# On Sequence of Location and Direction

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#### **Abstract**

The notion of *sequence of tense* has received wide attention since its (re)discovery roughly 20 years ago. It has recently been argued by Schlenker in [6] that the idea of sequencing a parameter is not restricted to tense. He gives examples showing that there is also sequence of world and sequence of person. These three parameters suggest a close link to verbal morphology, where all three categories are cross-referenced (appearing as tense, aspect, mood, and person). In this paper we shall show that there also is sequence of location and direction. This adds a fourth parameter to the list, and moreover one that is not standardly associated with verbal morphology, though there are languages (e.g. Uto-Aztecan) where verbal morphology reflects location. We give examples from Pima to demonstrate this.

## 1 Introduction

In pragmatic theory, the denotation of an item is a **character**, that is, a function from contexts to meanings. Meanings are typed expressions of some sort, while contexts may be construed as sequences of values. More exactly, we think of a **context** as a function from **parameter names** to values in the model. (We shall

also, somewhat loosely, speak of **parameters** rather than **parameter names**.) One obvious candidate for a parameter name is speaker. There may be interdependencies: if utterance and now are further parameters, then c(utterance) is that u which is uttered by c(speaker) at c(now). Certain expressions make use of these parameters. Consider the meaning of (English) I. Its character is that function which assigns to a context c the value c(speaker). Similarly, now is a parameter name and the character of the word now is  $\lambda c.c(\text{now})$ .

In recent years the phenomenon of sequence of tense has received quite a lot of attention. Although originally a phenomenon associated with tenses, it has been found not to be restricted to tenses alone; it appears also with tense adverbials in the same way. The main facts to be explained are the following. In a subordinate clause there is a difference between yesterday and the day before. The first makes the event time of the subordinate clause happen a day before utterance time, while the second makes it a day before event time. To capture this, let us introduce a parameter name ev-time. Let  $\Delta$  take as input an interval I and return the set of intervals that are at one day before I. Then the characters can be brought out as follows. ( $[-]^{\pi}$  shall denote the pragmatic meaning of the expression.)

(1) 
$$[yesterday]^{\pi} = \lambda c. \lambda Q. \lambda e. Q(e) \wedge time(e) \in \Delta(c(now))$$

(2) [the day before]<sup>$$\pi$$</sup> =  $\lambda c. \lambda Q. \lambda e. Q(e) \wedge time(e) \in \Delta(c(ev-time))$ 

In principle, it is possible to extend this analysis to any parameter that c is a function of. From this perspective it is logical to expect that we have sequence of world, since the characters of expressions are obviously world dependent; and likewise for person. Inverting the logic of this, we can say that the phenomenon of sequence of X shows that X actually is a context parameter. It is our claim that there are parameters for location and direction, which are not reducible to any of the above.

This paper is organised as follows. First, we shall set up a type theoretic language for parameter sequencing. Then we turn to linguistic questions surrounding the notion of sequencing and location. In particular, we shall show that the apparent flexibility of meaning for items based on the so-called *relative frame* (like left) is a consequence of sequencing with respect to viewpoint, a phenomenon that is actually widespread. Finally, we shall present data from Pima (Uto-Aztecan), demonstrating that direction sequencing also exists.

## 2 Some Theoretical Background

In a recent paper [7], Schlenker has proposed an account of sequencing that assumes an arbitrarily long history of values for variables that can be used in further processing. So, for tense there appears a potentially infinite list of time points to which one may connect in further discourse. This seems to be overkill, for it can be seen that grammaticised sequencing uses a bounded number of values for each type of variable that can be a value of a parameter (four for tenses), and if one ever needs to access a parameter value that has been lost one must resort to a description. (See [2] on this.)

Above we said that the characters are just functions from contexts to (semantic) meanings. Unfortunately, this picture is too simplistic. What it predicts is that ordinary expressions are incapable of resetting their values. There are several arguments against this. One is that utterances themselves are objects, so they can figure in the context of any utterance. This allows for paradoxical sentences such as What I am saying is false. Another argument, closer to the present subject matter, is this: If parameters cannot be reset, then if a clause  $S_2$  is contained in a subordinate sentence  $S_1$ , an occurrence of the day before inside  $S_2$  could only be construed relative to the event time of the main clause  $S_0$ , and not of the intermediate  $S_1$ . This means that in the example below the claim on behalf of Pete would be that he had lost his wallet on Saturday and not on Thursday, contrary to fact.

(3) John told Sue on Sunday that Pete had complained to him on Friday that he had lost his wallet the day before.

A solution to this problem has been proposed in [2]. We shall rephrase this approach in the style of Montague's intensional logic, for easy comparison. Recall that in Montague grammar intensions are functions from worlds to objects. In the present framework, meanings are now dependent on more than just the world; they are now dependent on all parameters. More exactly, say that a **context** is a function from parameter names to values; parameter names are sortal and the context has to comply with sortal restrictions. Let  $\gamma$  denote the type of contexts. Types are formed over basic types (or **sorts**) and  $\gamma$  in the usual way. For a standard type  $\mu$  define the **pragmatic lift**  $\mu^{\bullet}$  as follows.  $b^{\bullet} := \gamma \rightarrow b$  if b is basic. An object m of type b is lifted to the function  $m^{\heartsuit}$  such that  $m^{\heartsuit}(c) := m$ .  $(\mu \rightarrow \nu)^{\bullet} := \mu^{\bullet} \rightarrow \nu^{\bullet}$ . An object m of type  $\mu \rightarrow \nu$  is lifted to the object  $m^{\heartsuit} := \lambda \mathcal{P}.\lambda c.m(\mathcal{P}(c))$ . Thus,  $(\mu \rightarrow \nu)^{\bullet}(\mu^{\bullet}) = \nu^{\bullet}$ , and  $m^{\heartsuit}(n^{\heartsuit}) = (\lambda \mathcal{P}.\lambda c.m(\mathcal{P}(c))) = \lambda c.m(n^{\heartsuit}(c))$ . One shows

inductively that  $m^{\circ}(c) = m$ . This embeds the original (nonpragmatic) language into the pragmatic language. But there is more.

For a given sort (tense, person, world, location) there may be several names, but the list is finite and small for each sort. Expressions may make use of the context. In order to express the pragmatic meanings we use the functions

(4) 
$$\{\rho := a\} : \gamma \to \gamma$$

The result  $\{\rho := a\}c$  is a context c' such that  $c(\rho) = a$ , but  $c(\rho') = c(\rho)$  for all  $\rho' \neq \rho$ . There are constants  $\rho_{\nu}$  for every parameter name  $\nu$  (we use sans serife plus a mnemonic name to denote them). The type of  $\rho_{\nu}$  is  $\gamma \to \alpha$  if  $\nu$  is a parameter for sort  $\alpha$ . So, now is of type  $\gamma \to \tau$ ,  $\tau$  the sort of time points.

In order to analyse the data on sequence of tense, we use three parameters, now, ev-time and p-time, the latter being **predication time**. In the default or 'null context' they receive the same value. A sentence, main or subordinate, takes as input a context containing values for these three parameters and outputs again values for them.

Now, let us look at the expression I said \_\_. Extensionally, it takes a proposition and returns a proposition, so is of the type  $t \to t$  (recall: no intensions needed). Its pragmatic lift is  $(\gamma \to t) \to (\gamma \to t)$ . The complement sentence denotes a function Q from contexts to truth values. The expression denoted by I said takes Q as argument and feeds it a revised context.

(5) [I said]<sup>$$\pi$$</sup> = $\lambda Q.\lambda c.c$ (p-time) <  $c$ (now)  $\wedge$  say( $c$ (speaker),  $c$ (p-time),  $Q$ ({ev-time :=  $c$ (p-time)}( $c$ )))

This means in ordinary terms: given the context c, speaker-of-c says at predication-time-of-c, which is before now-of-c that Q(c'), where c' is different from c in that event-time-of-c' is the predication-time-of-c. Effectively, this allows the value of the predication time of the upper context c to be passed down as the event time of the subordinate clause.

We construe sequence of person and sequence of world, and of location in a similar spirit. The proposal accounts not only for demonstratives like here and there. It specifically also accounts for left which is notoriously flexible in meaning.

## 3 Linguistic Facets of Sequencing

There are several questions one may raise concerning this approach.

- Is the trigger for sequencing syntactic in nature or semantic?
- **2** Do all languages have sequencing and if so, do they display any differences?
- Is the triggering mechanism a global choice of a language or can items individually determine it?
- **4** What parameters are subject to triggering?

We shall address these questions in due course. First, we argue that sequencing occurs in special circumstances only. It must be a consequence of the meaning of the item that the resetting of parameters takes place. Consider by way of example the case in Amharic discussed in [6]. The pronoun for 'I' in Amharic can mean 'Peter' in a sentence with an indirect quote like

### (6) Peter says I do not like cigars.

This answers in some sense the second question: there are differences between languages in that most languages do not allow sequencing for pronouns but Amharic does. Similarly, there are languages that do not allow sequencing for locations, such as Tzeltal and Guugu-Yimithirr (see [4] for extensive discussion). However, person sequencing occurs only with verbs of saying. How come? If the pronoun 'I' actually means something like 'speaker' there is an implicit variable here that needs to be brought to light: speaker of the main utterance versus speaker of the utterance denoted by the embedded sentence. Thus, only if the verb supplies an additional speaker of the embedded clause is there any chance that it may become the denotation of 'I'. To return to English, there are cases where the same effect can be obtained:

### (7) If I were you, I would stop lending me money.

The embedded subject 'I' is actually the addressee of the main clause, and this squares well with the fact that the object is me and not myself. (We are asked to picture a world w where c(speaker) = c(addressee). In that world w, c(addressee) can now be referred to by I. On the other hand, in the present world it picks out c(speaker), which is a different individual, and may also be different in w. Obviously, an exact rendering will have to pay attention to the dependency on w.) This answers also the first question: the nature of the trigger is not syntactic in that it cannot be tied to a specific syntactic category: Some items trigger sequencing, some do not. On the other hand, whether the pronoun 'I' is subject to sequencing is an individual choice languages make. Sequencing is therefore not predictable on the basis of meaning alone.

### 4 Location and Direction

We claim that location and direction are also context parameters and therefore subject to sequencing. Below we shall present some data from actual field research. Before doing that we shall first sketch some details on location and direction in language. First, by **location** we mean a path connected subset of the ordinary space we live in ( $\mathbb{R}^3$ ). A material object has a location at every given time point of its existence. To make matters simple, locations are simply points. A **direction** is a vector (which can also be construed as a point of  $\mathbb{R}^3$ ). For example, if I say

### (8) Campbell Hall is 200 m to the left.

then the truth of that sentence depends, among other things, on my location and the direction I am facing. Note that this is a feature of the word left. Had I used north then the direction I was facing would be irrelevant.

In the literature it has been observed that there are various ways in which locative expressions can be sensitive to their syntactic environment. The absolute type pays no attention to the direction of any object; such is the case with north. The nonabsolute type allows dependency on the directionality; this could be the direction of its complement (intrinsic) or the vector from some other object to the complement's location (extrinsic). This other object is called the viewpoint (see [3]). The expression to the left of the chair, when used by Paul with Paul standing opposite of the chair and facing it, can be used to denote a location to Paul's right (= the chair's left; intrinsic) or to his left (= the chair's right; extrinsic). Our specific suggestion here is that these types square well with the kinds of sequencing behaviour that we expect with tense and person. The specific differences are attributable mainly to the fact that locations are of a different nature than tenses and worlds. We suggest there is a parameter of event location in addition to viewpoint, which figures in some uses of there. We could also introduce an utterance location (to explicate the meaning of here), but it seems to be definable in terms of speaker and utterance time. The viewpoint is not necessarily identical to utterance location. This is needed to account for the meaning of come as in

#### (9) I will come to Paris.

uttered by Paul on occasion when he is actually not in Paris. The use of the notion of coming is appropriate e.g. if he shall be approaching the viewpoint-at-predication time, and this latter location is inside Paris (see [1] for a similar phenomenon in Ambae (Oceanic)). A similar intuition underlies the analysis of

come and go postulated in [8]. The present approaches supplies a formalism for handling his 'hidden parameters' (like viewpoint). [8] also drew attention to the parallel behaviour of viewpoint and that of tense and person.

The shiftability of the viewpoint seen above seems to be language specific. It has been reported that Lakhota has two kinds of prepositions with virtually identical distribution and meaning, only that one suggests that the trajector is approaching or at the viewpoint, while the other suggests it is not (see [5]). The fact that the these two sets are interchangeable in any context derives from the fact that viewpoint can be shifted very easily in Lahota. Japanese and Quiché, on the other hand, are reported to have stricter requirements regarding the identity of the viewpoint and the location of speaker.

To make matters concrete, we shall give an analysis of English north and left. Let north be a function that takes a point and returns a direction vector. Let loc(x, t) be the location of x at t.

(10) [to the north of]<sup>$$\pi$$</sup> =  $\lambda c.\lambda x.north(loc(x, c(p-time)))$ 

This analysis determines the direction on the basis of the predication time location of x, which is the object denoted by the complement PP. Now, let  $\forall \vec{v}$  be the direction at 90° counterclockwise from  $\vec{v}$ . Let vec(x, y) be the vector defined by x as origin, and y as end. Then one meaning of left is given by

(11) [to the left<sub>1</sub> of]<sup>$$\pi$$</sup> =  $\lambda c.\lambda x. + (\text{vec}(c(\text{viewpoint}), \text{loc}(x, c(\text{p-time}))))$ 

We have construed the meaning of left to be dependent on the viewpoint, see [3]. To the extent that the latter is subject to sequencing, this makes the actual direction that is being denoted also subject to sequencing effects. This would be needed in sentences such as

#### (12) I told you that the book is to the left of the chair.

which allows 'left of' to be construed using either the axis between speaker and the chair or the axis between addressee and chair, depending on whether the viewpoint is shifted or not. A third reading is the **intrinsic** meaning, which uses another axis, denoted by face(x, t), which is the direction of the intrinsic axis of x at t:

(13) [to the left<sub>2</sub> of]<sup>$$\pi$$</sup> =  $\lambda c.\lambda x. + (face(x, c(p-time)))$ 

The intrinsic meaning is unavailable if there is no intrinsic axis. The availability of an intrinsic axis is subject to cross-linguistic variation, see [3] and references therein.

## 5 Location and Direction Marking in Pima

Pima has a series of deictic particles that encode distance and direction holding between an event participant and a deictic center. The particles used below are 'ab 'towards', 'am 'away', and 'an 'parallel, perpendicular', all distals. (There are also proximates, 'i, 'im, and 'in.) The typical situation is for the speaker to be the deictic center, and to specify the direction of an event participant relative to the speaker (14), (15).

When such particles occur in an embedded clause, the deictic center is identified with an argument of the matrix clause. Thus, in (16), the first particle 'an specifies that Bart is facing sidewards relative to the speaker, while the second specifies that the dog is facing sidewards relative to Bart, even if the dog is facing the speaker. If the dog were facing Bart, on the other hand, then the second particle would be 'ab (17). This shift also occurs with perception verbs: in (18), the deictic center for the particle 'ab is Marge, not the speaker. The sequencing in these examples is obligatory: the embedded deictics in (16), (17), and (18) cannot be interpreted with the speaker as deictic center. Since the specification of a location is dependent on the perception of it, the deictic center can be reset with predicates that report (directly or indirectly) an individual's perception.

```
Keli
             'at
                       'ab
                              'i'iho.
(14)
             AUX:PF D:FR cough
      'The man coughed (while facing me).'
      Keli
             at
                       'am
                              'i'iho.
(15)
             AUX:PF D:BK cough
      'The man coughed (while facing away from me).'
      Bart
             'о
                    an
                           'aagid heg
                                              Lisa mash
                                                             heg
                                                                   gogs
      Bart
             AUX
                   D:SD
                          tell
                                    DET
                                              Lisa
                                                    C:AUX DET dog
             'an
                    keek
                          Homer
                                    veegaj.
(16)
             D:SD stand
                          Homer
                                    behind
      'Bart (who is looking to my side) is telling Lisa that the dog
             (which is facing to Bart's side) is standing behind Homer.'
      Bart
                    'an
                           'aagid heg
                                              Lisa mash
                                                             heg
                                                                   gogs
             AUX
                                   DET
                                                    C:AUX DET dog
      Bart
                   D:SD
                          tell
                                              Lisa
             'ab
                   keek
                          Homer
                                   veegaj.
(17)
             D:FR stand
                          Homer
                                   behind
      'Bart (who is looking to my side) is telling Lisa that the dog
```

(which is facing to Bart's side) is standing behind Homer.'

```
ki'ikash
      Marge
              'o
                    ñeid
                               heg
                                                     'ab
                                      gogs
                                           mo
      Marge
             AUX
                               DET
                                     dog
                                            C:AUX D:FR bite
                    see
(18)
                    viappoi.
             heg
              DET
                    boy
      'Marge sees the dog that bit the boy (while facing her).'
```

The data is analyzed as follows. The particles indicate a relationship between an actant and a viewer. The default case is for the viewer to be the speaker. Predicates that directly or indirectly report another's perceptions reset the viewer value for the embedded context. Verbs of perception, like <code>neid</code> 'see', directly report the subject's perception, and thus any embedded clause takes the subject of the matrix clause as its viewer. Verbs of communication indirectly report the

We define here as a set of points in  $\mathbb{R}^3$  encompassing the viewpoint. Similar to  $\exists (\vec{v})$ , we let  $\exists (\vec{v})$  be the direction 180° from  $\vec{v}$  and  $\exists (\vec{v})$  be the set of directions 90° clockwise or counterclockwise to  $\vec{v}$ . We then define the particles 'ab and 'an as

This general approach fits well with intuitions regarding the potential confusions behind uses of relative directions like left and right: it is unclear whose perspective on the event is being taken.

## 6 Conclusion

perceptions of their subjects.

In order to account for sequencing in general, we have introduced the notion of a parameter name. For each sort (time, location, world etc.) there are up to four parameter names on which the context is defined. Meanings are 'intensionalised' with respect to contexts. The difference in sequencing behaviour can be attributed to the way in which values for parameter names get reassigned. In English, I is tied to utterer, while in Amharic it is tied to the speaker. On the other hand, come and go are not using utterer (nor speaker), but viewpoint. We have presented data from Pima to show that location may in some languages be highly grammaticised,

and that sequence of location and direction phenomena can be observed that are quite like those of tense and person.

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