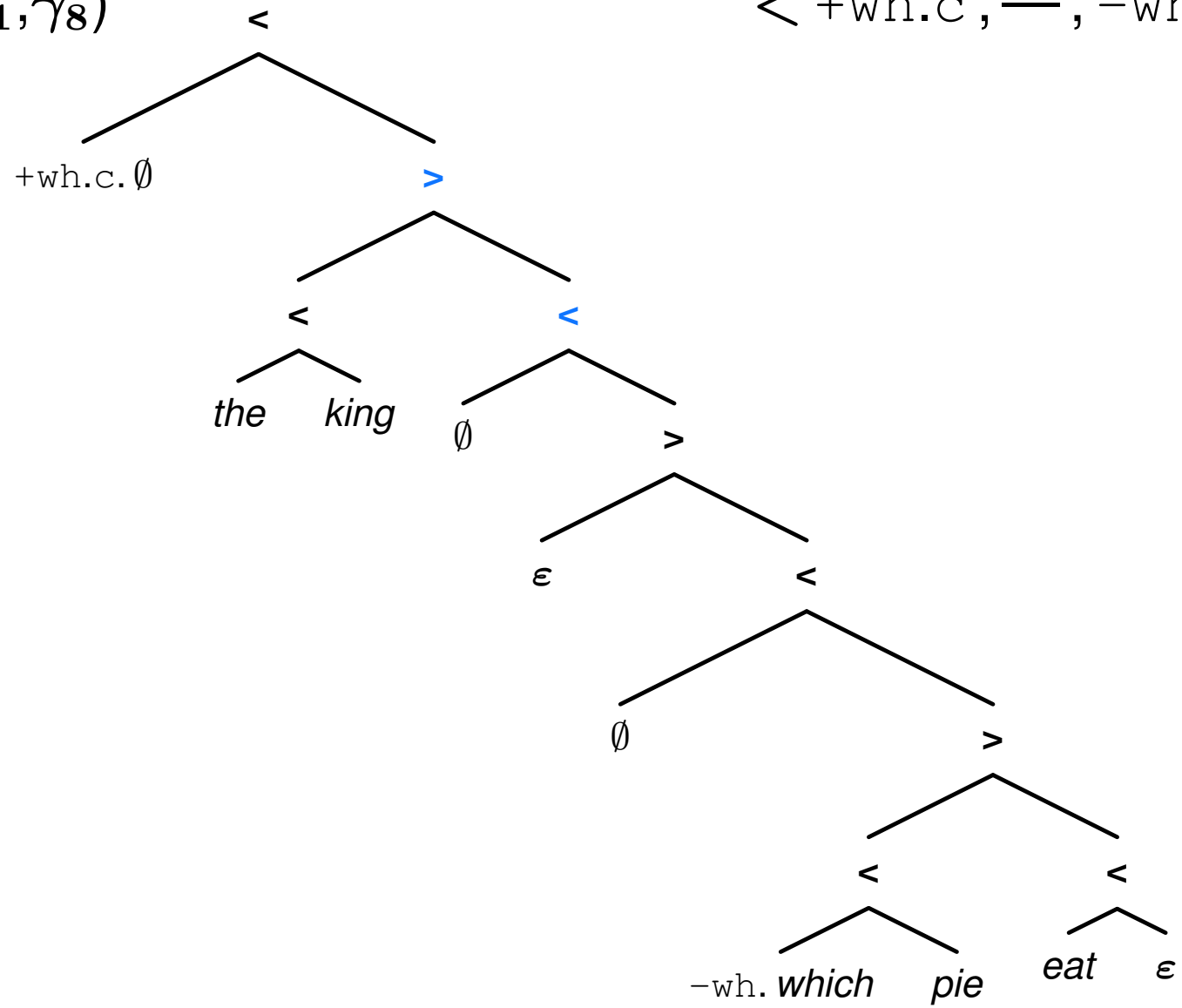
(α_1) =t.+wh.c.∅

$\langle =t.+wh.c, -k, -wh, \text{sim} \rangle$
-p.42

MG-example 2

(γ_9) $\text{merge}(\alpha_1, \gamma_8)$

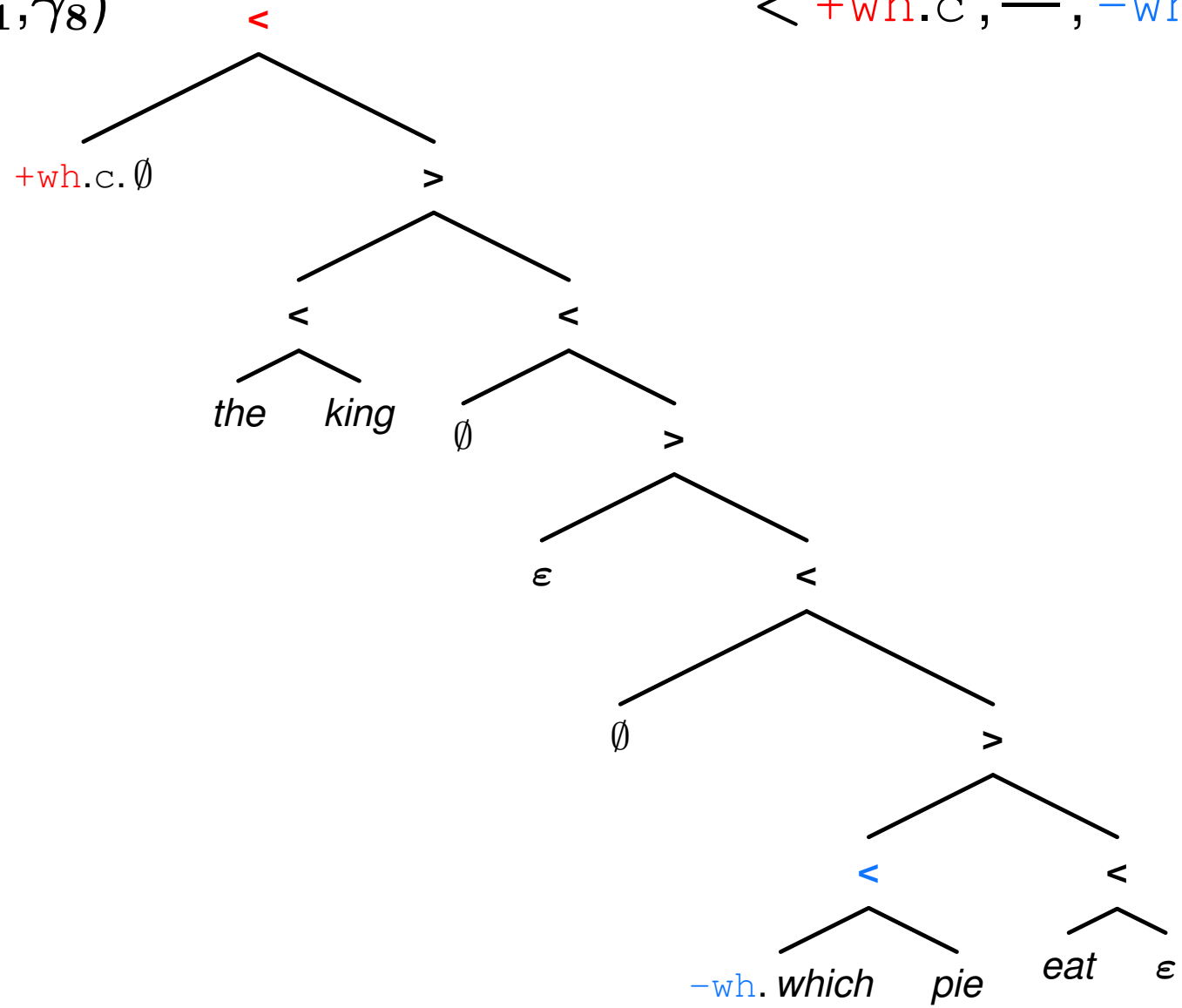
$\langle +\text{wh.c}, -, -\text{wh}, \text{com} \rangle$



MG-example 2

(γ_9) $\text{merge}(\alpha_1, \gamma_8)$

$\langle +wh.c, \text{---}, -wh, \text{com} \rangle$



MG-example 2

(γ_{10}) move(γ_9)

$\langle c, \text{---}, \text{---}, \text{com} \rangle$

