

An Introduction to Minimalist Grammars:
Complexity of the Shortest Move Constraint

(July 22, 2009)

Gregory Kobele

Humboldt Universität zu Berlin

`kobele@rz.hu-berlin.de`

Jens Michaelis

Universität Bielefeld

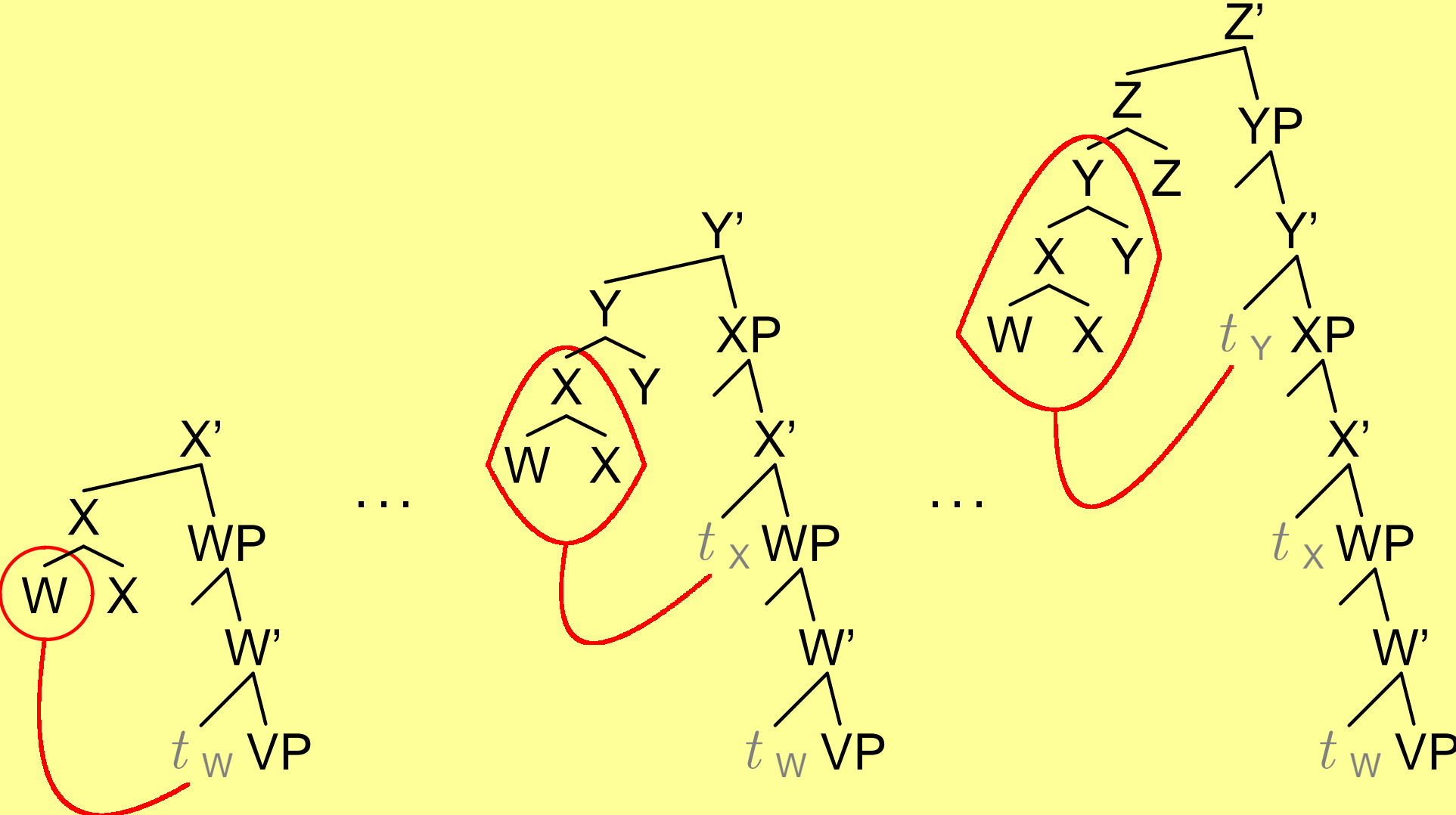
`jens.michaelis@uni-bielefeld.de`

- The implementation of head movement in MGs is in accordance with the HMC
 - demanding a moving head not to pass over the closest c-commanding head.

To put it differently,

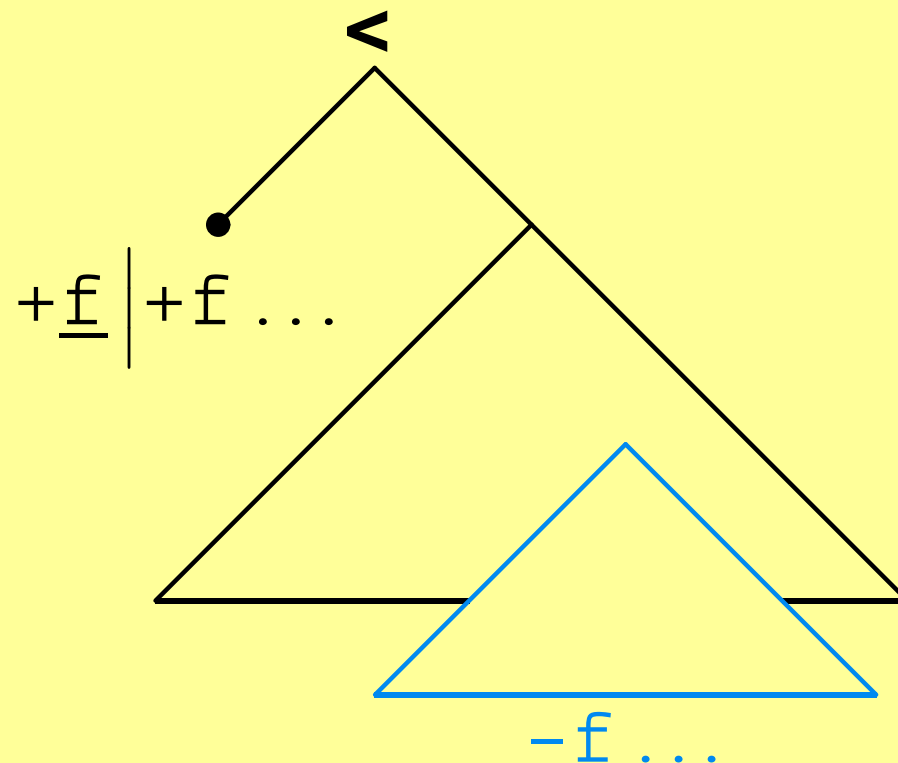
whenever we are concerned with a case of successive head movement, i.e. recursive adjunction of a (complex) head to a higher head, it obeys strict cyclicity.

Successive cyclic left head adjunction

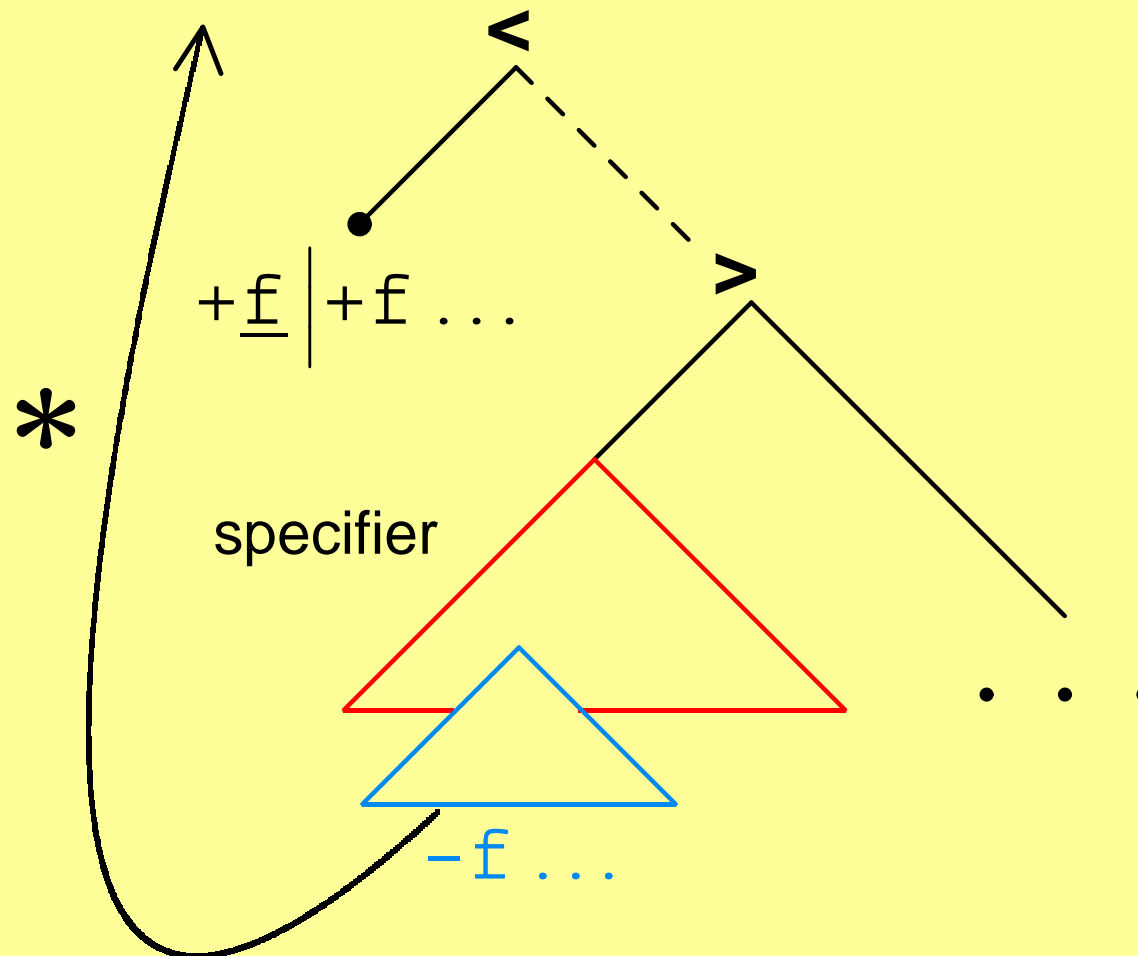


- The number of competing licensee features triggering a movement is (finitely) bounded by n .

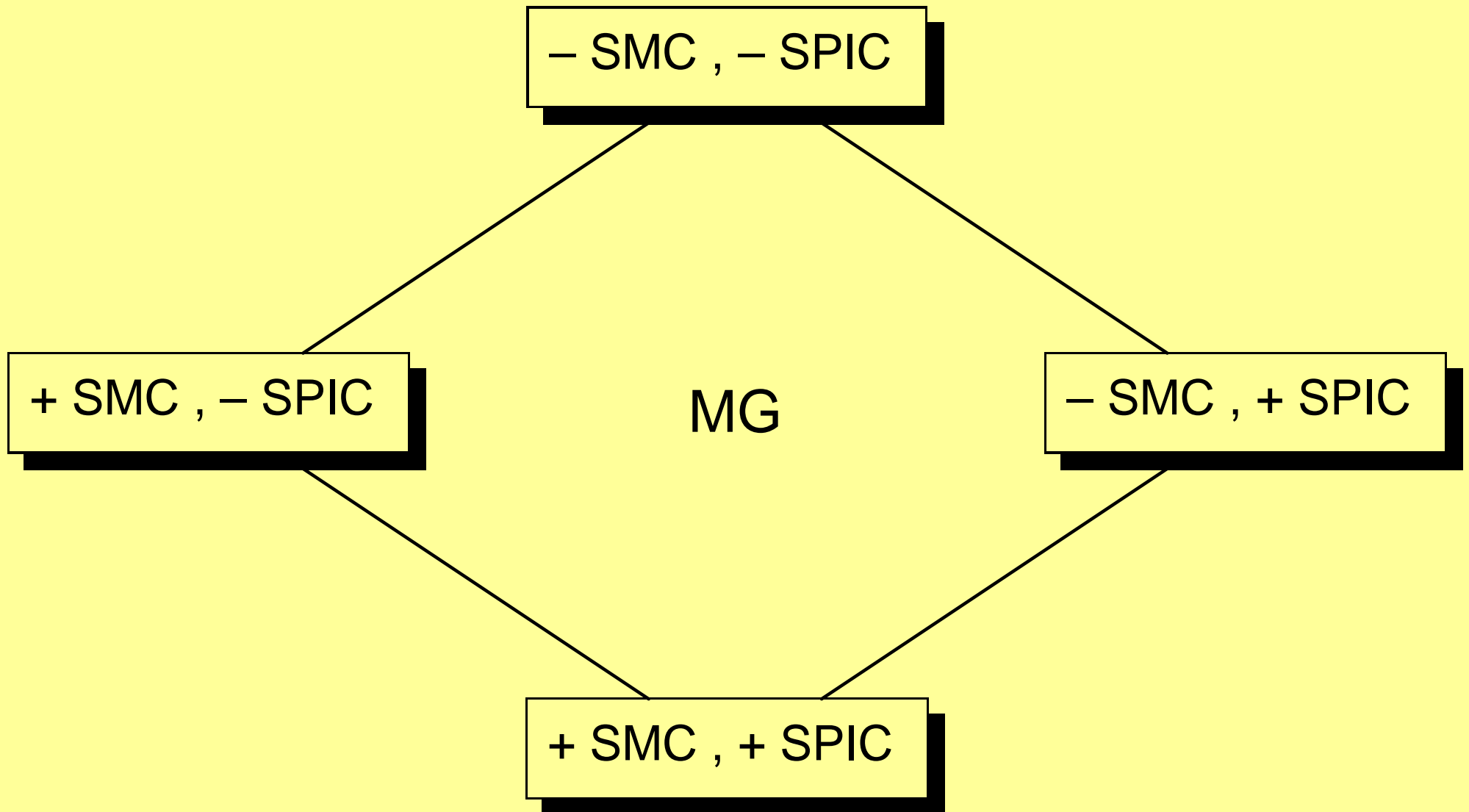
In the strictest version $n = 1$, i.e., there is at most one maximal projection displaying a matching licensee feature:



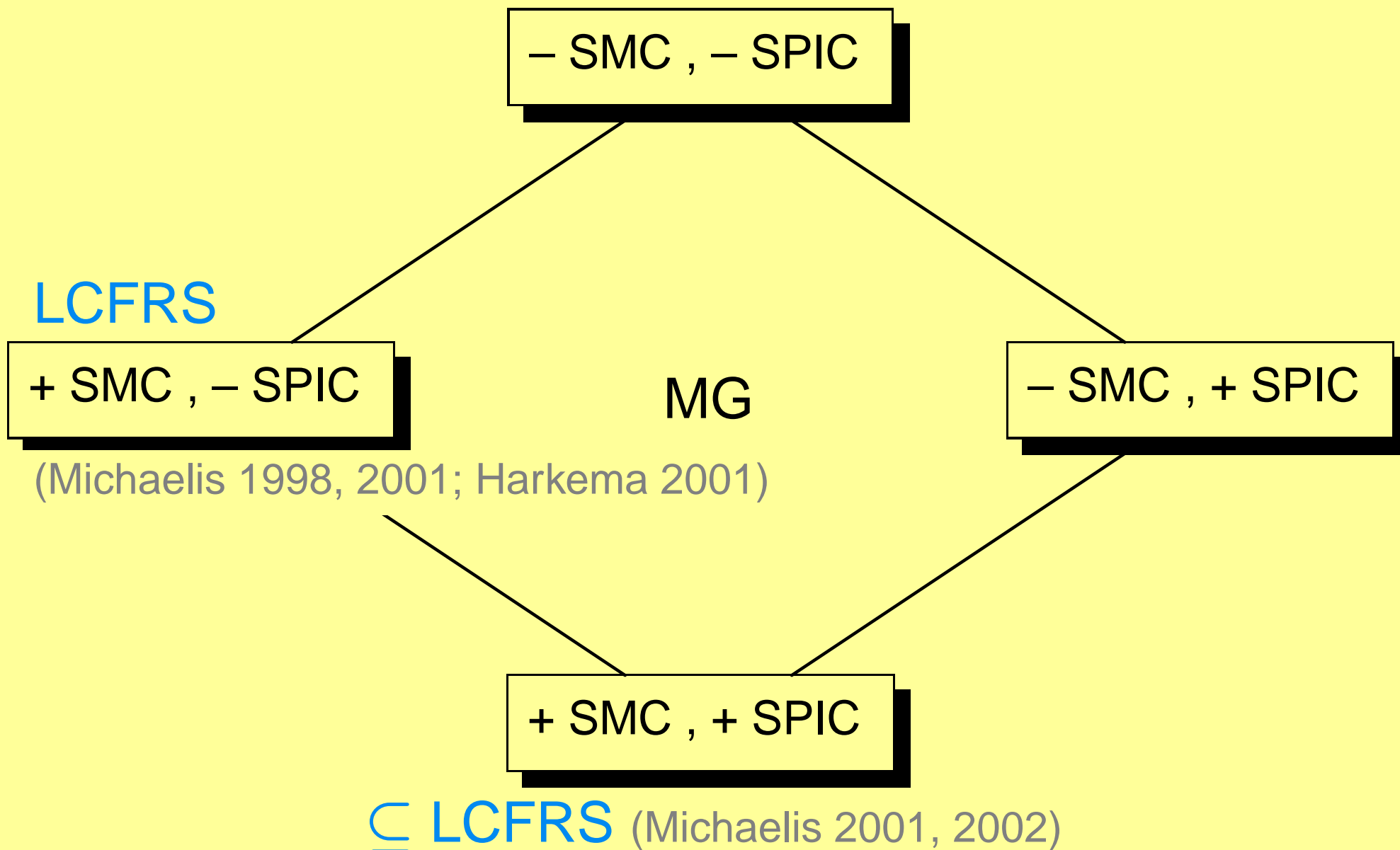
- Proper “extraction” from specifiers is blocked.



SMC and SPIC — restricting the move-operator domain



SMC and SPIC — restricting the move-operator domain



+ SMC , – SPIC — generative capacity

- The crucial methods, in particular,
 - ◆ developed to prove that MGs provide a weakly equivalent subclass of LCFRSs (cf. Michaelis 1998), and
 - ◆ leading to the succinct, chain-based MG-reformulation presented in Stabler & Keenan 2000 [2003] — reducing “classical” MGs to their “bare essentials:”
- Defining a finite partition on the “relevant” MG-tree set,
 - giving rise to a finite set of nonterminals in LCFRS-terms,
 - deriving all possible “terminal yields.”

Reducing an MG(+SMC,-/+SPIC)

Let $G = \langle \text{Features}, \text{Lexicon}, \Omega, c \rangle$ be an MG

A minimal expression $\tau \in \text{Closure}(G)$ is **relevant** : \iff

for each licensee $-x$, there is at most one maximal projection in τ that displays $-x$.

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A minimal expression $\tau \in \text{Closure}(G)$ is **relevant** : \Leftrightarrow

for each licensee $-x$, there is at most one maximal projection in τ that displays $-x$.

- In fact, this kind of structure is **characteristic of each expression $\tau \in \text{Closure}(G)$ involved in creating a complete expression in G due to the SMC.**

A finite partition of set of relevant expressions

Basic idea: consider relevant $\tau \in \text{Closure}(G)$

- Reduce τ to a tuple such that for each maximal projection displaying an unchecked syntactic feature, there is exactly one component of the tuple consisting of the projection's head-label, but with the suffix of non-syntactic features truncated.

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↗ only **finitely many equivalence classes**

Relevance:

The resulting tuple has at most $m+1$ components, $m = |\text{Licensees}|$.

Structure building by cancellation of features:

Each tuple component is the suffix of the syntactic prefix of the label of a lexical item.

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⚡→ only **finitely many equivalence classes**

Relevance:

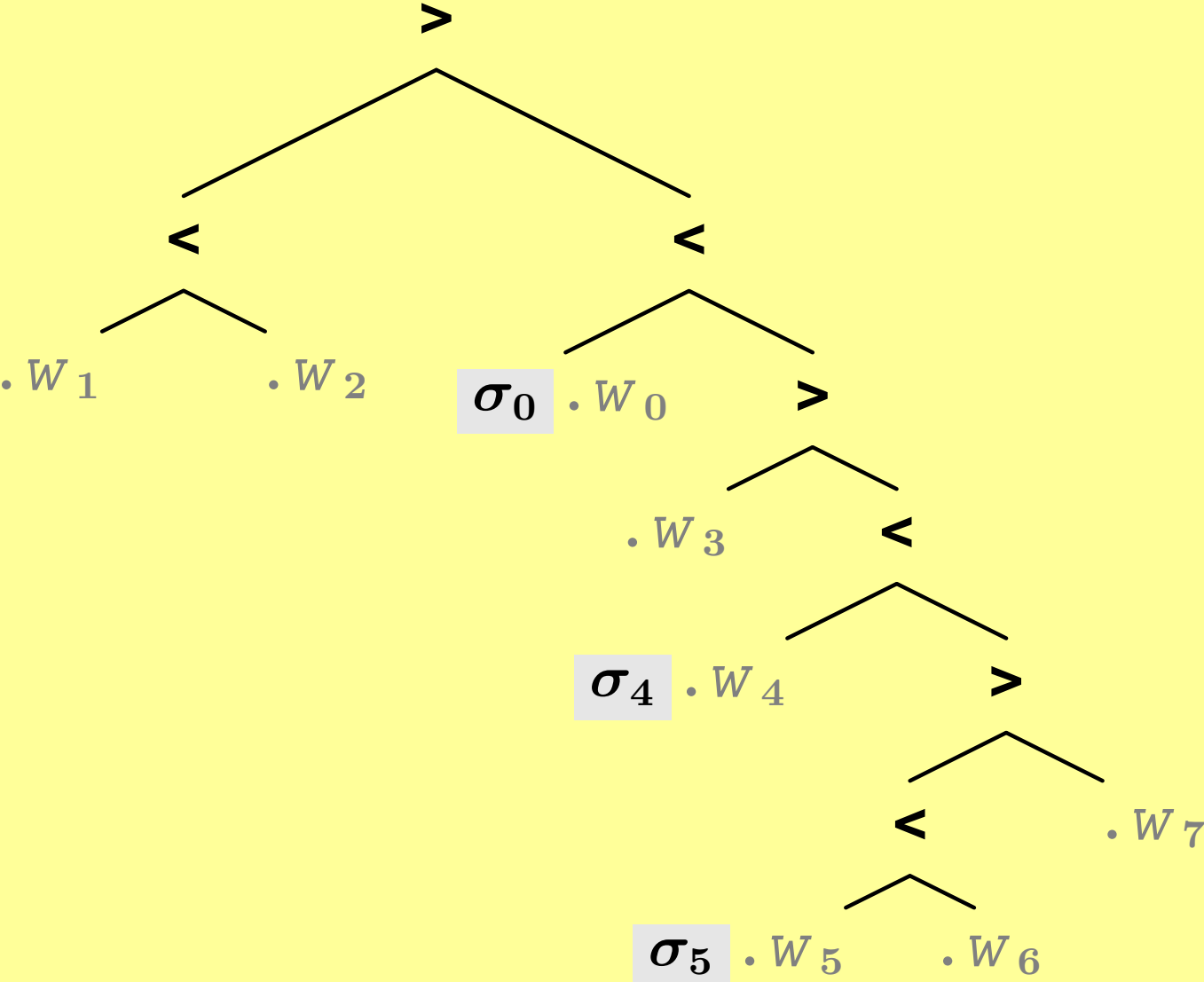
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Structure building by cancellation of features:

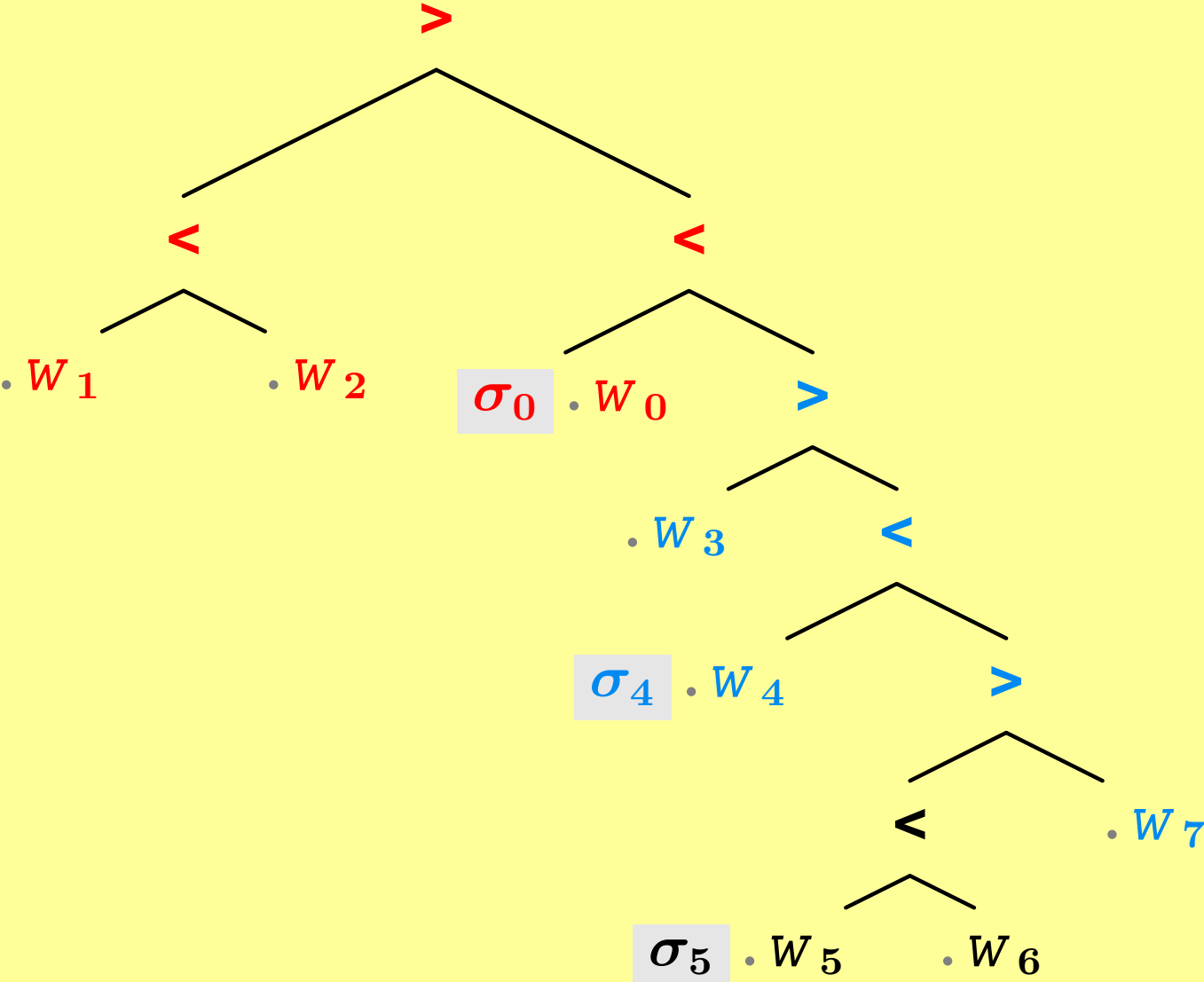
Each tuple component is the suffix of the syntactic prefix of the label of a lexical item.

⚡→ regarding the partition, applications of 'merge' and 'move' do not depend on the chosen representatives

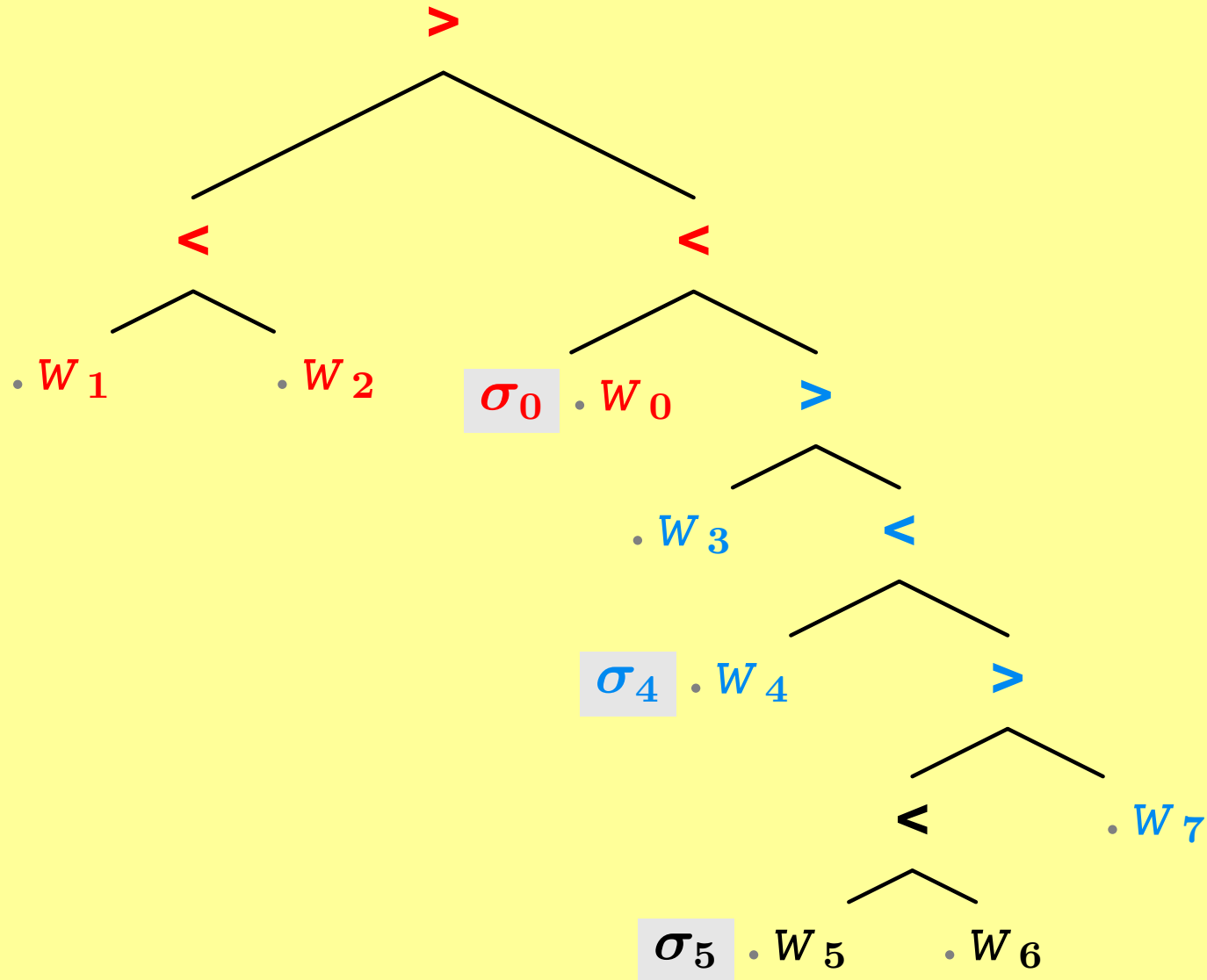
Reducing an MG(+SMC,-/+SPIC)



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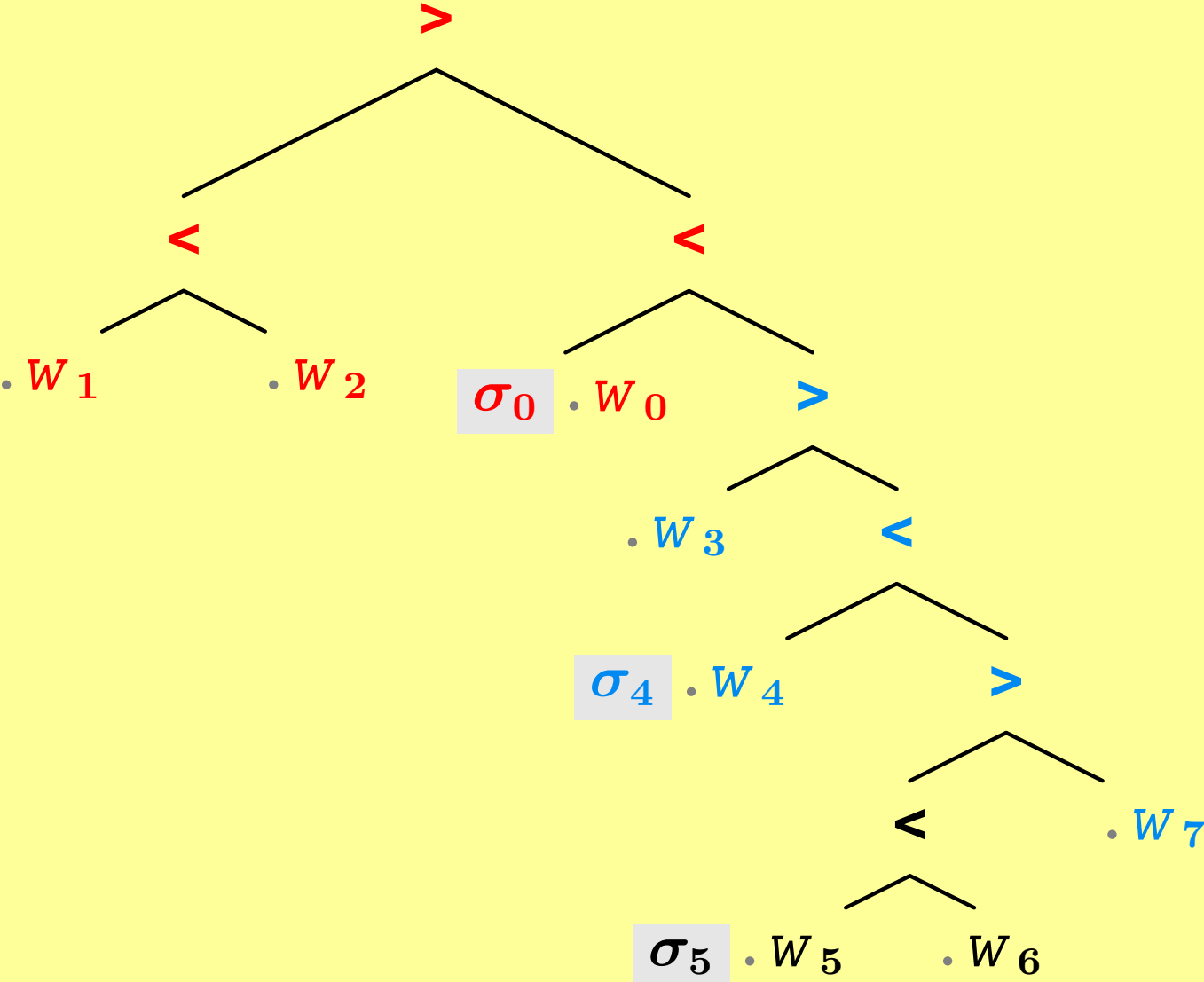


Reducing an MG(+SMC,-/+SPIC)



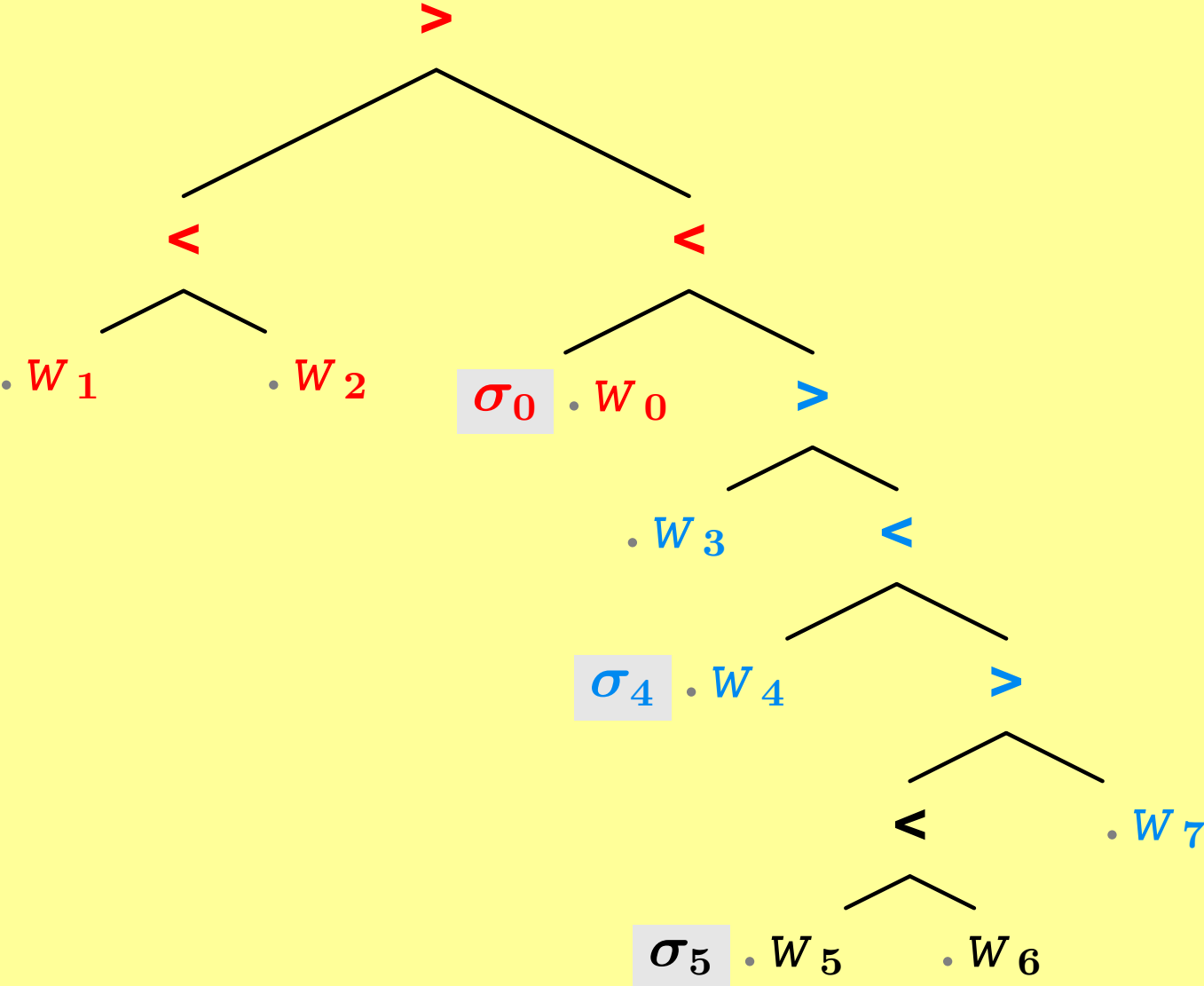
$\langle \sigma_0 .W_1W_2W_0 , \sigma_4 .W_3W_4W_7 , \sigma_5 .W_5W_6 \rangle$

Reducing an MG(+SMC,-/+SPIC)



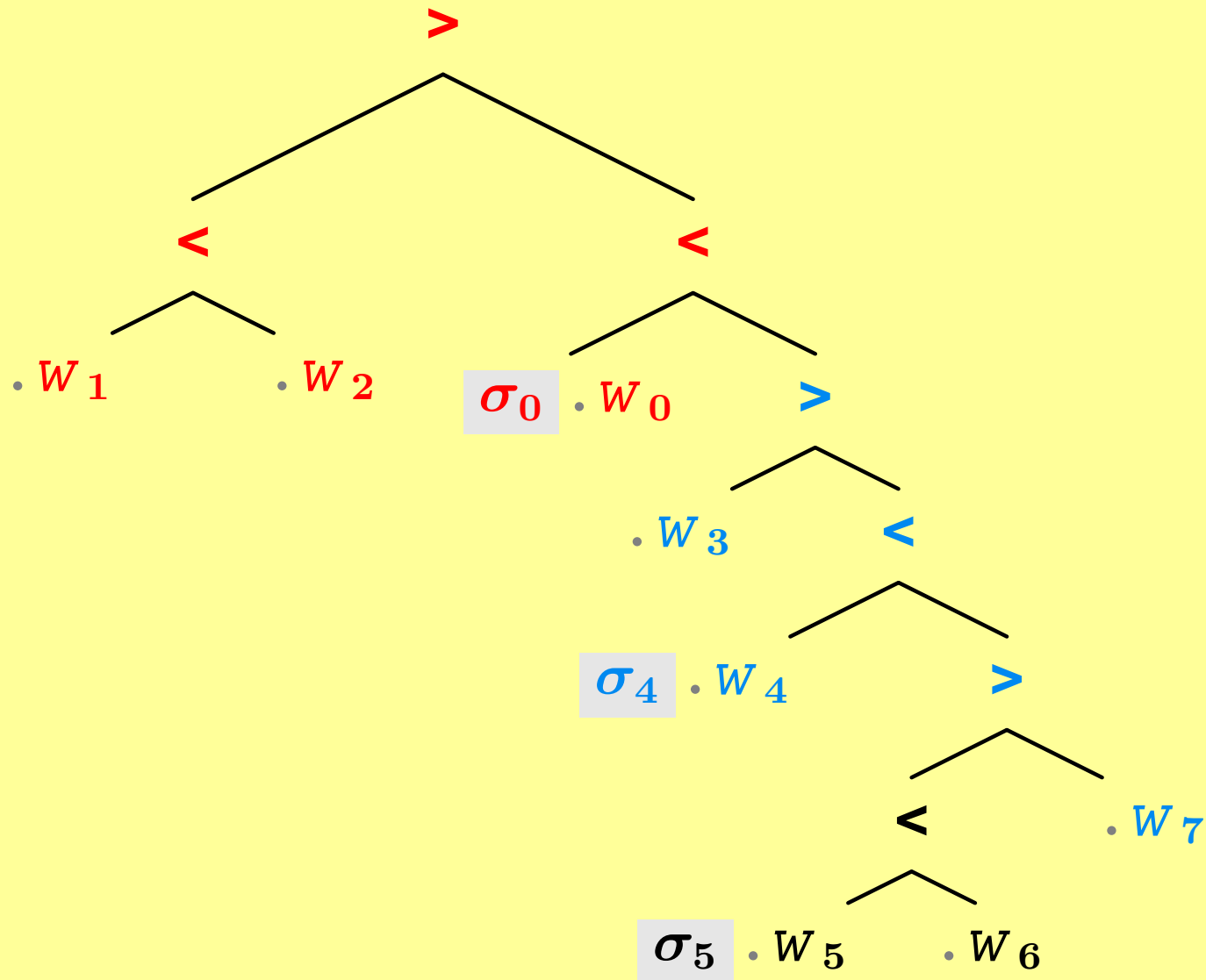
$\langle \sigma_0, \sigma_4, \sigma_5 \rangle$

Reducing an MG(+SMC,-/+SPIC)



$\langle \sigma_0, \sigma_4, \sigma_5 \rangle$

Reducing an MG(+SMC,-/+SPIC)



$$\langle \sigma_0, \sigma_4, \sigma_5 \rangle \Rightarrow \langle W_1 W_2 W_0, W_3 W_4 W_7, W_5 W_6 \rangle$$

MG-example 2

(α_0) = t . c . *that*

(α_5) v . *laugh*

(α_1) = t . + wh . c . \emptyset

(α_6) = n . d . - k . *the*

(α_2) = \tilde{v} . + k . t . \emptyset

(α_7) = n . d . - k . - wh . *which*

(α_3) = v . = d . \tilde{v} . \emptyset

(α_8) n . *king*

(α_4) = d . + k . v . *eat*

(α_9) n . *pie*

MG-example 2

=n .d .-k .-wh .*which*

n .*pie*

MG-example 2

$:: \hat{=} \text{simple}$, $: \hat{=} \text{complex}$

=n.d.-k.-wh.which

$\langle \text{=n.d.-k.-wh.which}, :: \rangle$

n.pie

$\langle \text{n.pie}, :: \rangle$

MG-example 2

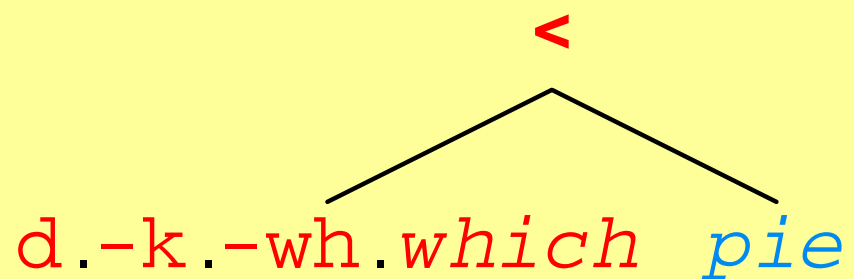
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MG-example 2

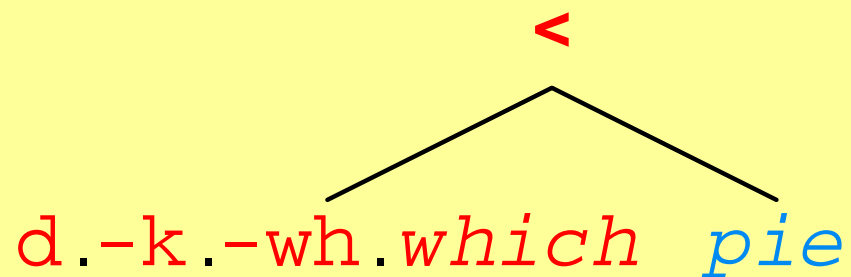
$:: \hat{=} \text{simple}$, $: \hat{=} \text{complex}$

=n.d.-k.-wh.which

$\langle \text{=n.d.-k.-wh.which}, :: \rangle$

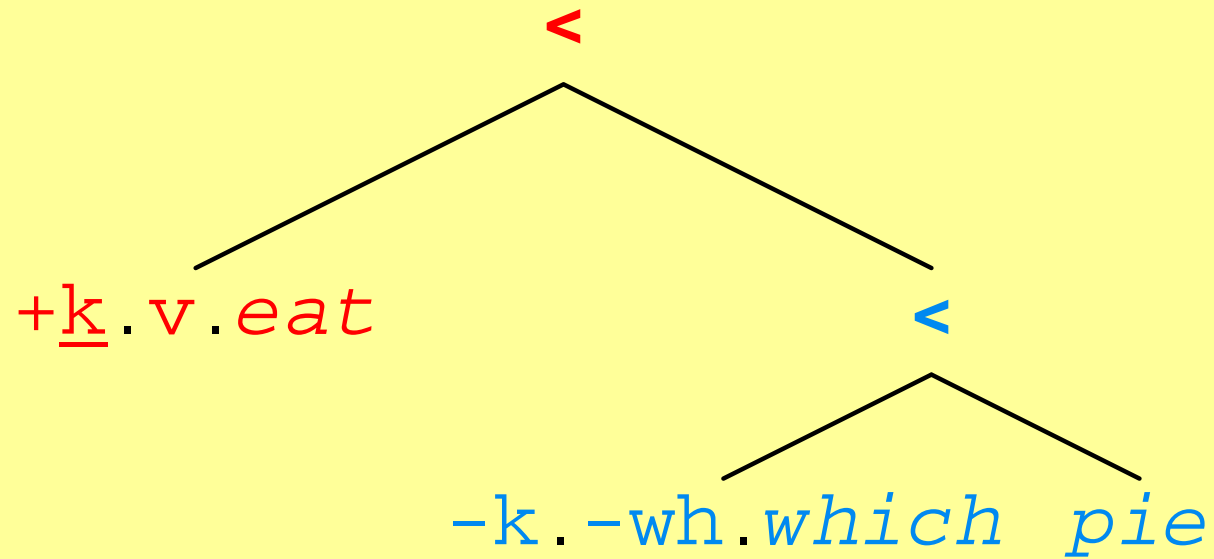
n.pie

$\langle \text{n.pie}, :: \rangle$



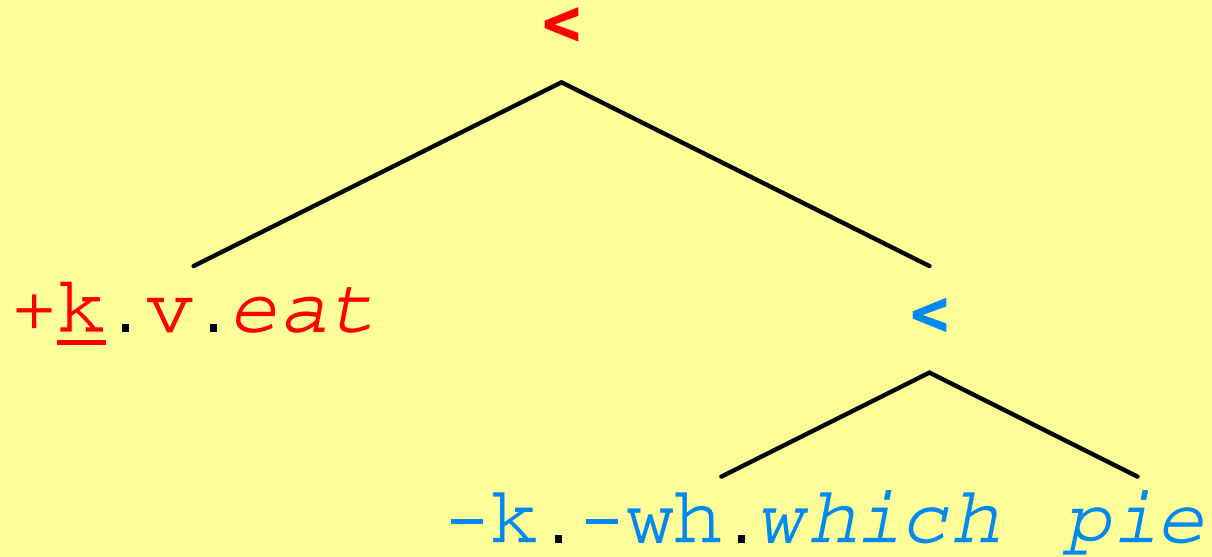
$\langle \text{d.-k.-wh.which pie}, : \rangle$

MG-example 2



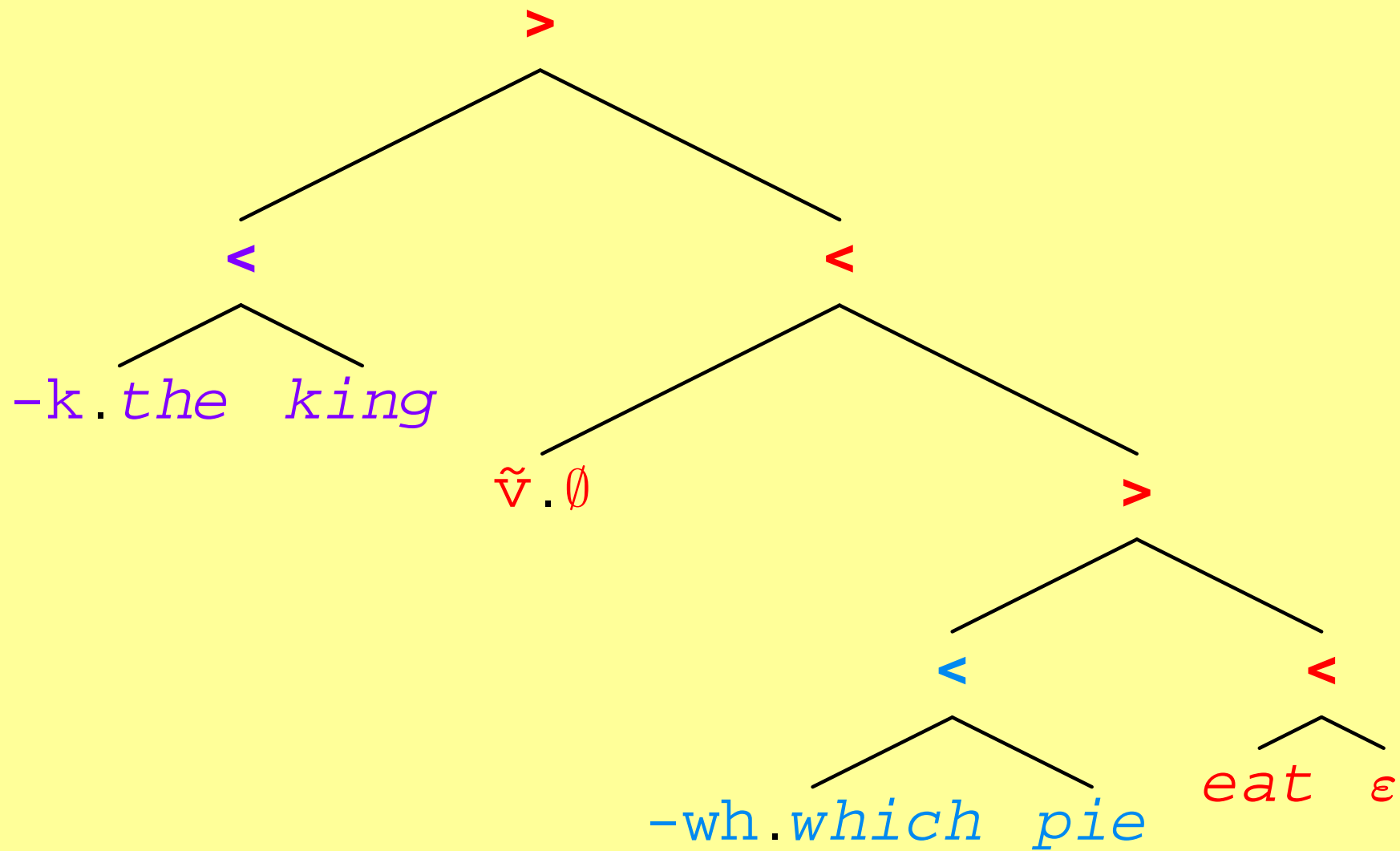
MG-example 2

:: $\hat{=}$ simple , : $\hat{=}$ complex



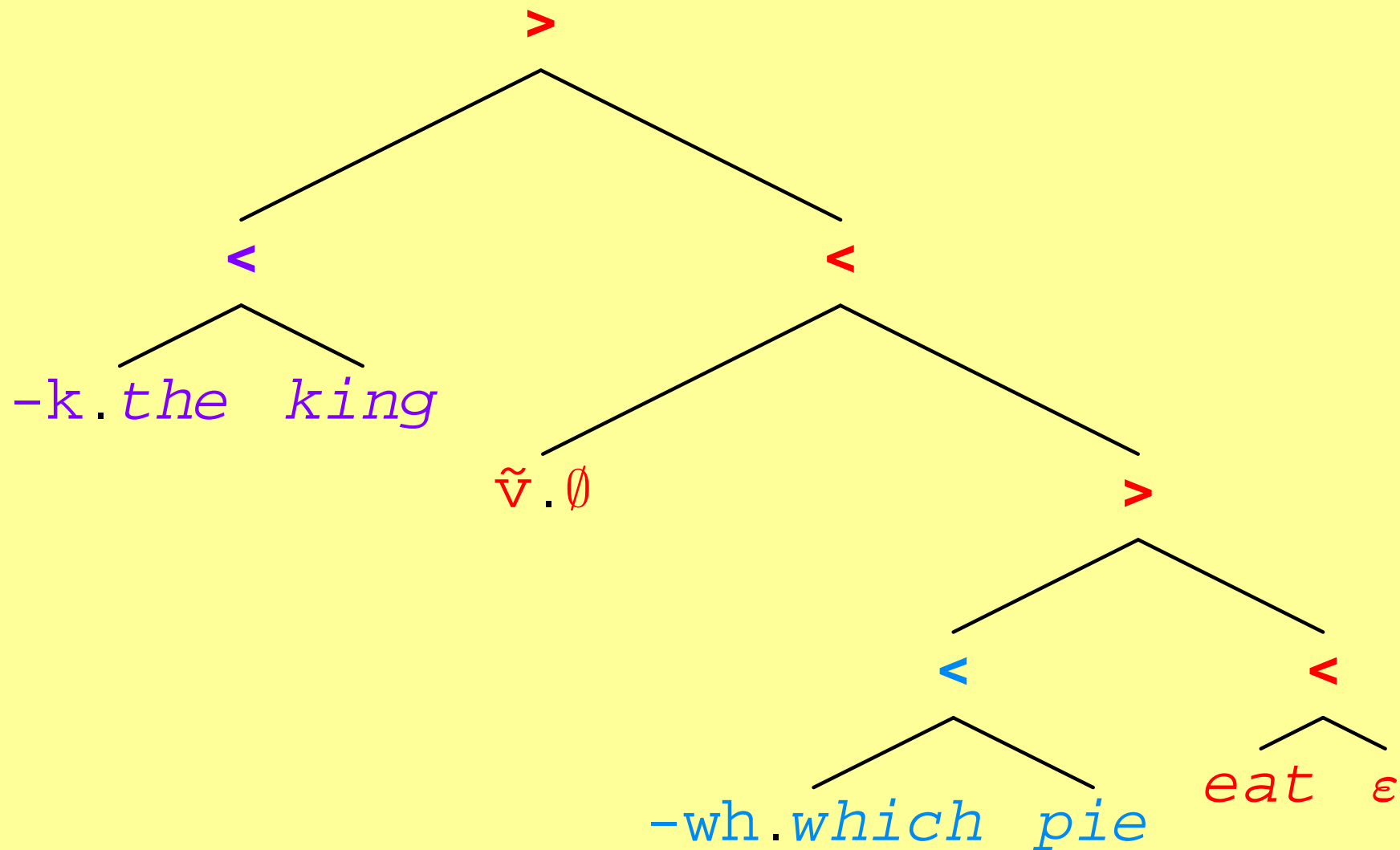
$\langle +\underline{k}.v.eat, -k.-wh.which\ pie, : \rangle$

MG-example 2



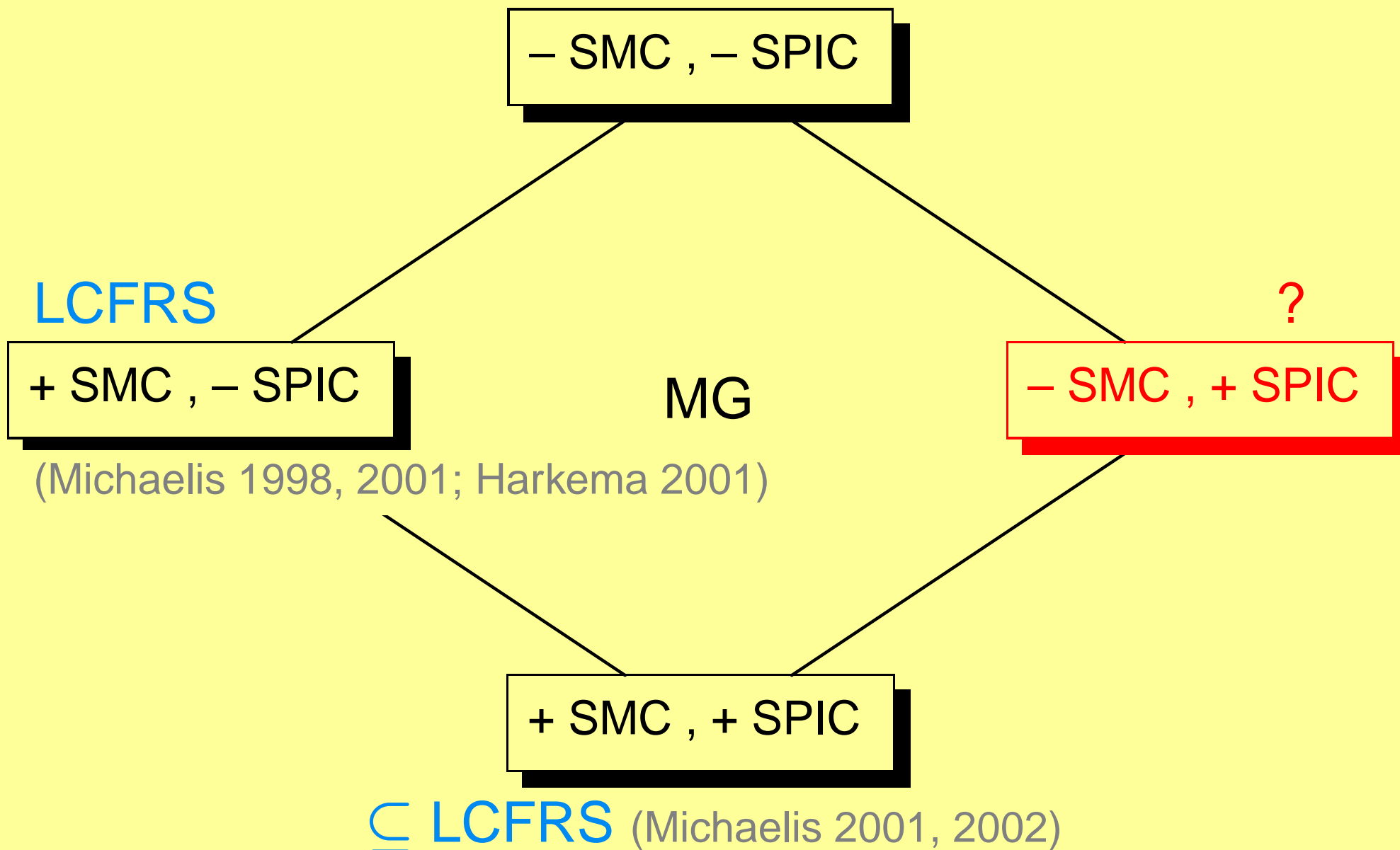
MG-example 2

$:: \hat{=}$ simple , $: \hat{=}$ complex



$\langle \tilde{v}.eat, -wh.which\ pie, -k.the\ king, : \rangle$

SMC and SPIC — restricting the move-operator domain

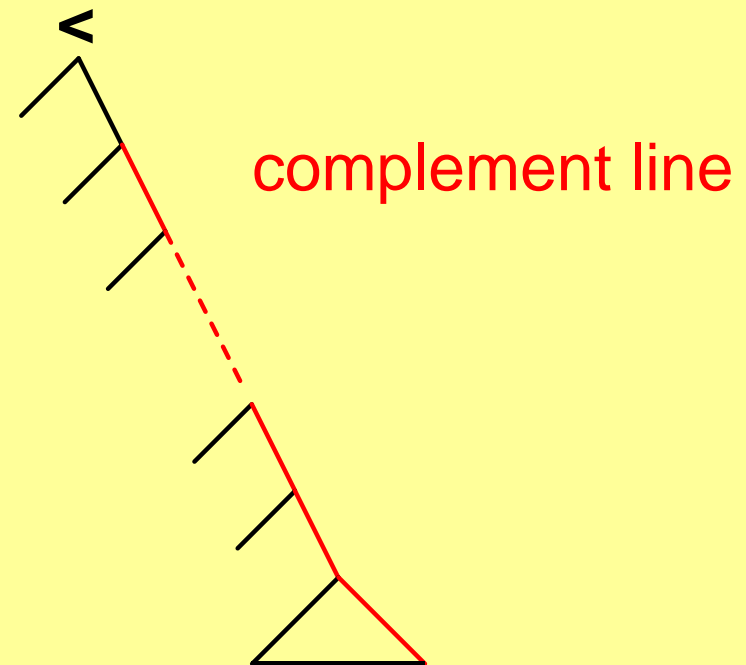
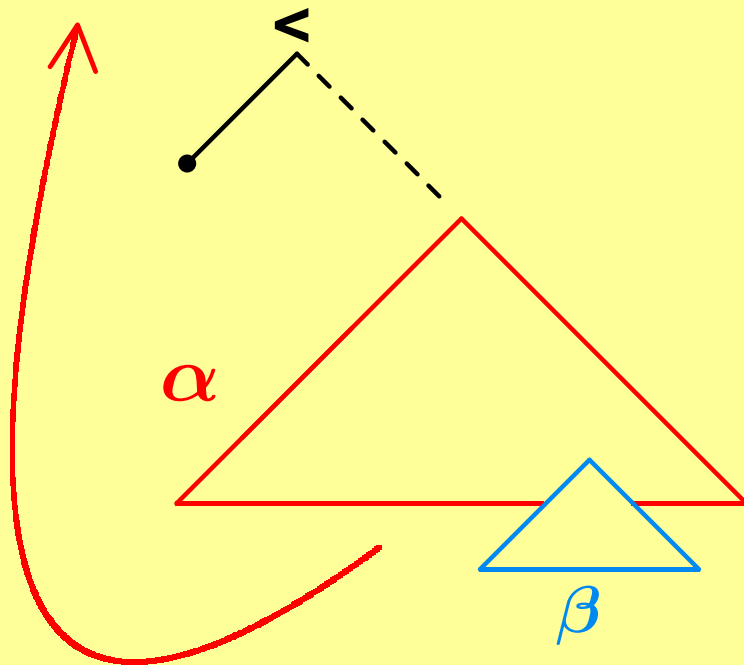


– SMC , + SPIC — generative capacity

- Gärtner & Michaelis 2005 shows that $MG(-SMC,+SPIC)$ s allow derivation of non-mildly context-sensitive languages.
- Kobele & Michaelis 2005 shows that, in fact, **every recursively enumerable language can be derived by an $MG(-SMC,+SPIC)$** .
This is true for essentially two reasons:

– SMC , + SPIC — generative capacity

- Because of the SPIC, movement of a constituent α into a specifier position freezes every proper subconstituent β within α .
- Without the SMC, therefore, the complement line of a tree can technically be used as two independent counters, or, as a queue.



MG-example — complexity results concerning LCs

- An example of a non-mildly context-sensitive MG(−SMC,+SPIC) deriving a language without constant growth property, namely,

$$\{ a^{2^n} \mid n \geq 0 \} = \{ a, aa, aaaa, aaaaaaaaa, \dots \}$$

1 2 4 8 ...

MG-example — complexity results concerning LCs

w.-m

=w.x.-l

=x.+m.y.-m

=y.+l.z.-l

=z.y.-l

=z.x.-l

=x.+m.c

=c.+l.c.a

MG-example — complexity results concerning LCs

licensee $-m$ “marks”
end/start of “outer” cycle

$w.-m$

“initialize”

$=w.x.-1$

end “outer” cycle “appropriately:”
check licensee $-m$

$=x.+m.y.-m$

“outer” cycle

start new “outer” cycle:
introduce new licensee $-m$

$=y.+1.z.-1$

“reintroduce” and “double”
the just checked licensee -1

$=z.y.-1$

“inner” cycle

$=z.x.-1$

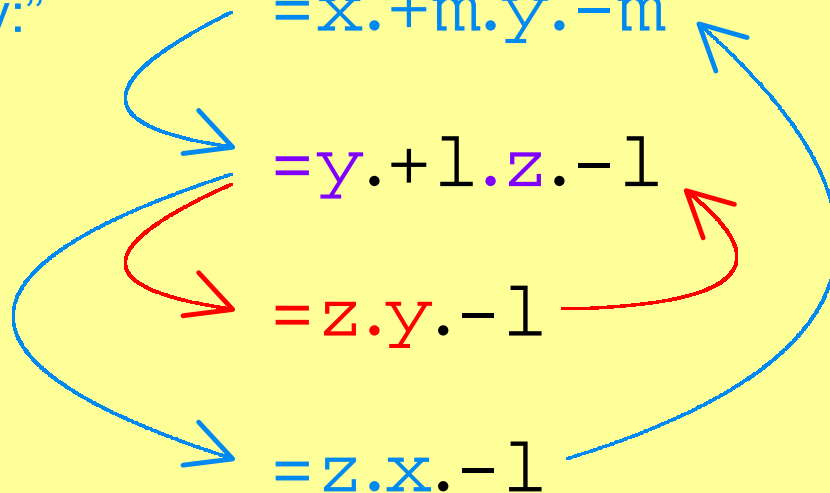
leave final cycle “appropriately:”
check licensee $-m$

$=x.+m.c$

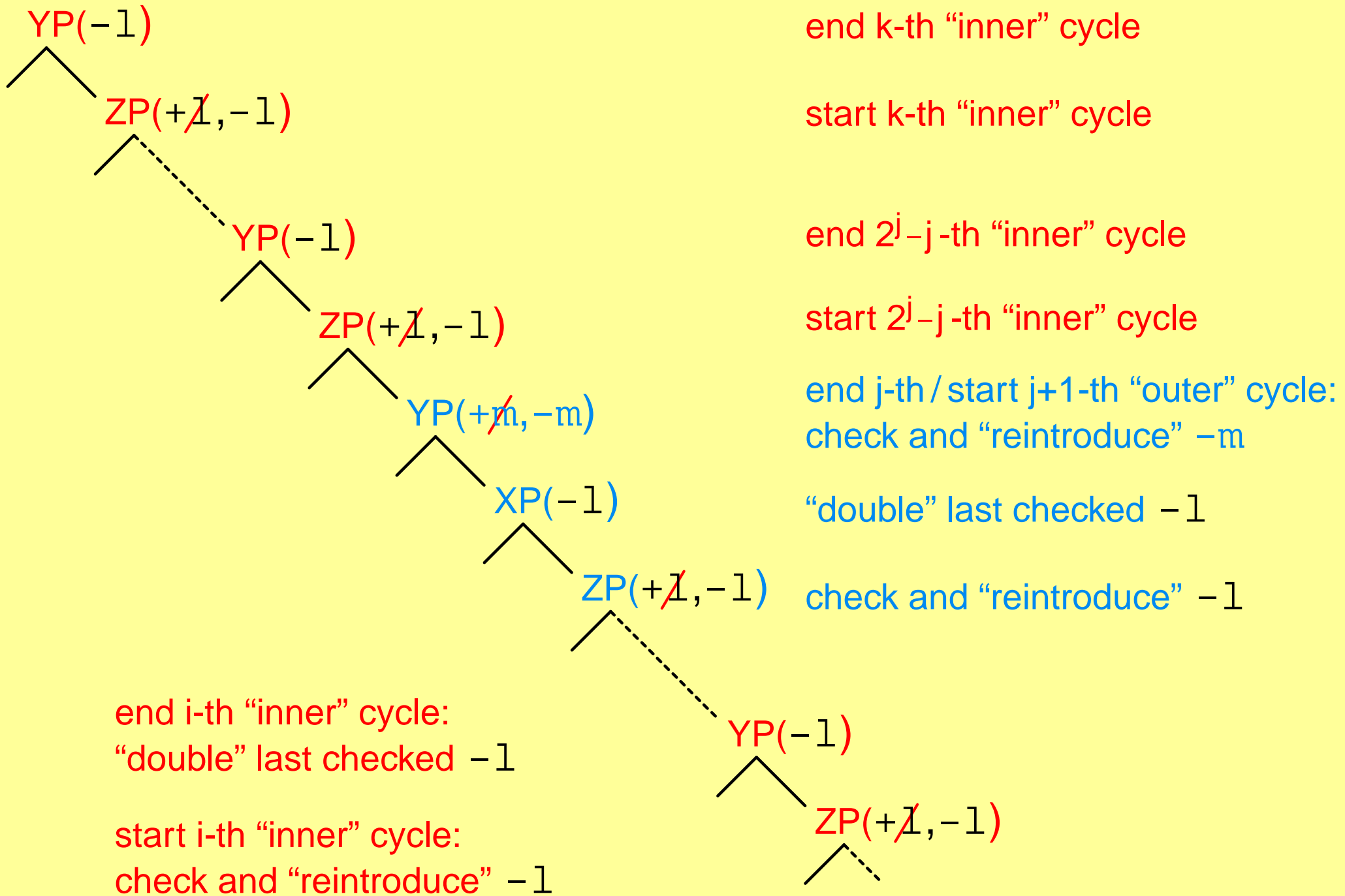
“finalize”

check successively licensee -1 ,
each time introducing an a

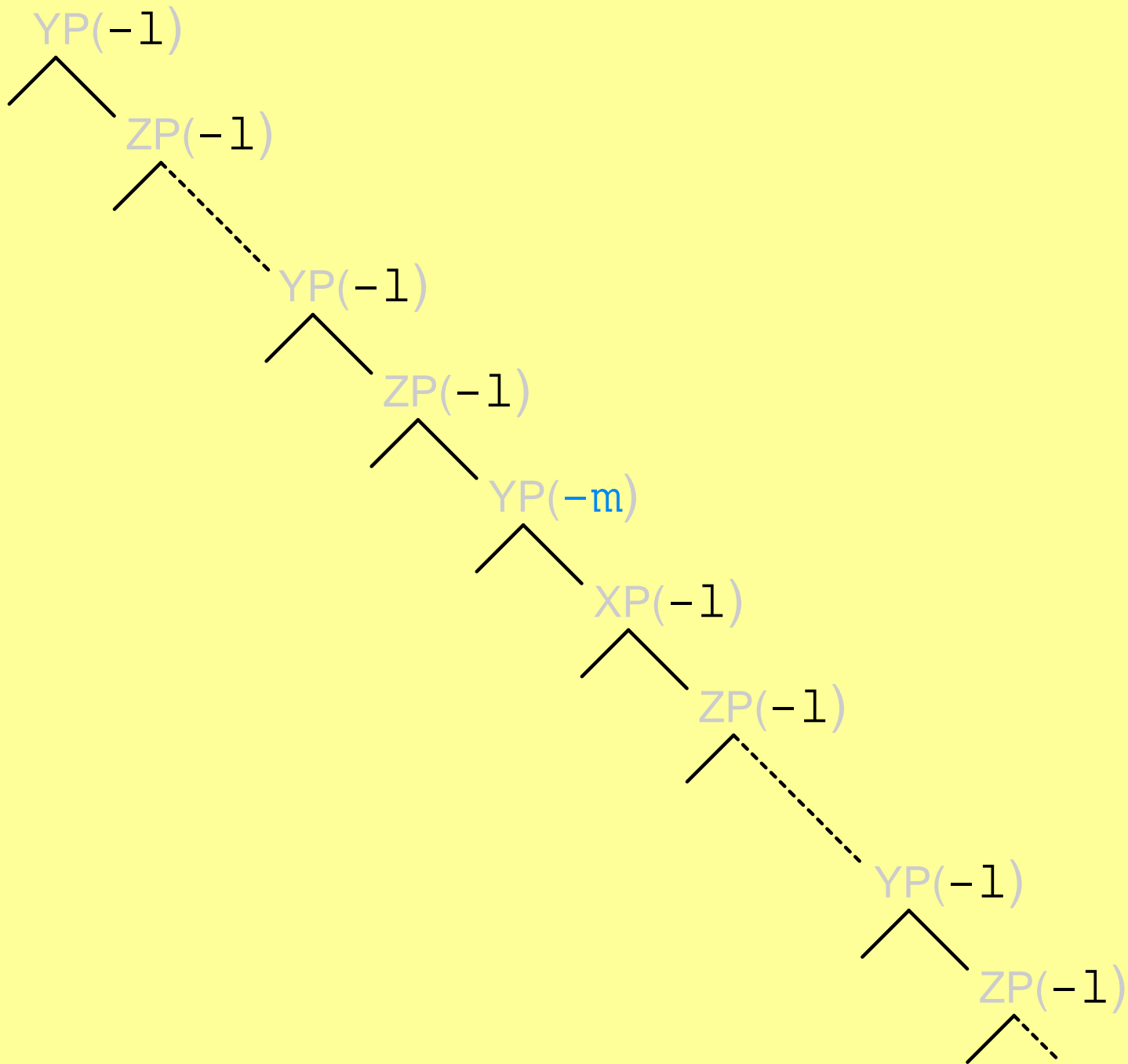
$=c.+1.c.a$



MG-example — complexity results concerning LCs



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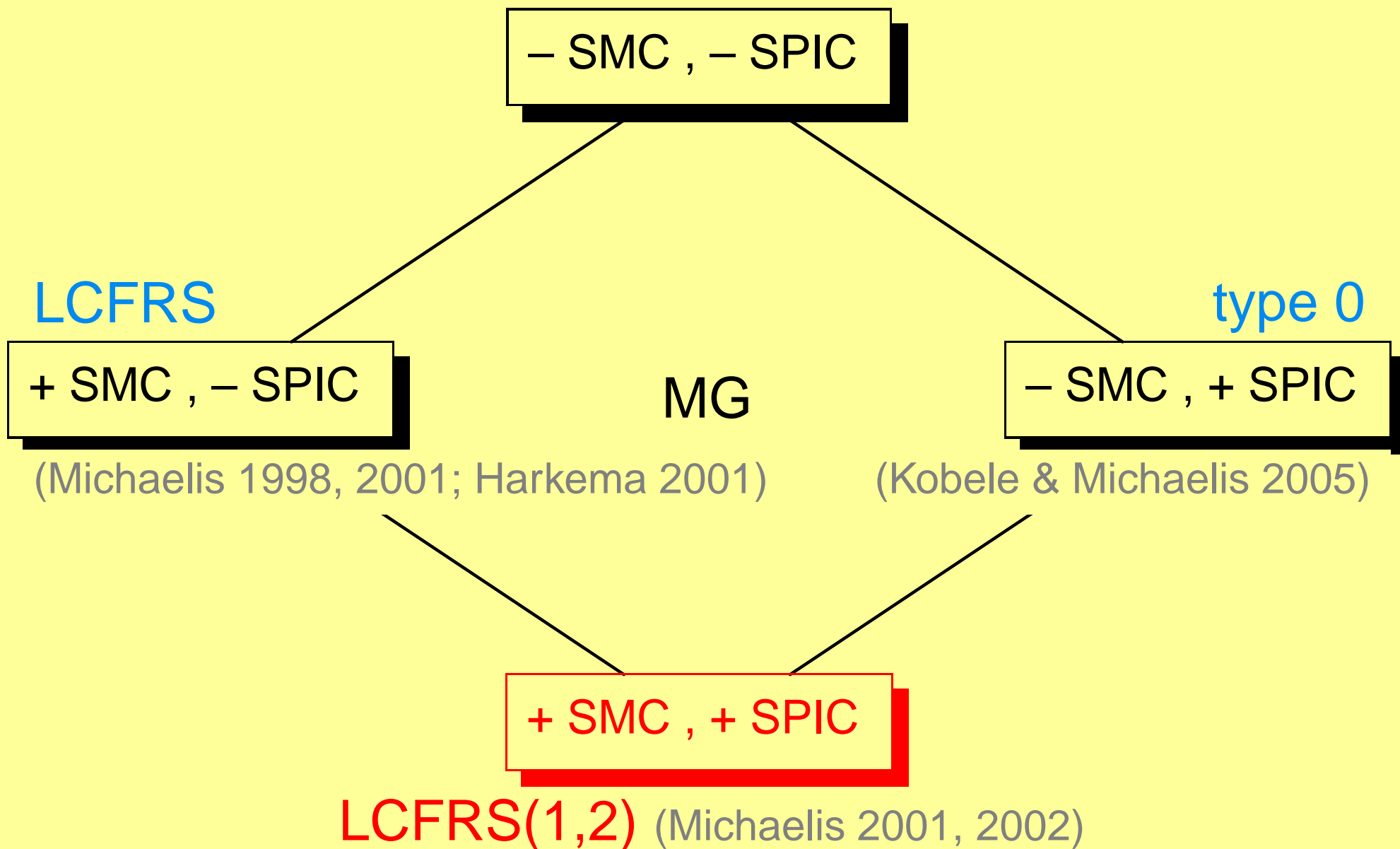
MG-example — complexity results concerning LCs

- Starting the “outer” cycle, the currently derived tree shows 2^n successively embedded complements on the complement line each with an unchecked instance of -1 , and a lowest one with an unchecked instance of $-m$.
- Going through the cycle provides a successive “roll-up” of those complements in order to check the displayed features. Thereby, 2^{n+1} successively embedded complements on the complement line are created, again, all displaying feature -1 and a lowest one displaying feature $-m$.
- Leaving the cycle procedure after a cycle has been completed, leads to a final checking of the displayed licensees, where for each instance of -1 an instance of a is introduced in the structure.

+ SMC , + SPIC — generative capacity

- In contrast to the – SMC , + SPIC - case,
adding the SPIC to the SMC has a restrictive effect (Michaelis 2005)

+ SMC , + SPIC — generative capacity



LCFRS(1,2) — a restricted LCFRS-normal form

An LCFRS $G = \langle N, T, F, R, S \rangle$ is an **LCFRS(1,2)** iff

- ◆ each nonterminating rule is of the form $A \rightarrow f(B)$ or $A \rightarrow f(B, C)$,
- ◆ if $A \rightarrow f(B, C)$, nonterminal B derives only simple terminal strings.

LCFRS(1,2) — a restricted LCFRS-normal form

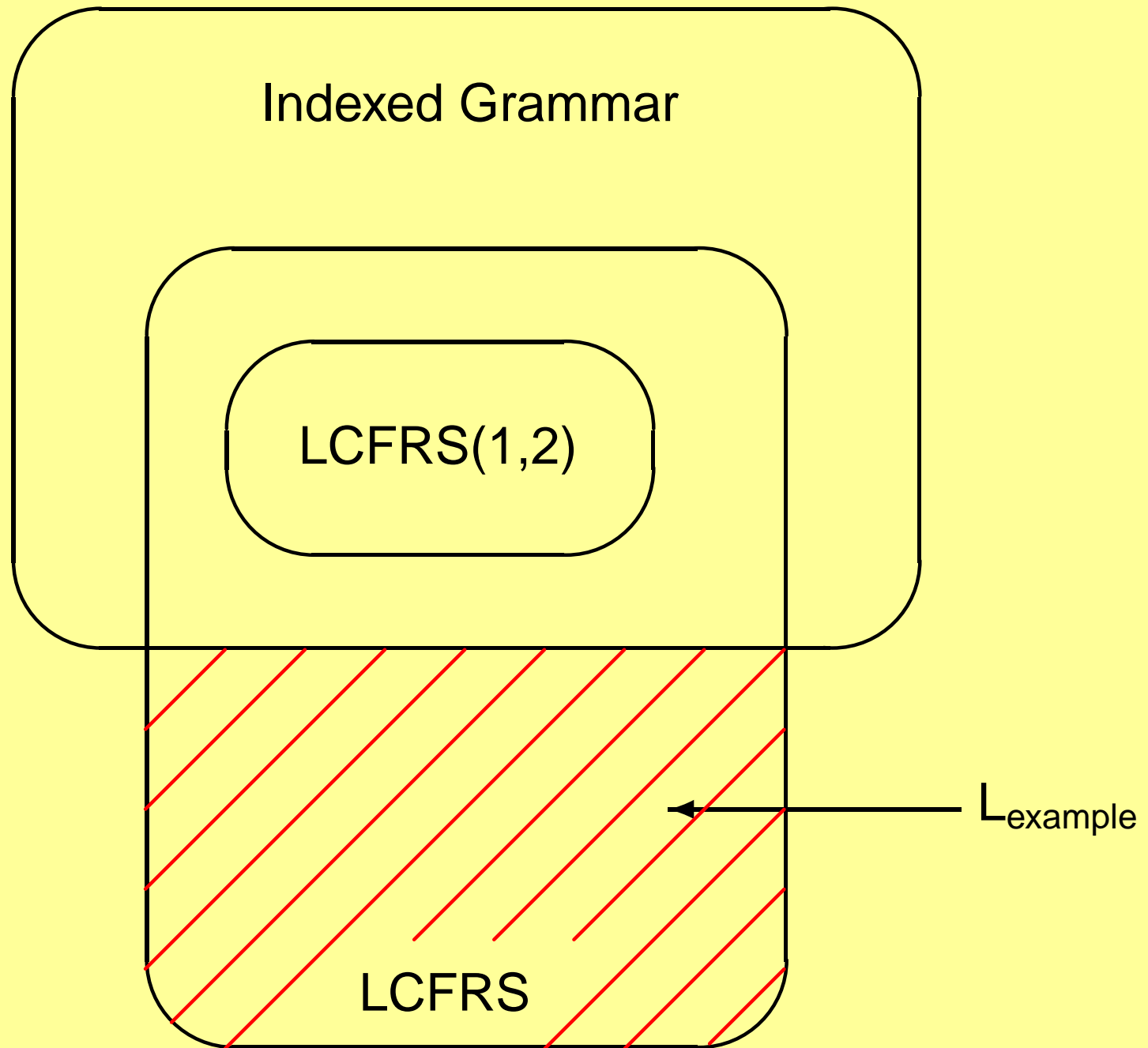
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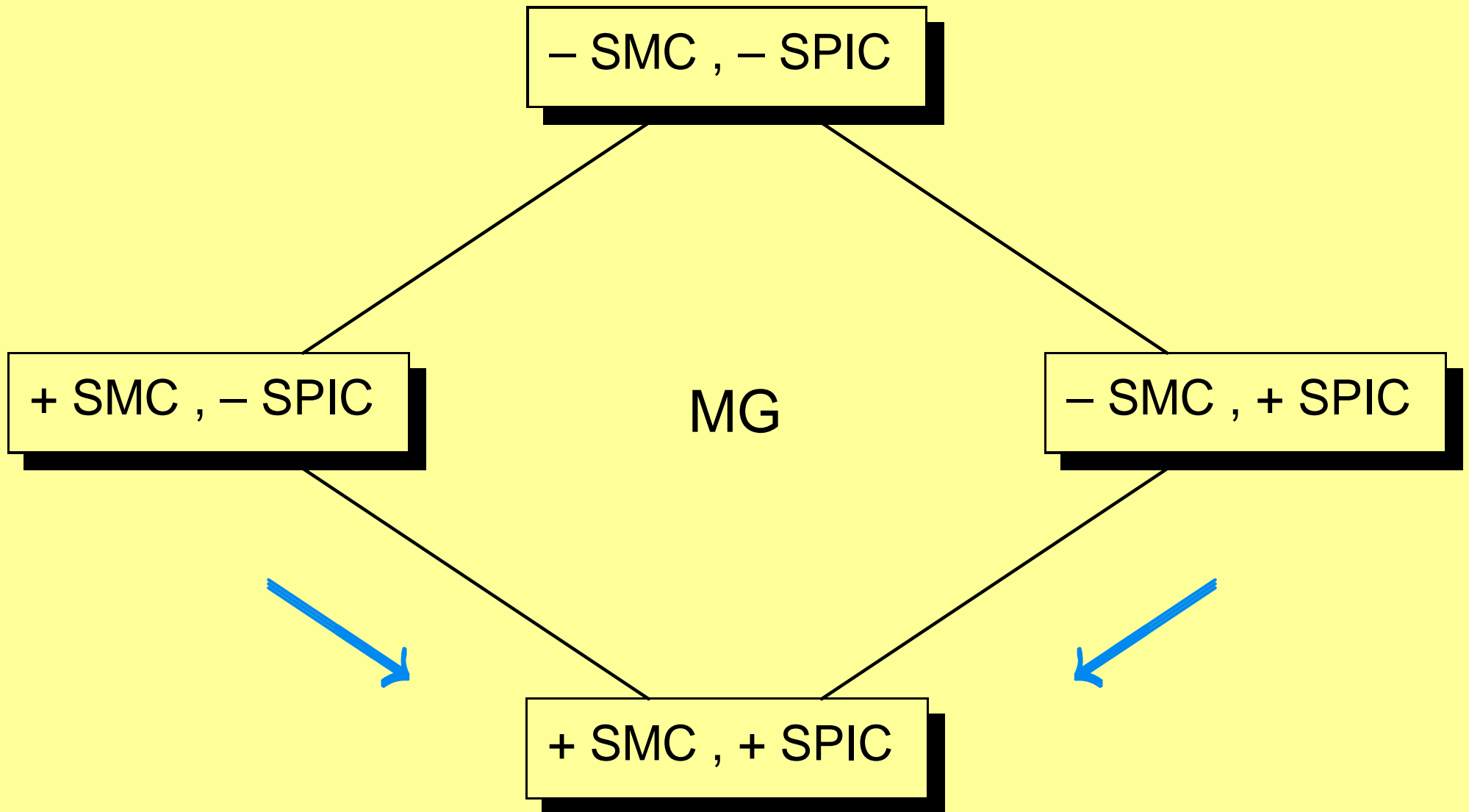
■ Excludes a **non-indexed, but LCFRS-string language** such as:

$$\left\{ w_1 \cdots w_n z_n w_n \cdots z_1 w_1 z_0 w_n^R \cdots w_1^R \mid w_i \in \{a, b\}^+, z_n \cdots z_0 \text{ Dyck word} \right\}$$

LCFRS(1,2) — a restricted LCFRS-normal form

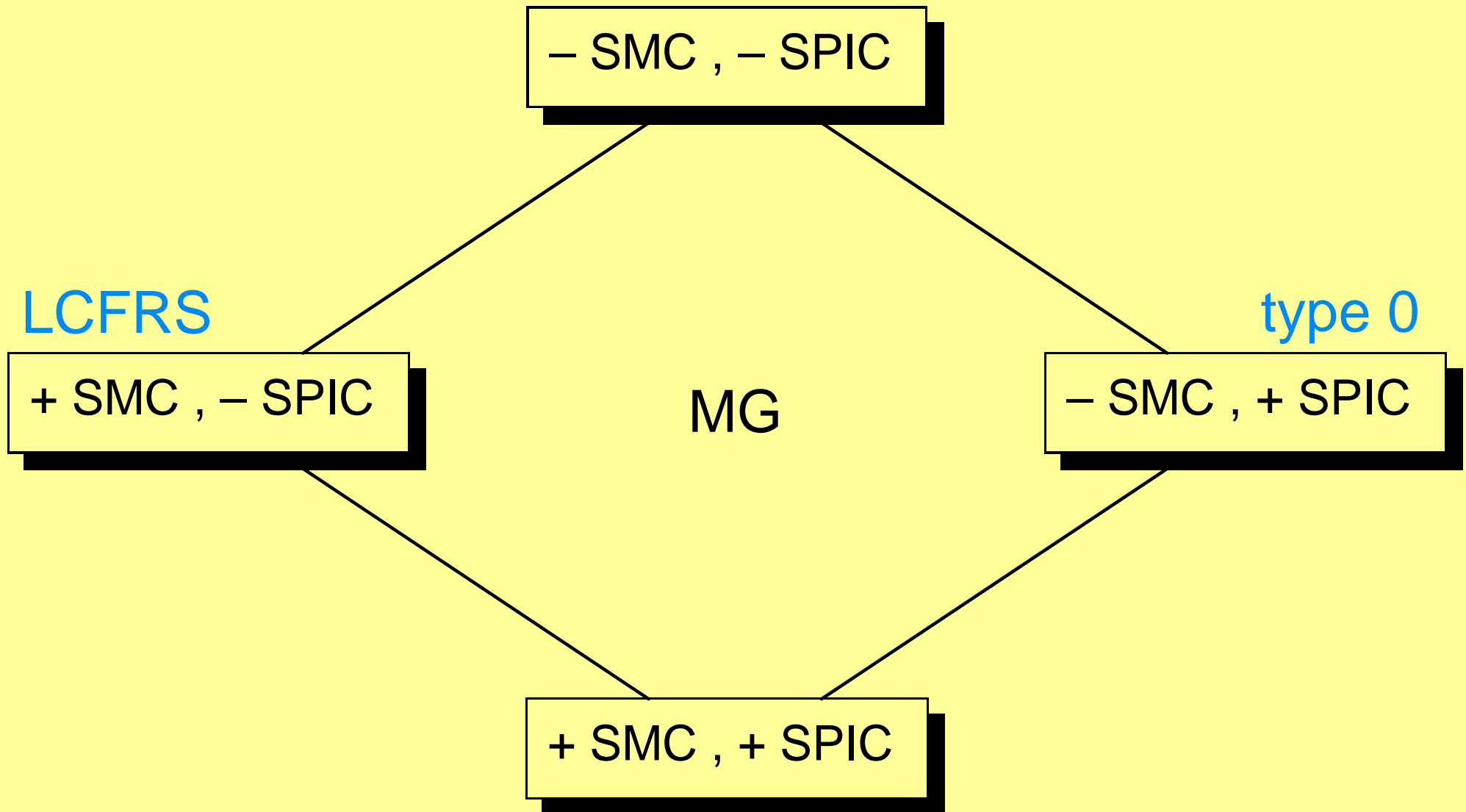


SMC and SPIC — restricting the move-operator domain

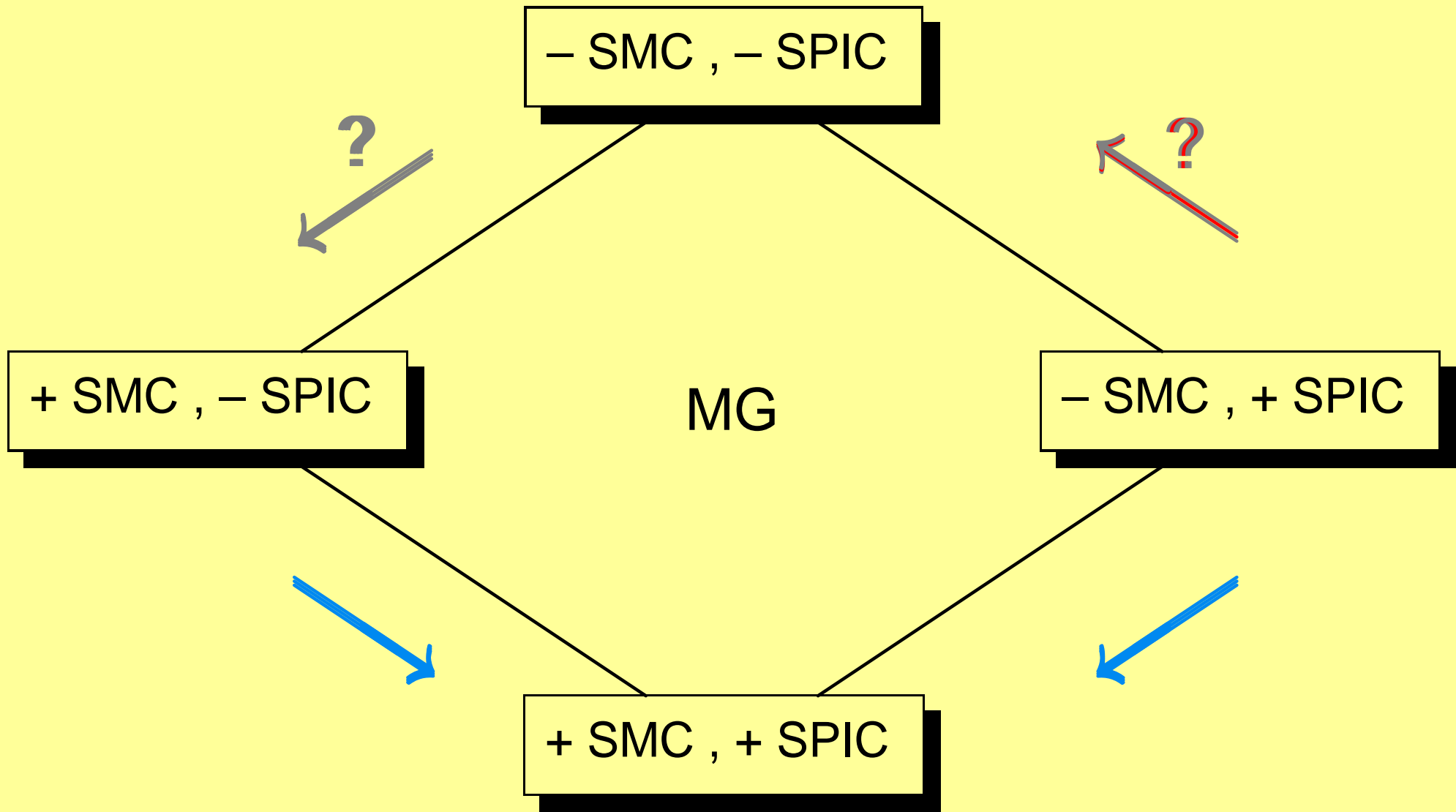


SMC and SPIC — restricting the move-operator domain

MELL-proof-search (Salvati 2008)



SMC and SPIC — restricting the move-operator domain



A further extension — multiple wh-movement and the SMC

- A potential **objection** against MG(+SMC)'s: you **cannot deal with multiple wh-movement**. /* example from Bulgarian */

ko_j kogo_j kakvo_k t_i e pital t_j t_k
who whom what AUX ask

- ◆ Recall the SMC-implementation in MGs: the number of competing licensee features triggering a movement is (finitely) bounded.
- **Answer**: we can, if we **implement the wh-cluster hypothesis** going back to Rudin (1988) such that we **introduce two new syntactic feature types and a corresponding operator**.

A further extension — multiple wh-movement and the SMC

- *c(luster)-licensees*: $\triangle x, \triangle y, \triangle z, \dots$
c(luster)-licensors: $\nabla x, \nabla y, \nabla z, \dots$

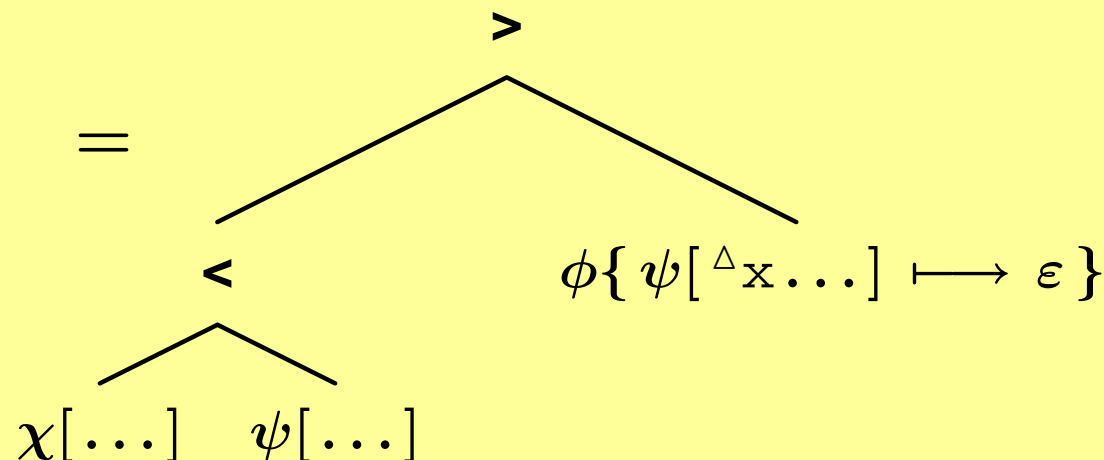
Structure building functions

$\text{cluster} : \text{Trees} \xrightarrow{\text{part}} 2^{\text{Trees}}$

■ $\phi \in \text{Domain}(\text{cluster}) : \iff$

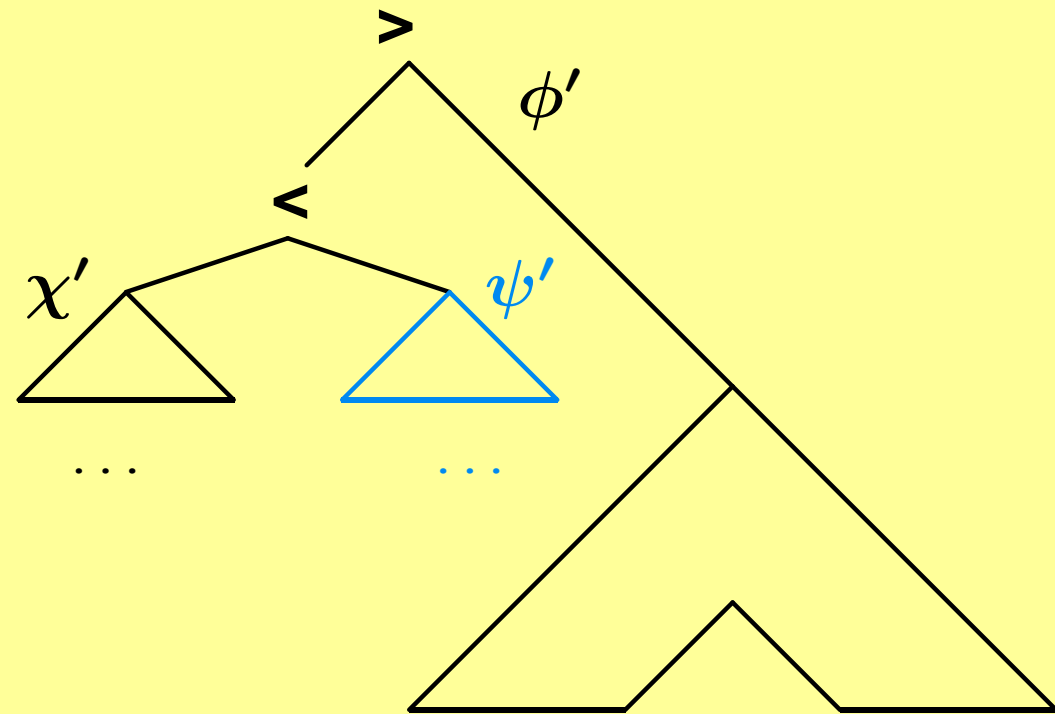
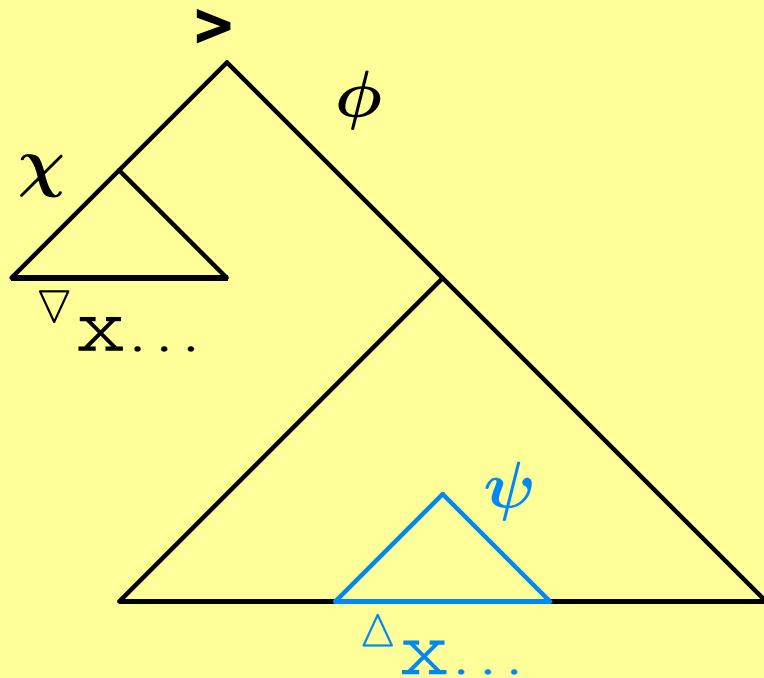
- The highest specifier χ of ϕ displays c-licensor $\nabla_{\mathbf{x}}$
- there is a (unique [SMC]) maximal projection ψ within ϕ that displays the corresponding c-licensee $\triangle_{\mathbf{x}}$

■ $\text{cluster}(\phi) =$



Structure building functions

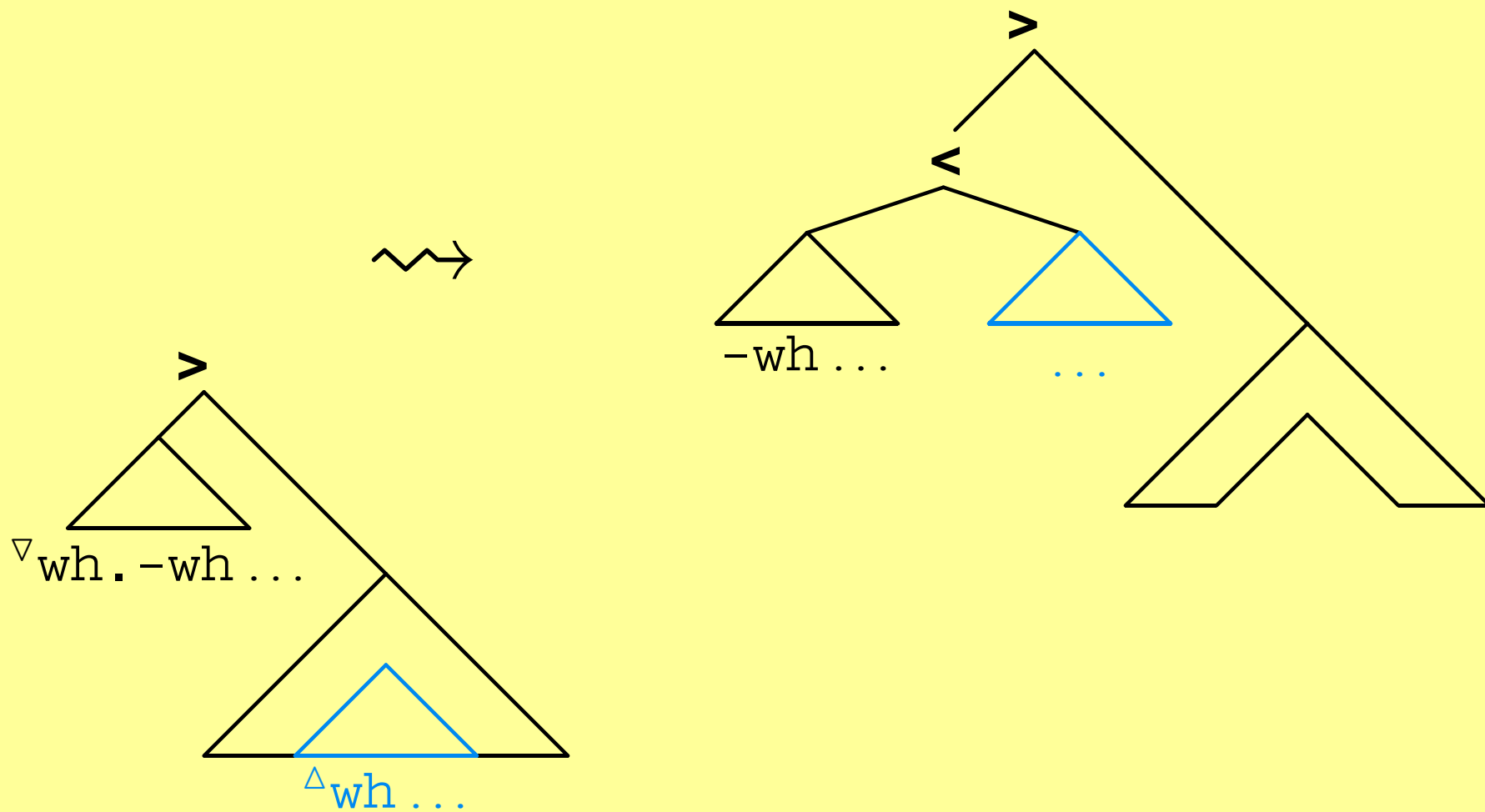
cluster : Trees $\xrightarrow{\text{part}}$ 2Trees



A further extension — multiple wh-movement and the SMC

- In order to outline the general case, we next sketch derivations for wh-clustering with two wh-phrases: crucially **exactly one $-wh$ licensee is necessary** for deriving a well-formed cluster, and **no more than one $\triangle wh$ is displayed at any derivation step**.

Wh-clustering, $n = 2$, crucial step 1



Wh-clustering, $n = 2$, crucial step 2

